

Computation

Visualization

**Programming** 

# Language Reference Manual

Version 5

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#### MATLAB Language Reference

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Printing History: December 1996 First printing (for MATLAB 5)

June 1997 Revised for 5.1 (online version)

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# **Command Summary**

This chapter lists MATLAB commands by functional area.

# **General Purpose Commands**

Managing	g Commands and Functions	
addpath	Add directories to MATLAB's search path	page 2-24
doc	Load hypertext documentation	page 2-199
hel p	Online help for MATLAB functions and M-files	page 2-350
lasterr	Last error message	page 2-408
lookfor	Keyword search through all help entries	page 2-425
path	Control MATLAB's directory search path	page 2-503
profile	Measure and display M-file execution profiles	page 2-533
rmpath	Remove directories from MATLAB's search path	page 2-57
type	List file	page 2-684
versi on	MATLAB version number	page 2-693
what	Directory listing of M-files, MAT-files, and MEX-files	page 2-701
whatsnew	Display README files for MATLAB and toolboxes	page 2-702
whi ch	Locate functions and files	page 2-70
Managing	g Variables and the Workspace	
clear	Remove items from memory	page 2-11
di sp	Display text or array	page 2-19
length	Length of vector	page 2-413
l oad	Retrieve variables from disk	page 2-410
pack	Consolidate workspace memory	page 2-499
save	Save workspace variables on disk	page 2-58
si ze	Array dimensions	page 2-59
who, whos	List directory of variables in memory	page 2-700
Controllin	g the Command Window	
echo	Echo M-files during execution	page 2-202
format	Control the output display format	
more	Control paged output for the command window	page 2-45
Working	with Files and the Operating Enviro	nment
асору	Copy Macintosh file from one folder to another	page 2-19
amove	Move Macintosh file from one folder to another	
appl escri pt	Load a compiled AppleScript from a file and execute it	
arename	Rename Macintosh File	
areveal	Reveal filename on Macintosh desktop	
cd	Change working directory	

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page 2-191

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page 2-203

	fileparts	Filename parts	page 2-254
	fullfile	Build full filename from parts	page 2-295
	gestal t	Macintosh gestalt function	page 2-330
	i nmem	Functions in memory	page 2-375
	matlabroot	Root directory of MATLAB installation	page 2-442
	tempdi r	Return the name of the system's temporary directory	page 2-674
	tempname	Unique name for temporary file	page 2-675
	!	Execute operating system command	page 2-13
	Starting	and Quitting MATLAB	
	matlabrc	MATLAB startup M-file	page 2-441
	qui t	Terminate MATLAB	page 2-547
	startup	MATLAB startup M-file	page 2-638
Operators	s and Speci	al Characters	
	+	Plus	page 2-2
	-	Minus	page 2-2
	*	Matrix multiplication	page 2-2
	. *	Array multiplication	page 2-2
	٨	Matrix power	page 2-2
	. ^	Array power	page 2-2
	kron	Kronecker tensor product	page 2-407
	\	Backslash or left division	page 2-2
	/	Slash or right division	page 2-2
	. / and . \	Array division, right and left	page 2-2
	:	Colon	page 2-16
	( )	Parentheses	page 2-13
	[ ]	Brackets	page 2-13
	{}	Curly braces	page 2-13
		Decimal point	page 2-13
		Continuation	page 2-13
	,	Comma	page 2-13
	;	Semicolon	page 2-13
	%	Comment	page 2-13
	!	Exclamation point	page 2-13
	1	Transpose and quote	page 2-13

Delete files and graphics objects.....

Save session in a disk file.....

Directory listing.....

Edit an M-file.....

del et e di ary

di r

edi t

	.' = == < > &   ~ xor	Nonconjugated transpose Assignment Equality Relational operators Logical AND Logical OR. Logical NOT Logical EXCLUSIVE OR	page 2-13 page 2-9 page 2-9 page 2-11 page 2-11
Logical Funct	tions		
	all any exist find is* *isa logical	Test to determine if all elements are nonzero.  Test for any nonzeros.  Check if a variable or file exists  Find indices and values of nonzero elements.  Detect state.  Detect an object of a given class.  Convert numeric values to logical.	page 2-32 page 2-231 page 2-258 page 2-398 page 2-402
		and Debugging s a Programming Language	
	builtin eval feval function global nargchk script	Execute builtin function from overloaded method	page 2-228 page 2-244 page 2-296 page 2-332 page 2-457
	Control Flo	ow	
	break case el se el sei f end	Break out of flow control structures	page 2-86 page 2-217 page 2-218 icate last in-
	error	dex	

Repeat statements a specific number of times . . . . . . page 2-276

for

Conditionally execute statements  Default part of switch statement  Return to the invoking function  Switch among several cases based on expression  Display warning message  Repeat statements an indefinite number of times	page 2-354 page 2-497 page 2-569 page 2-666 page 2-696 page 2-705
e Input	
Request user input.  Invoke the keyboard in an M-file.  Generate a menu of choices for user input.  Halt execution temporarily.	page 2-377 page 2-406 page 2-446 page 2-505
iented Programming	
Create object or return class of object Convert to double precision Inferior class relationship Construct an inline object Detect an object of a given class Superior class relationship Convert to unsigned 8-bit integer	page 2-110 page 2-200 page 2-371 page 2-372 page 2-402 page 2-661 page 2-685
g	
Clear breakpoints. Resume execution Change local workspace context Enable MEX-file debugging Quit debug mode. Display function call stack List all breakpoints Execute one or more lines from a breakpoint. Set breakpoints in an M-file function List M-file with line numbers Change local workspace context	page 2-148 page 2-150 page 2-151 page 2-155 page 2-156 page 2-157 page 2-158 page 2-159 page 2-162 page 2-163
	Default part of switch statement Return to the invoking function Switch among several cases based on expression Display warning message Repeat statements an indefinite number of times  Pipput Request user input. Invoke the keyboard in an M-file. Generate a menu of choices for user input. Halt execution temporarily.  Inferior class relationship Construct an inline object Detect an object of a given class Superior class relationship Convert to unsigned 8-bit integer  Clear breakpoints. Resume execution Change local workspace context Enable MEX-file debugging Quit debug mode. Display function call stack List all breakpoints Execute one or more lines from a breakpoint. Set breakpoints in an M-file function List M-file with line numbers

# **Elementary Matrices and Matrix Manipulation**

<b>Elementar</b>	y Matrices and Arrays	
eye	Identity matrix	page 2-238
linspace	Generate linearly spaced vectors	page 2-415
logspace	Generate logarithmically spaced vectors	page 2-424
ones	Create an array of all ones	page 2-495
rand	Uniformly distributed random numbers and arrays	page 2-549
randn	Normally distributed random numbers and arrays	page 2-551
zeros	Create an array of all zeros	page 2-715
: (colon)	Regularly spaced vector	page 2-16
Special Va	ariables and Constants	
ans	The most recent answer	page 2-31
computer	Identify the computer on which MATLAB is running	page 2-31
eps	Floating-point relative accuracy	page 2-113
flops	Count floating-point operations	page 2-266
i i	Imaginary unit	page 2-200 page 2-353
Inf	Infinity	page 2-330 page 2-370
i nput name	Input argument name	page 2-378
j	Imaginary unit	page 2-405
NaN	Not-a-Number	page 2-456
nargin, nargo		page 2 100
nargin, narge	Number of function arguments	page 2-458
pi	Ratio of a circle's circumference to its diameter, $\pi$	page 2-513
real max	Largest positive floating-point number	page 2-561
real mi n	Smallest positive floating-point number	page 2-562
	rargout	page 2 oo2
8,	Pass or return variable numbers of arguments	page 2-690
Time and	Dates	
cal endar	Calendar	page 2-82
clock	Current time as a date vector	page 2-113
cputime	Elapsed CPU time	page 2-136
date	Current date string	page 2-143
datenum	Serial date number	page 2-144
datestr	Date string format	page 2-145
datevec	Date components	page 2-147
eomday	End of month	page 2-221

Elapsed time......page 2-227

eti me

	now tic, toc weekday	Current date and time	page 2-470 page 2-676 page 2-700
	Matrix Ma	anipulation	
	cat diag fliplr flipud repmat reshape rot90 tril triu : (colon)	Concatenate arrays Diagonal matrices and diagonals of a matrix Flip matrices left-right. Flip matrices up-down Replicate and tile an array. Reshape array Rotate matrix 90 degrees. Lower triangular part of a matrix. Upper triangular part of a matrix Index into array, rearrange array	page 2-87 page 2-190 page 2-263 page 2-264 page 2-565 page 2-574 page 2-681 page 2-682 page 2-16
Specialized	Matrices		
	compan gallery hadamard hankel hilb invhilb magic pascal toeplitz wilkinson	Companion matrix Test matrices Hadamard matrix Hankel matrix Hilbert matrix Inverse of the Hilbert matrix Magic square Pascal matrix Toeplitz matrix Wilkinson's eigenvalue test matrix	page 2-118 page 2-306 page 2-344 page 2-352 page 2-396 page 2-438 page 2-502 page 2-677 page 2-708
Elementary	Math Fun	ctions	
	abs acos, acosh acot, acoth acsc, acsch angle asec, asech asin, asinh atan, atanh atan2	Absolute value and complex magnitude	page 2-18 page 2-20 page 2-21 page 2-22 page 2-30 page 2-37 page 2-38 page 2-40 page 2-42

	cei l	Round toward infinity	nage 2-91
	conj	Complex conjugate	
	cos, cosh	Cosine and hyperbolic cosine	
	cot, coth	Cotangent and hyperbolic cotangent	
	,		
	csc, csch	Cosecant and hyperbolic cosecant	
	exp	Exponential	
	fix	Round towards zero	
	floor	Round towards minus infinity	
	gcd	Greatest common divisor	
	i mag	Imaginary part of a complex number	
	l cm	Least common multiple	
	l og	Natural logarithm	page 2-418
	l og2	Base 2 logarithm and dissect floating-point numbers into ex	
		mantissa	
	l og 10	Common (base 10) logarithm	
	mod	Modulus (signed remainder after division)	
	real	Real part of complex number	
	rem	Remainder after division	
	round	Round to nearest integer	
	sec, sech	Secant and hyperbolic secant	page 2-587
	si gn	Signum function	page 2-594
	sin, sinh	Sine and hyperbolic sine	page 2-595
	sqrt	Square root	page 2-630
	tan, tanh	Tangent and hyperbolic tangent	
Specialized I	Math Fun	ctions	
•	a.;	Aim functions	nogo 9 95
	ai ry	Airy functions	
	besselh	Bessel functions of the third kind (Hankel functions)	page 2-49
	besseli, bess		naga 9 51
	1 1. 1	Modified Bessel functions	page z-51
	besselj, bess	Sel y	. 0.70
		Bessel functions	page 2-53
	beta, betaind	c, betaln	0.50
		Beta functions	
	ellipj	Jacobi elliptic functions	
	el l i pke	Complete elliptic integrals of the first and second kind	page 2-215
	erf, erfc, er		
		Error functions	
	expi nt	Exponential integral	page 2-234
	gamma, gammai		
		Gamma functions	page 2-326

	legendre pow2 rat, rats	Associated Legendre functions	page 2-411 page 2-530 page 2-555
Coordinat	te System (	Conversion	
	cart2pol cart2sph pol2cart sph2cart	Transform Cartesian coordinates to polar or cylindrical Transform Cartesian coordinates to spherical Transform polar or cylindrical coordinates to Cartesian	page 2-83 page 2-85 page 2-517 page 2-615
Matrix Fu	nctions - N	lumerical Linear Algebra	
	Matrix A	nalysis	
	cond	Condition number with respect to inversion	page 2-121
	condei g	Condition number with respect to eigenvalues	page 2-122
	det	Matrix determinant	page 2-189
	norm	Vector and matrix norms	page 2-468
	nul l	Null space of a matrix	page 2-471
	orth	Range space of a matrix	page 2-496
	rank	Rank of a matrix	page 2-554
	rcond	Matrix reciprocal condition number estimate	page 2-558
	rref, rrefm		
	_	Reduced row echelon form	page 2-576
	subspace	Angle between two subspaces	page 2-659
	trace	Sum of diagonal elements	page 2-678
	Linear Ed	quations	
	\ /	Linear equation solution	page 2-2
	chol	Cholesky factorization	page 2-103
	i nv	Matrix inverse	page 2-393
	lscov	Least squares solution in the presence of known covariance	page 2-427
	lu	LU matrix factorization	page 2-428
	nnls	Nonnegative least squares	page 2-464
	pi nv	Moore-Penrose pseudoinverse of a matrix	page 2-514
	qr	Orthogonal-triangular decomposition	page 2-539

	Eigenvalues and Singular Values		
	bal ance cdf2rdf ei g hess pol y qz rsf2csf schur syd	Improve accuracy of computed eigenvalues.  Convert complex diagonal form to real block diagonal form Eigenvalues and eigenvectors.  Hessenberg form of a matrix.  Polynomial with specified roots.  QZ factorization for generalized eigenvalues.  Convert real Schur form to complex Schur form  Schur decomposition.  Singular value decomposition	page 2-204 page 2-348 page 2-518 page 2-548 page 2-578 page 2-584
	Matrix F		1.0
	expm funm logm sqrtm	Matrix exponential	page 2-298 page 2-422
	Low Leve	el Functions	
	qrdel ete qri nsert	Delete column from QR factorization	
Data Analys	sis and F	ourier Transform Functions	
	Basic Op	erations	
	convhul l cumprod cumsum cumtrapz del aunay dsearch factor i npol ygon max	Convex hull Cumulative product Cumulative sum Cumulative trapezoidal numerical integration Delaunay triangulation Search for nearest point Prime factors Detect points inside a polygonal region Maximum elements of an array	page 2-128 page 2-139 page 2-140 page 2-141 page 2-185 page 2-201 page 2-240 page 2-376 page 2-443 page 2-444

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Minimum elements of an array . . . . . . page 2-452

All possible permutations..... page 2-511

Area of polygon..... page 2-521 Generate list of prime numbers . . . . . . . . . page 2-531

medi an

mi n

perms pol yarea

primes

prod sort sortrows std sum trapz tsearch voronoi	Product of array elements. Sort elements in ascending order Sort rows in ascending order Standard deviation Sum of array elements. Trapezoidal numerical integration Search for enclosing Delaunay triangle Voronoi diagram	page 2-532 page 2-599 page 2-600 page 2-639 page 2-660 page 2-679 page 2-683 page 2-694
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del 2 di ff gradi ent	Discrete Laplacian	page 2-182 page 2-192 page 2-338
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conv conv2 deconv filter	Convolution and polynomial multiplication	page 2-125 page 2-126 page 2-181 response page 2-255 page 2-257
Fourier Tr	ransforms	
abs angle cpl xpair fft fft2 fftshift	Absolute value and complex magnitude	page 2-18 page 2-30 page 2-135 page 2-245 page 2-248 pectrum
ifft ifft2 nextpow2 unwrap	Inverse one-dimensional fast Fourier transform	page 2-356 page 2-357 page 2-463 page 2-688

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VC	CLU	r Fu	ai ic	แบ	113

cross	Vector cross product	page 2-137
intersect	Set intersection of two vectors	page 2-392
ismember	Detect members of a set	page 2-403
setdiff	Return the set difference of two vectors	page 2-589
setxor	Set exclusive-or of two vectors	page 2-592
uni on	Set union of two vectors	page 2-686
uni que	Unique elements of a vector	page 2-687

# **Polynomial and Interpolation Functions**

## **Polynomials**

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Convert between partial fraction expansion and polynomial	coefficients
	page 2-567
Polynomial roots	page 2-572
	Deconvolution and polynomial division Polynomial with specified roots. Polynomial derivative Polynomial eigenvalue problem Polynomial curve fitting Polynomial evaluation Matrix polynomial evaluation Convert between partial fraction expansion and polynomial

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	fmi ns	Minimize a function of several variables	page 2-269
	fzero	Zero of a function of one variable	page 2-303
	ode45, ode23,	ode113, ode15s, ode23s	
		Solve differential equations	page 2-475
	odefile	Define a differential equation problem for ODE solvers	page 2-483
	odeget	Extract properties from options structure created with or 2-488	lesetpage
	odeset	Create or alter opt i ons structure for input to ODE solvers	s page 2-489
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	vectorize	Vectorize expression	page 2-692
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	Elementar	ry Sparse Matrices	
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	sprand	Sparse uniformly distributed random matrix	page 2-622
	sprandn	Sparse normally distributed random matrix	page 2-623
	sprandsym	Sparse symmetric random matrix	page 2-624
	Full to Spa	arse Conversion	
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	full	Convert sparse matrix to full matrix	page 2-294
	sparse	Create sparse matrix	page 2-605
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	Working v	with Nonzero Entries of Sparse Ma	trices
	nnz	Number of nonzero matrix elements	page 2-466
	nonzeros	Nonzero matrix elements	page 2-467
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	Visualizin	g Sparse Matrices	
	spy	Visualize sparsity pattern	page 2-629

		9 7 119 9 1 1 1 1 1 1 1 1	
	col mmd col perm dmperm randperm symmmd symrcm	Sparse column minimum degree permutation  Sparse column permutation based on nonzero count  Dulmage-Mendelsohn decomposition  Random permutation  Sparse symmetric minimum degree ordering  Sparse reverse Cuthill-McKee ordering	page 2-117 page 2-198 page 2-553 page 2-668
	Norm, Co	ndition Number, and Rank	
	condest	1-norm matrix condition number estimate	
	Sparse Sy	stems of Linear Equations	
	bicg bicgstab cgs cholinc gmres luinc pcg qmr	BiConjugate Gradients method	page 2-65 page 2-97 page 2-105 page 2-334 page 2-431 page 2-506
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	ei gs svds	Find a few eigenvalues and eigenvectors	
	Miscelland	eous	
	spparms	Set parameters for sparse matrix routines	page 2-619
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	General S	ound Functions	
	sound	Convert vector into sound	page 2-601
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	auread	Read NeXT/SUN (. au) sound file	page 2-43

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	.WAV SOL	and Functions	
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	readsnd recordsound soundcap speak writesnd	Read snd resources and files Record sound Sound capabilities Speak text string. Write snd resources and files	page 2-559 page 2-563 page 2-602 page 2-612 page 2-711
Character S	String Fund	ctions	
	General		
	abs	Absolute value and complex magnitude	page 2-18
	eval	Interpret strings containing MATLAB expressions	page 2-228
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	strings	MATLAB string handling	page 2-646
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	debl ank	Strip trailing blanks from the end of a string	page 2-177
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	lower	Convert string to lower case	page 2-426
	strcat	String concatenation	page 2-642
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	strj ust	Justify a character array	page 2-647
	strmatch	Find possible matches for a string	page 2-648
	strncmp	Compare the first n characters of two strings	page 2-649
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	Radix Cor	nversion	
	bi n2dec dec2bi n dec2hex hex2dec hex2num	Binary to decimal number conversion	page 2-179 page 2-180 page 2-350
Low-Level F	ile I/O Fu	nctions	
	File Open	ing and Closing	
	fclose fopen	Close one or more open files	
	Unformat	ted I/O	
	fread fwrite	Read binary data from file	
	Formatted	d I/O	
	fgetl	Return the next line of a file as a string without line terminal	
	fgets	Return the next line of a file as a string with line terminator(	$(\mathbf{s})$
	fprintf fscanf	Write formatted data to file	page 2-279
	File Positi	oning	
	feof ferror frewind fseek	Test for end-of-file	page 2-243 page 2-288

	ftell	Get file position indicator	page 2-293
	String Co	nversion	
	sprintf sscanf	Write formatted data to a string	page 2-625 page 2-635
	Specialize	ed File I/O	
	qtwrite dl mread dl mwrite imfinfo imread imwrite wk1read wk1write xl getrange xl setrange	Write QuickTime movie file to disk Read an ASCII delimited file into a matrix Write a matrix to an ASCII delimited file Return information about a graphics file Read image from graphics file Write an image to a graphics file Read a Lotus123 WK1 spreadsheet file into a matrix. Write a matrix to a Lotus123 WK1 spreadsheet file Get range of cells from Microsoft Excel worksheet Set range of cells in Microsoft Excel worksheet	page 2-544 page 2-196 page 2-197 page 2-360 page 2-363 page 2-709 page 2-710 page 2-712 page 2-713
Bitwise Fund	ctions		
	bitand bitcmp bitor bitmax bitset bitshift bitget bitxor	Bit-wise AND . Complement bits . Bit-wise OR . Maximum floating-point integer . Set bit . Bit-wise shift . Get bit . Bit-wise XOR .	page 2-70 page 2-71 page 2-74 page 2-73 page 2-75 page 2-76 page 2-72 page 2-77
Structure Fu	nctions		
	fieldnames getfield rmfield setfield struct struct2cell	Field names of a structure.  Get field of structure array  Remove structure fields.  Set field of structure array.  Create structure array.  Structure to cell array conversion	page 2-253 page 2-331 page 2-570 page 2-590 page 2-652 page 2-653

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cl ass	Create object or return class of object	page 2-110
i sa	Detect an object of a given class	page 2-402

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shi ftdi m	Shift dimensions page 2-5	
squeeze	Remove singleton dimensions page 2-6	
sub2i nd	Single index from subscripts page 2-6	

# Reference

This chapter describes all MATLAB operators, commands, and functions in alphabetical order.

### **Purpose**

Matrix and array arithmetic

## **Syntax**

A+D	
A-B	
A*B	A. *B
A/B	A. /B
$A \setminus B$	<b>A.</b> \ <b>B</b>
A^B	A. ^B
A'	A. '

Α . D

## **Description**

+ - \*

/ \ ^ MATLAB has two different types of arithmetic operations. Matrix arithmetic operations are defined by the rules of linear algebra. Array arithmetic operations are carried out element-by-element. The period character (.) distinguishes the array operations from the matrix operations. However, since the matrix and array operations are the same for addition and subtraction, the character pairs .+ and .- are not used.

- + Addition or unary plus. A+B adds A and B. A and B must have the same size, unless one is a scalar. A scalar can be added to a matrix of any size.
- Subtraction or unary minus. A–B subtracts B from A. A and B must have the same size, unless one is a scalar. A scalar can be subtracted from a matrix of any size.
- \* Matrix multiplication. C = A\*B is the linear algebraic product of the matrices A and B. More precisely,

$$C(i,j) = \sum_{k=1}^{n} A(i,k)B(k,j)$$

For nonscalar A and B, the number of columns of A must equal the number of rows of B. A scalar can multiply a matrix of any size.

- .\* Array multiplication. A.\*B is the element-by-element product of the arrays A and B. A and B must have the same size, unless one of them is a scalar.
- Slash or matrix right division. B/A is roughly the same as B\*i nv(A). More precisely,  $B/A = (A' \setminus B')'$ . See  $\setminus$ .

# Arithmetic Operators + - \* / \ ^ '

- Array right division. A. /B is the matrix with elements A(i,j)/B(i,j). A and B must have the same size, unless one of them is a scalar.
- Backslash or matrix left division. If A is a square matrix,  $A \setminus B$  is roughly the same as  $i \cdot nv(A) *B$ , except it is computed in a different way. If A is an n-by-n matrix and B is a column vector with n components, or a matrix with several such columns, then  $X = A \setminus B$  is the solution to the equation AX = B computed by Gaussian elimination (see "Algorithm" for details). A warning message prints if A is badly scaled or nearly singular.

If A is an m-by-n matrix with m  $\sim$ = n and B is a column vector with m components, or a matrix with several such columns, then X = A\B is the solution in the least squares sense to the under- or overdetermined system of equations AX = B. The effective rank, k, of A, is determined from the QR decomposition with pivoting (see "Algorithm" for details). A solution X is computed which has at most k nonzero components per column. If k < n, this is usually not the same solution as pi nv(A) \*B, which is the least squares solution with the smallest norm, |X| = A

- Array left division. A.  $\B$  is the matrix with elements B(i,j)/A(i,j). A and B must have the same size, unless one of them is a scalar.
- ^ Matrix power. X^p is X to the power p, if p is a scalar. If p is an integer, the power is computed by repeated multiplication. If the integer is negative, X is inverted first. For other values of p, the calculation involves eigenvalues and eigenvectors, such that if [V, D] = eig(X), then  $X^p = V*D$ . ^p/V.

If x is a scalar and P is a matrix,  $x^P$  is x raised to the matrix power P using eigenvalues and eigenvectors.  $X^P$ , where X and P are both matrices, is an error.

- Array power. A. ^B is the matrix with elements A(i,j) to the B(i,j) power. A and B must have the same size, unless one of them is a scalar.
- Matrix transpose. A' is the linear algebraic transpose of A. For complex matrices, this is the complex conjugate transpose.
- Array transpose. A. ' is the array transpose of A. For complex matrices, this does not involve conjugation.

# Arithmetic Operators + - \* / \ ^ '

## **Remarks** The arithmetic operators have M-file function equivalents, as shown:

Binary addition	A+B	plus(A, B)
Unary plus	+A	uplus(A)
Binary subtraction	A–B	minus(A, B)
Unary minus	-A	umi nus(A)
Matrix multiplication	A*B	mtimes(A, B)
Array-wise multiplication	A. *B	times(A,B)
Matrix right division	A/B	mrdi vi de(A, B)
Array-wise right division	A. /B	rdi vi de (A, B)
Matrix left division	$A \setminus B$	ml di vi de(A, B)
Array-wise left division	<b>A.</b> \ <b>B</b>	l di vi de(A, B)
Matrix power	A^B	mpower(A, B)
Array-wise power	A. ^B	power(A, B)
Complex transpose	A'	ctranspose(A)
Matrix transpose	A. '	transpose(A)

## **Examples**

Here are two vectors, and the results of various matrix and array operations on them, printed with format  $\mbox{rat}$ .

Matrix Operations		Array Operations		
x	1 2 3	у	4 5 6	
<b>x</b> '	1 2 3	у'	4 5 6	
x+y	5 7 9	х-у	-3 -3 -3	
x + 2	3 4 5	x-2	-1 0 1	
x * y	Error	x. *y	4 10 18	
x' *y	32	x' . *y	Error	
x*y'	4 5 6 8 10 12 12 15 18	x. *y'	Error	
x*2	2 4 6	x. *2	2 4 6	
<b>x</b> \ <b>y</b>	16/7	x. \y	4 5/2 2	
2\x	1/2 1 3/2	2. /x	2 1 2/3	

Matrix Operations		Array Operat	Array Operations	
x/y	0 0 1/6 0 0 1/3 0 0 1/2	x. /y	1/4 2/5 1/2	
x/2	1/2 1 3/2	x. /2	1/2 1 3/2	
x^y	Error	x. ^y	1 32 729	
x^2	Error	x. ^2	1 4 9	
2^x	Error	2. ^x	2 4 8	
(x+i *y) '	1 - 4i 2 -	5i 3 – 6i		
(x+i *y). '	1 + 4i 2 +	5i 3 + 6i		

## **Algorithm**

The specific algorithm used for solving the simultaneous linear equations denoted by  $X = A \setminus B$  and X = B / A depends upon the structure of the coefficient matrix A.

- If A is a triangular matrix, or a permutation of a triangular matrix, then X can be computed quickly by a permuted backsubstitution algorithm. The check for triangularity is done for full matrices by testing for zero elements and for sparse matrices by accessing the sparse data structure. Most nontriangular matrices are detected almost immediately, so this check requires a negligible amount of time.
- If A is symmetric, or Hermitian, and has positive diagonal elements, then a Cholesky factorization is attempted (see chol). If A is sparse, a symmetric minimum degree preordering is applied (see symmmd and spparms). If A is found to be positive definite, the Cholesky factorization attempt is successful and requires less than half the time of a general factorization. Nonpositive

definite matrices are usually detected almost immediately, so this check also requires little time. If successful, the Cholesky factorization is

$$A = R' *R$$

where R is upper triangular. The solution X is computed by solving two triangular systems,

$$X = R \setminus (R' \setminus B)$$

• If A is square, but not a permutation of a triangular matrix, or is not Hermitian with positive elements, or the Cholesky factorization fails, then a general triangular factorization is computed by Gaussian elimination with partial pivoting (see 1 u). If A is sparse, a nonsymmetric minimum degree preordering is applied (see col mmd and spparms). This results in

$$A = L*U$$

where L is a permutation of a lower triangular matrix and U is an upper triangular matrix. Then X is computed by solving two permuted triangular systems.

$$X = U \setminus (L \setminus B)$$

• If A is not square and is full, then Householder reflections are used to compute an orthogonal-triangular factorization.

$$A*P = Q*R$$

where P is a permutation, Q is orthogonal and R is upper triangular (see qr). The least squares solution X is computed with

$$X = P*(R\setminus(Q'*B)$$

• If A is not square and is sparse, then the augmented matrix is formed by:

$$S = [c*I A; A' 0]$$

The default for the residual scaling factor is c = max(max(abs(A)))/1000 (see spparms). The least squares solution X and the residual R = B-A\*X are computed by

$$S * [R/c; X] = [B; 0]$$

with minimum degree preordering and sparse Gaussian elimination with numerical pivoting.

The various matrix factorizations are computed by MATLAB implementations of the algorithms employed by LINPACK routines ZGECO, ZGEFA and ZGESL for

# Arithmetic Operators + - \* / \ ^ '

square matrices and ZQRDC and ZQRSL for rectangular matrices. See the *LINPACK Users' Guide* for details.

### **Diagnostics**

From matrix division, if a square A is singular:

Matrix is singular to working precision.

From element-wise division, if the divisor has zero elements:

Divide by zero.

On machines without IEEE arithmetic, like the VAX, the above two operations generate the error messages shown. On machines with IEEE arithmetic, only warning messages are generated. The matrix division returns a matrix with each element set to I  $\inf$ ; the element-wise division produces NaNs or I  $\inf$ s where appropriate.

If the inverse was found, but is not reliable:

Warning: Matrix is close to singular or badly scaled.

Results may be inaccurate. RCOND = xxx

From matrix division, if a nonsquare A is rank deficient:

Warning: Rank deficient, rank = xxx tol = xxx

#### See Also

det Matrix determinant i nv Matrix inverse

 $\begin{array}{ccc} l\,u & & LU\ matrix\ factorization \\ orth & & Range\ space\ of\ a\ matrix \end{array}$ 

qr Orthogonal-triangular decomposition

rref Reduced row echelon form

#### References

[1] Dongarra, J.J., J.R. Bunch, C.B. Moler, and G.W. Stewart, *LINPACK Users' Guide*, SIAM, Philadelphia, 1979.

### **Purpose**

#### Relational operations

## **Syntax**

$$A >= B$$

$$A == B$$

$$A \sim= B$$

## Description

The relational operators are <,  $\le$ , >,  $\ge$ , ==, and  $\sim$ =. Relational operators perform element-by-element comparisons between two arrays. They return an array of the same size, with elements set to logical true (1) where the relation is true, and elements set to logical false (0) where it is not.

The operators <,  $\le$ , >, and  $\ge$  use only the real part of their operands for the comparison. The operators == and  $\sim=$  test real and imaginary parts.

The relational operators have precedence midway between the logical operators and the arithmetic operators.

To test if two strings are equivalent, use strcmp, which allows vectors of dissimilar length to be compared.

## **Examples**

If one of the operands is a scalar and the other a matrix, the scalar expands to the size of the matrix. For example, the two pairs of statements:

$$X = 5$$
;  $X >= [1 2 3; 4 5 6; 7 8 10]$   
 $X = 5*ones(3,3); X >= [1 2 3; 4 5 6; 7 8 10]$ 

produce the same result:

# **Relational Operators < > <= >= == ~=**

**See Also** Logical Operators &  $\mid \sim$ 

all Test to determine if all elements are nonzero

any Test for any nonzeros

find Find indices and values of nonzero elements

strcmp Compare strings

**Purpose** 

Logical operations

**Syntax** 

A & B
A | B
~A

#### Description

The symbols &, |, and  $\sim$  are the logical operators AND, OR, and NOT. They work element-wise on arrays, with 0 representing logical false (F), and anything nonzero representing logical true (T). The & operator does a logical AND, the | operator does a logical OR, and  $\sim$ A complements the elements of A. The function xor(A, B) implements the exclusive OR operation. Truth tables for these operators and functions follow.

Inputs A	В	and A&B	or A B	xor xor(A, B)	NOT ~A
0	0	0	0	0	1
0	1	0	1	1	1
1	0	0	1	1	0
1	1	1	1	0	0

The logical operators have the lowest precedence, with arithmetic operators and relational operators being evaluated first.

The precedence for the logical operators with respect to each other is:

1 not has the highest precedence.

2 and and or have equal precedence, and are evaluated from left to right.

#### Remarks

The logical operators have M-file function equivalents, as shown:

and	A&B	and(A, B)
or	A   B	or(A, B)
not	~A	not (A)

## **Examples**

Here are two scalar expressions that illustrate precedence relationships for arithmetic, relational, and logical operators:

$$1 \& 0 + 3$$
  
 $3 > 4 \& 1$ 

They evaluate to 1 and 0 respectively, and are equivalent to:

Here are two examples that illustrate the precedence of the logical operators to each other:

#### See Also

The relational operators: <, <=, >=, ==,  $\sim=$ , as well as:

al l Test to determine if all elements are nonzero any Test for any nonzeros find Find indices and values of nonzero elements logical Convert numeric values to logical xor Exclusive or

**Purpose** Special characters

**Syntax** [ ] ( ) {} = ' . . . . , ; %!

### Description

Brackets are used to form vectors and matrices. [6.99.64 sqrt(-1)] is a vector with three elements separated by blanks. [6.9,9.64,i] is the same thing. [1+j2-j3] and [1+j2-j3] are not the same. The first has three elements, the second has five.

[  $11\ 12\ 13;\ 21\ 22\ 23$  ] is a 2-by-3 matrix. The semicolon ends the first row.

Vectors and matrices can be used inside [ ] brackets. [A B; C] is allowed if the number of rows of A equals the number of rows of B and the number of columns of A plus the number of columns of B equals the number of columns of C. This rule generalizes in a hopefully obvious way to allow fairly complicated constructions.

A = [ ] stores an empty matrix in A. A(m,:) = [ ] deletes row m of A. A(:,n) = [ ] deletes column n of A. A(n) = [ ] reshapes A into a column vector and deletes the third element.

[A1, A2, A3...] = function assigns function output to multiple variables.

For the use of [ and ] on the left of an "=" in multiple assignment statements, see lu, eig, svd, and so on.

{ } Curly braces are used in cell array assignment statements. For example.,

 $A(2, 1) = \{[1\ 2\ 3;\ 4\ 5\ 6]\}, or A\{2, 2\} = ('str').$  See help paren for more information about  $\{ \}.$ 

# Special Characters [](){} = ' . ... , ; %!

- ( ) Parentheses are used to indicate precedence in arithmetic expressions in the usual way. They are used to enclose arguments of functions in the usual way. They are also used to enclose subscripts of vectors and matrices in a manner somewhat more general than usual. If X and V are vectors, then X(V) is  $[X(V(1)), X(V(2)), \ldots, X(V(n))]$ . The components of V must be integers to be used as subscripts. An error occurs if any such subscript is less than 1 or greater than the size of X. Some examples are
  - X(3) is the third element of X.
  - X([1 2 3]) is the first three elements of X.

See help paren for more information about ( ).

If X has n components, X(n:-1:1) reverses them. The same indirect subscripting works in matrices. If V has m components and W has n components, then A(V, W) is the m-by-n matrix formed from the elements of A whose subscripts are the elements of V and W For example, A([1,5],:) = A([5,1],:) interchanges rows 1 and 5 of A.

- Used in assignment statements. B = A stores the elements of A in B.
   is the relational equals operator. See the Relational Operators page.
- Matrix transpose. X' is the complex conjugate transpose of X. X. ' is the nonconjugate transpose.

Quotation mark. 'any text' is a vector whose components are the ASCII codes for the characters. A quotation mark within the text is indicated by two quotation marks.

- Decimal point. 314/100, 3.14 and .314e1 are all the same. Element-by-element operations. These are obtained using .\*,  $.^{\wedge}$ , ./, or  $. \setminus .$  See the Arithmetic Operators page.
- . Field access. A. (field) and A(i). field, when A is a structure, access the contents of field.
- .. Parent directory. See cd.
- ... Continuation. Three or more points at the end of a line indicate continuation.

## Special Characters [](){} = ' . ... , ; %!

- Comma. Used to separate matrix subscripts and function arguments. Used to separate statements in multistatement lines. For multi-statement lines, the comma can be replaced by a semicolon to suppress printing.
- Semicolon. Used inside brackets to end rows. Used after an expression or statement to suppress printing or to separate statements.
- Percent. The percent symbol denotes a comment; it indicates a logical end of line. Any following text is ignored. MATLAB displays the first contiguous comment lines in a M-file in response to a help command.
- ! Exclamation point. Indicates that the rest of the input line is issued as a command to the operating system.

#### Remarks

Some uses of special characters have M-file function equivalents, as shown:

Horizontal concatenation	[A, B, C ]	horzcat(A, B, C)
Vertical concatenation	[A; B; C ]	vertcat(A, B, C)
Subscript reference	A(i,j,k)	$subsref(A,S).Seehelp\\subsref.$
Subscript assignment	A(i,j,k) = B	subsasgn(A, S, B). See hel p

#### See Also

Arithmetic, relational, and logical operators.

## Colon:

### **Purpose**

Create vectors, array subscripting, and for iterations

### Description

The colon is one of the most useful operators in MATLAB. It can create vectors, subscript arrays, and specify for iterations.

The colon operator uses the following rules to create regularly spaced vectors:

```
\begin{array}{lll} j:k & \text{is the same as } [j\,,j\,+1,\ldots\,,k] \\ \\ j:k & \text{is empty if } j>k \\ \\ j:i:k & \text{is the same as } [j\,,j\,+i\,,j\,+2i\,,\ldots\,,k] \\ \\ j:i:k & \text{is empty if } i>0 \text{ and } j>k \text{ or if } i<0 \text{ and } j< k \end{array}
```

where i,j, and k are all scalars.

Below are the definitions that govern the use of the colon to pick out selected rows, columns, and elements of vectors, matrices, and higher-dimensional arrays:

A(:,j)	is the j -th column of A
A(i,:)	is the i -th row of A
A(:,:)	is the equivalent two-dimensional array. For matrices this is the same as ${\tt A}. \\$
A(j:k)	is $A(j)$ , $A(j+1)$ ,, $A(k)$
A(:,j:k)	is $A(:,j)$ , $A(:,j+1)$ ,, $A(:,k)$
A(:,:,k)	is the kth page of three-dimensional array A.
A(i, j, k,:)	is a vector in four-dimensional array A. The vector includes $A(i,j,k,1),A(i,j,k,2),A(i,j,k,3),$ and so on.
A(:)	is all the elements of A, regarded as a single column. On the left side of an assignment statement, $A(:)$ fills A, preserving its shape from before. In this case, the right side must contain the same number of elements as A.

**Examples** 

Using the colon with integers,

$$D = 1:4$$

results in

$$D = 1 2 3 4$$

Using two colons to create a vector with arbitrary real increments between the elements,

$$E = 0:.1:.5$$

results in

The command

$$A(:,:,2) = pascal(3)$$

generates a three-dimensional array whose first page is all zeros. \\

$$\begin{array}{rcl} A(:\,,:\,,\,2) & = & & \\ & 1 & 1 & 1 \\ & 1 & 2 & 3 \\ & 1 & 3 & 6 \end{array}$$

See Also

for linspace logspace reshape Repeat statements a specific number of times Generate linearly spaced vectors Generate logarithmically spaced vectors Reshape array

## abs

**Purpose** Absolute value and complex magnitude

Syntax Y = abs(X)

**Description** abs(X) returns the absolute value, |X|, for each element of X.

If X is complex, abs(X) returns the complex modulus (magnitude):

 $abs(X) = sqrt(real(X).^2 + imag(X).^2)$ 

**Examples** abs(-5) = 5

abs(3+4i) = 5

**See Also** angle Phase angle

si gn Signum function
unwrap Correct phase angles

**Purpose** Copy Macintosh file from one folder to another

**Syntax** acopy(filename, foldername)

**Description** acopy(filename, foldername) copies the file filename to the folder

foldername. Both filename and foldername can be full or partial path names.

**See Also** amove Move Macintosh file from one folder to another

appl escript Load a compiled AppleScript from a file and execute it

arename Rename Macintosh File

areveal Reveal filename on Macintosh desktop

## acos, acosh

**Purpose** 

Inverse cosine and inverse hyperbolic cosine

**Syntax** 

Y = acos(X)Y = acosh(X)

Description

The acos and acosh functions operate element-wise on arrays. The functions' domains and ranges include complex values. All angles are in radians.

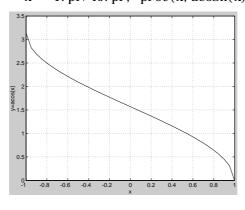
Y = acos(X) returns the inverse cosine (arccosine) for each element of X. For real elements of X in the domain [-1,1], acos(X) is real and in the range  $[0,\pi]$ . For real elements of X outside the domain [-1,1], acos(X) is complex.

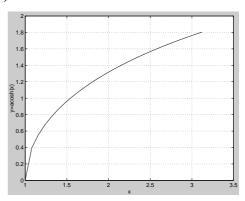
Y = acosh(X) returns the inverse hyperbolic cosine for each element of X.

**Examples** 

Graph the inverse cosine function over the domain  $-1 \le x \le 1$ , and the inverse hyperbolic cosine function over the domain  $1 \le x \le \pi$ .

$$x = -1:.05:1$$
; plot(x, acos(x))  
 $x = 1: pi/40: pi$ ; plot(x, acosh(x))





**Algorithm** 

$$\cos^{-1}(z) = -i \log \left[z + i(1-z^2)^{\frac{1}{2}}\right]$$

$$\cosh^{-1}(z) = \log \left[ z + (z^{2} - 1)^{\frac{1}{2}} \right]$$

See Also

cos, cosh

Cosine and hyperbolic cosine

Inverse cotangent and inverse hyperbolic cotangent

**Syntax** 

$$Y = acot(X)$$
  
 $Y = acoth(X)$ 

**Description** 

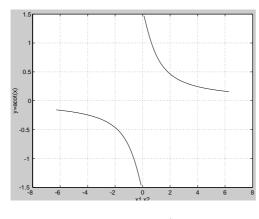
The acot and acoth functions operate element-wise on arrays. The functions' domains and ranges include complex values. All angles are in radians.

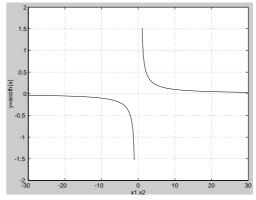
Y = acot(X) returns the inverse cotangent (arccotangent) for each element of X.

Y = acoth(X) returns the inverse hyperbolic cotangent for each element of X.

**Examples** 

Graph the inverse cotangent over the domains  $-2\pi \le x < 0$  and  $0 < x \le 2\pi$ , and the inverse hyperbolic cotangent over the domains  $-30 \le x < -1$  and  $1 < x \le 30$ .





**Algorithm** 

$$\cot^{-1}(z) = \tan^{-1}\left(\frac{1}{z}\right)$$

$$\coth^{-1}(z) = \tanh^{-1}\left(\frac{1}{z}\right)$$

See Also

cot, coth

Cotangent and hyperbolic cotangent

## acsc, acsch

**Purpose** 

Inverse cosecant and inverse hyperbolic cosecant

**Syntax** 

$$Y = acsc(X)$$
  
 $Y = acsch(X)$ 

**Description** 

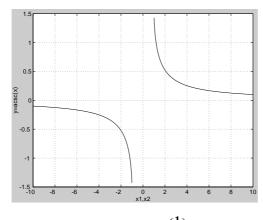
The acsc and acsch functions operate element-wise on arrays. The functions' domains and ranges include complex values. All angles are in radians.

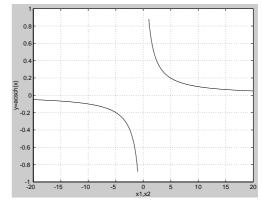
Y = acsc(X) returns the inverse cosecant (arccosecant) for each element of X.

Y = acsch(X) returns the inverse hyperbolic cosecant for each element of X.

**Examples** 

Graph the inverse cosecant over the domains  $-10 \le x < -1$  and  $1 < x \le 10$ , and the inverse hyperbolic cosecant over the domains  $-20 \le x \le -1$  and  $1 \le x \le 20$ .





**Algorithm** 

$$\csc^{-1}(z) = \sin^{-1}\left(\frac{1}{z}\right)$$

$$\operatorname{csch}^{-1}(z) = \sinh^{-1}\left(\frac{1}{z}\right)$$

See Also

csc, csch

Cosecant and hyperbolic cosecant

## addpath

**Purpose** Add directories to MATLAB's search path **Syntax** addpath(' di rectory') addpath('dir1', 'dir2', 'dir3', ...)addpath(...,'-flag') **Description** addpath ('directory') prepends the specified directory to MATLAB's current search path. addpath ('dir1', 'dir2', 'dir3',...) prepends all the specified directories to the path. addpath (..., '-flag') either prepends or appends the specified directories to the path depending the value of flag: 0 or begin Prepend specified directories 1 or end Append specified directories **Examples** path MATLABPATH c: \matl ab\tool box\general c: \matl ab\tool box\ops c: \matlab\toolbox\strfun addpath('c:\matlab\myfiles') path MATLABPATH c: \matlab\myfiles c: \matl ab\tool box\general c: \matlab\toolbox\ops c: \matlab\toolbox\strfun See Also Control MATLAB's directory search path path Remove directories from MATLAB's search rmpath path

Airy functions

**Syntax** 

$$W = \operatorname{airy}(Z)$$

$$W = \operatorname{airy}(k, Z)$$

$$[W, i \operatorname{err}] = \operatorname{airy}(k, Z)$$

**Definition** 

The Airy functions form a pair of linearly independent solutions to:

$$\frac{d^2W}{dZ^2} - ZW = 0$$

The relationship between the Airy and modified Bessel functions is:

$$Ai(Z) = \left[\frac{1}{\pi}\sqrt{Z/3}\right] K_{1/3}(\zeta)$$
 
$$Bi(Z) = \sqrt{Z/3} \left[I_{-1/3}(\zeta) + I_{1/3}(\zeta)\right]$$

where,

$$\zeta = \frac{2}{3}Z^{3/2}$$

**Description** 

 $W = \operatorname{airy}(Z)$  returns the Airy function,  $\operatorname{Ai}(Z)$ , for each element of the complex array Z.

 $W = ai \, ry(k, Z)$  returns different results depending on the value of k:

k	Returns
0	The same result as ai $ry(Z)$ .
1	The derivative, $Ai'(Z)$ .
2	The Airy function of the second kind, $Bi(Z)$ .
3	The derivative, $Bi'(Z)$ .

[W, ierr] = airy(k, Z) also returns an array of error flags.

ierr = 1	Illegal arguments.
ierr = 2	Overflow. Return Inf.
ierr = 3	Some loss of accuracy in argument reduction.
ierr = 4	Unacceptable loss of accuracy, Z too large.
ierr = 5	No convergence. Return NaN.

### See Also

bessel i	Modified Bessel functions of the first kind
besselj	Bessel functions of the first kind
bessel k	Modified Bessel functions of the third kind
bessely	Bessel functions of the second kind

#### References

[1] Amos, D. E., "A Subroutine Package for Bessel Functions of a Complex Argument and Nonnegative Order," *Sandia National Laboratory Report*, SAND85-1018, May, 1985.

[2] Amos, D. E., "A Portable Package for Bessel Functions of a Complex Argument and Nonnegative Order," *Trans. Math. Software*, 1986.

Test to determine if all elements are nonzero

#### **Syntax**

$$B = all(A)$$
  
 $B = all(A, dim)$ 

### Description

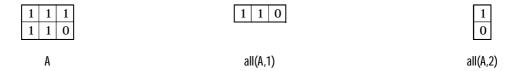
B = all(A) tests whether *all* the elements along various dimensions of an array are nonzero or logical true (1).

If A is a vector, all (A) returns logical true (1) if all of the elements are nonzero, and returns logical false (0) if one or more elements are zero.

If A is a matrix, all (A) treats the columns of A as vectors, returning a row vector of 1s and 0s.

If A is a multidimensional array, all (A) treats the values along the first non-singleton dimension as vectors, returning a logical condition for each vector.

B = all(A, dim) tests along the dimension of A specified by scalar dim.



## **Examples**

Given,

$$A = [0.53 \ 0.67 \ 0.01 \ 0.38 \ 0.07 \ 0.42 \ 0.69]$$

then B = (A < 0.5) returns logical true (1) only where A is less than one half:

The all function reduces such a vector of logical conditions to a single condition. In this case, all (B) yields 0.

This makes all particularly useful in if statements,

where code is executed depending on a single condition, not a vector of possibly conflicting conditions.

Applying the all function twice to a matrix, as in all(all(A)), always reduces it to a scalar condition.

```
all(all(eye(3)))
ans =
0
```

### See Also

The logical operators: &, |, ~, and:

any

Test for any nonzeros

Other functions that collapse an array's dimensions include:

max, mean, median, min, prod, std, sum, trapz

**Purpose** Move Macintosh file from one folder to another

**Syntax** amove (filename, foldername)

**Description** amove (filename, foldername) moves the file filename to the folder

foldername. Both filename and foldername can be full or partial path names.

See Also acopy Copy Macintosh file from one folder to another

appl escript Load a compiled AppleScript from a file and execute it

arename Rename Macintosh File

areveal Reveal filename on Macintosh desktop

## angle

**Purpose** Phase angle **Syntax** P = angle(Z)**Description** P = angle(Z) returns the phase angles, in radians, for each element of complex array Z. The angles lie between  $\pm \pi$ . For complex Z, the magnitude and phase angle are given by % magnitude R = abs(Z)theta = angle(Z)% phase angle and the statement Z = R. \*exp(i \*theta)converts back to the original complex Z. **Examples** Z =1. 0000 - 1. 0000i 2. 0000 + 1. 0000i 3. 0000 - 1. 0000i 4.0000 + 1.0000i 1. 0000 + 2. 0000i 2. 0000 - 2. 0000i 3. 0000 + 2. 0000i 4. 0000 - 2. 0000i 1. 0000 - 3. 0000i 2. 0000 + 3. 0000i 3. 0000 - 3. 0000i 4. 0000 + 3. 0000i 1. 0000 + 4. 0000i 2. 0000 - 4. 0000i 3. 0000 + 4. 0000i 4. 0000 - 4. 0000i P = angle(Z)P =-0.3218-0.78540.4636 0.2450 1.1071 -0.78540. 5880 -0.4636-1.24900.9828 -0.78540.6435 1.3258 -1.10710.9273 -0.7854

**Algorithm** 

angle can be expressed as:

$$angle(z) = i mag(log(z)) = atan2(i mag(z), real(z))$$

See Also

abs unwrap Absolute value and complex magnitude Correct phase angles

**Purpose** The most recent answer

Syntax ans

**Description** The ans variable is created automatically when no output argument is speci-

fied.

**Examples** The statement

2+2

is the same as

ans = 2+2

Test for any nonzeros

#### Syntax

$$B = any(A)$$
  
 $B = any(A, dim)$ 

### Description

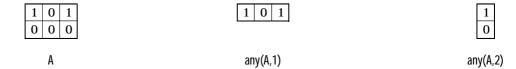
B = any(A) tests whether *any* of the elements along various dimensions of an array are nonzero or logical true (1).

If A is a vector, any(A) returns logical true (1) if any of the elements of A are nonzero, and returns logical false (0) if all the elements are zero.

If A is a matrix, any (A) treats the columns of A as vectors, returning a row vector of 1s and 0s.

If A is a multidimensional array, any(A) treats the values along the first non-singleton dimension as vectors, returning a logical condition for each vector.

B = any(A, dim) tests along the dimension of A specified by scalar dim.



## **Examples**

Given,

$$A = [0.53 \ 0.67 \ 0.01 \ 0.38 \ 0.07 \ 0.42 \ 0.69]$$

then B = (A < 0.5) returns logical true (1) only where A is less than one half:

$$0 \quad 0 \quad 1 \quad 1 \quad 1 \quad 1 \quad 0$$

The any function reduces such a vector of logical conditions to a single condition. In this case, any (B) yields 1.

This makes any particularly useful in if statements,

```
if any(A < 0.5)
    do something
end</pre>
```

where code is executed depending on a single condition, not a vector of possibly conflicting conditions.

Applying the any function twice to a matrix, as in any (any(A)), always reduces it to a scalar condition.

```
any(any(eye(3)))
ans =
1
```

See Also

The logical operators &, |,  $\sim$ , and:

al l Test to determine if all elements are nonzero Other functions that collapse an array's dimensions include:

max, mean, medi an, mi n, prod, std, sum, trapz

Load a compiled AppleScript from a file and execute it

#### Syntax

```
appl escri pt (filename)
appl escri pt (filename '-useEnglish')
result = appl escri pt (filename)
appl escri pt (filename, 'VarName1', 'VarValue1', ...)
```

#### Description

appl escript (filename) loads a compiled AppleScript from the file filename and executes it. If filename is not a full path name, then appl escript searches for filename along the MATLAB path.

appl escri pt (filename '-useEnglish') forces appl escri pt to use the English AppleScript dialect when compiling both the script in filename and any AppleScript variables passed to the script. By default, appl escri pt uses the current system AppleScript dialect, which can be set with (for example) the Script Editor application.

result = appl escript (filename) returns in result the value that the AppleScript returns, converted to a string.

appl escript (fil ename, 'VarName1', 'VarValue1',...) sets the value of the AppleScript's property or variable whose name is specified in VarName to the value specified in VarValue.

#### Remarks

appl escript is available on the Macintosh only.

### **Examples**

Compile an AppleScript and save it to the file rename:

```
tell application "Finder"
   set name of item itemName to newName
end tell
```

The appl escript command renames file hello on volume MyDisk to the new name world.

**Purpose** Rename Macintosh File

**Syntax** arename(oldfilename, newname)

**Description** arename (oldfilename, newname) renames the file oldfilename to have the

name newname. ol dfil ename can be a full or partial path name.

See Also acopy Copy Macintosh file from one folder to another

amove Move Macintosh file from one folder to another

areveal Reveal filename on Macintosh desktop

appl escript Load a compiled AppleScript from a file and execute it

## areveal

**Purpose** Reveal filename on Macintosh desktop

**Syntax** areveal (filename)

**Description** are veal (filename) opens the window of the folder containing filename on

the Macintosh desktop. filename can be a full orpartial path name.

See Also acopy Copy Macintosh file from one folder to another

amove Move Macintosh file from one folder to another

appl escript Load a compiled AppleScript from a file and execute it

arename Rename Macintosh File

Inverse secant and inverse hyperbolic secant

**Syntax** 

$$Y = asec(X)$$
  
 $Y = asech(X)$ 

**Description** 

The asec and asech functions operate element-wise on arrays. The functions' domains and ranges include complex values. All angles are in radians.

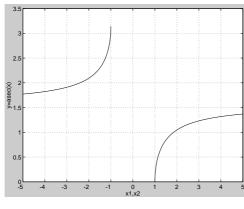
Y = asec(X) returns the inverse secant (arcsecant) for each element of X.

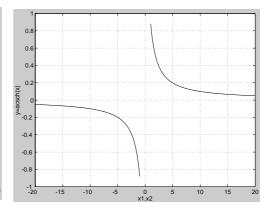
Y = asech(X) returns the inverse hyperbolic secant for each element of X.

**Examples** 

Graph the inverse secant over the domains  $1 \le x \le 5$  and  $-5 \le x \le -1$ , and the inverse hyperbolic secant over the domain  $0 < x \le 1$ .

$$x1 = -5:0.01:-1; x2 = 1:0.01:5;$$
  
 $plot(x1, asec(x1), x2, asec(x2))$   
 $x = 0.01:0.001:1; plot(x, asech(x))$ 





**Algorithm** 

$$\sec^{-1}(z) = \cos^{-1}\left(\frac{1}{z}\right)$$

$$\mathrm{sech}^{-1}(z) = \mathrm{cosh}^{-1}\left(\frac{1}{z}\right)$$

See Also

sec, sech

Secant and hyperbolic secant

## asin, asinh

**Purpose** 

Inverse sine and inverse hyperbolic sine

**Syntax** 

Y = asi n(X)Y = asi nh(X)

**Description** 

The asi n and asi nh functions operate element-wise on arrays. The functions' domains and ranges include complex values. All angles are in radians.

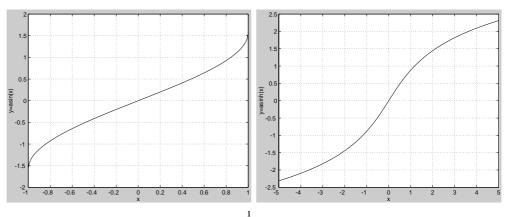
 $Y = asi\ n(X)$  returns the inverse sine (arcsine) for each element of X. For real elements of X in the domain [-1,1],  $asi\ n(X)$  is in the range  $[-\pi/2,\pi/2]$ . For real elements of X outside the range [-1,1],  $asi\ n(X)$  is complex.

Y = asi nh(X) returns the inverse hyperbolic sine for each element of X.

**Examples** 

Graph the inverse sine function over the domain  $-1 \le x \le 1$ , and the inverse hyperbolic sine function over the domain  $-5 \le x \le 5$ .

$$x = -1:.01:1$$
; plot(x, asin(x))  
 $x = -5:.01:5$ ; plot(x, asinh(x))



**Algorithm** 

$$\sin^{-1}(z) = -i \log \left[ iz + (1 - z^{2})^{\frac{1}{2}} \right]$$
  
$$\sinh^{-1}(z) = \log \left[ z + (z^{2} + 1)^{\frac{1}{2}} \right]$$

See Also

si n, si nh

Sine and hyperbolic sine

**Purpose** Assign value to variable in workspace

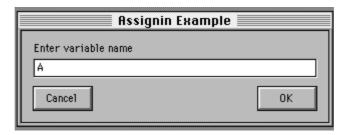
**Syntax** assignin(ws, 'name', v)

 $\textbf{Description} \qquad \quad \text{assigni n(ws, 'name', v)} \quad \text{assigns the variable '} \quad \text{name' in the workspace ws the} \\$ 

value v. 'name' is created if it doesn't exist. ws can be either 'caller' or 'base'.

**Examples** Here's a function that creates a variable with a user-chosen name in the base workspace. The variable is assigned the value  $\sqrt{\pi}$ .

function sqpi
var = inputdlg('Enter variable name','Assignin Example',1,{'A'})
assignin('base','var',sqrt(pi))



See Also evalin

Evaluate expression in workspace.

## atan, atanh

**Purpose** 

Inverse tangent and inverse hyperbolic tangent

Syntax

Y = atan(X)Y = atanh(X)

Description

The atan and atanh functions operate element-wise on arrays. The functions' domains and ranges include complex values. All angles are in radians.

Y = atan(X) returns the inverse tangent (arctangent) for each element of X.

For real elements of X, at an(X) is in the range  $[-\pi/2, \pi/2]$ .

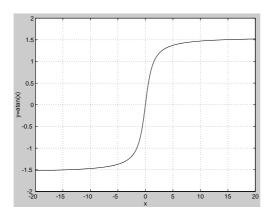
Y = atanh(X) returns the inverse hyperbolic tangent for each element of X.

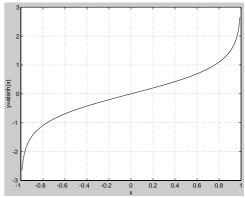
**Examples** 

Graph the inverse tangent function over the domain  $-20 \le x \le 20$ , and the inverse hyperbolic tangent function over the domain -1 < x < 1.

x = -20: 0.01: 20; plot(x, atan(x))

x = -0.99: 0.01: 0.99; plot(x, atanh(x))





**Algorithm** 

$$\tan^{-1}(z) = \frac{i}{2} \log \left( \frac{i+z}{i-z} \right)$$

$$tanh^{-1}(z) = \frac{1}{2} log \left(\frac{1+z}{1-z}\right)$$

See Also

at an2

Four-quadrant inverse tangent

tan, tanh

Tangent and hyperbolic tangent

Four-quadrant inverse tangent

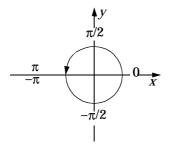
**Syntax** 

P = atan2(Y, X)

**Description** 

P = atan2(Y, X) returns an array P the same size as X and Y containing the element-by-element, four-quadrant inverse tangent (arctangent) of the real parts of Y and X. Any imaginary parts are ignored.

Elements of P lie in the half-open interval  $[-\pi, \pi]$ . The specific quadrant is determined by  $si\ gn(Y)$  and  $si\ gn(X)$ :



This contrasts with the result of atan(Y/X), which is limited to the interval  $[-\pi/2, \pi/2]$ , or the right side of this diagram.

**Examples** 

Any complex number z = x+iy is converted to polar coordinates with

```
r = abs(z)
theta = atan2(i mag(z), real(z))
```

To convert back to the original complex number:

```
z = r *exp(i *theta)
```

This is a common operation, so MATLAB provides a function, angle (z), that simply computes at an 2(i mag(z), real(z)).

See Also

atan, atanh tan, tanh Inverse tangent and inverse hyperbolic tangent Tangent and hyperbolic tangent

Read NeXT/SUN (. au) sound file

### Syntax

```
y = auread(aufile)
[y, Fs, bits] = auread(aufile)
[...] = auread(aufile, N)
[...] = auread(aufile, [N1, N2])
siz = auread(aufile, 'size')
```

### Description

Supports multi-channel data in the following formats:

- 8-bit mu-law
- 8-, 16-, and 32-bit linear
- floating-point

y = auread(aufile) loads a sound file specified by the string aufile, returning the sampled data in y. The . au extension is appended if no extension is given. Amplitude values are in the range [-1, +1].

[y, Fs, bits] = auread(aufile) returns the sample rate (Fs) in Hertz and the number of bits per sample (bits) used to encode the data in the file.

 $[\dots]$  = auread(aufile, N) returns only the first N samples from each channel in the file.

 $[\dots]$  = auread(aufile, [N1 N2]) returns only samples N1 through N2 from each channel in the file.

siz = auread(aufile, 'size') returns the size of the audio data contained in the file in place of the actual audio data, returning the vector siz = [samples channels].

#### See Also

auwri te	Write NeXT/SUN (. au) sound file
wavread	Read Microsoft WAVE (. wav) sound file

## auwrite

Purpose Write NeXT/SUN (. au) sound file

**Syntax** auwrite(y, aufile)

auwrite(y, Fs, aufile)
auwrite(y, Fs, N, aufile)

auwrite(y, Fs, N, method, aufile)

**Description** auwri te supports multi-channel data for 8-bit mu-law, and 8- and 16-bit linear

formats.

auwrite(y, aufile) writes a sound file specified by the string aufile. The data should be arranged with one channel per column. Amplitude values

outside the range [-1, +1] are clipped prior to writing.

auwrite(y, Fs, aufile) specifies the sample rate of the data in Hertz.

 $auwri\,te(y,Fs,N,\mathit{aufile})\ \ selects\ the\ number\ of\ bits\ in\ the\ encoder.\ Allowable$ 

settings are N = 8 and N = 16.

auwrite(y, Fs, N, method, aufile) allows selection of the encoding method, which can be either 'mu' or 'linear'. Note that mu-law files must be 8-bit. By

default, method=' mu'.

See Also auread Read NeXT/SUN (. au) sound file

wavwrite Write Microsoft WAVE (. wav) sound file

Improve accuracy of computed eigenvalues

**Syntax** 

Description

 $[D, B] = bal \, ance(A)$  returns a diagonal matrix D whose elements are integer powers of two, and a balanced matrix B so that  $B = D \setminus A*D$ . If A is symmetric, then B = A and D is the identity matrix.

B = bal ance(A) returns just the balanced matrix B.

Remarks

Nonsymmetric matrices can have poorly conditioned eigenvalues. Small perturbations in the matrix, such as roundoff errors, can lead to large perturbations in the eigenvalues. The quantity which relates the size of the matrix perturbation to the size of the eigenvalue perturbation is the condition number of the eigenvector matrix,

```
cond(V) = norm(V)*norm(i nv(V))
where
[V, D] = eig(A)
```

(The condition number of A itself is irrelevant to the eigenvalue problem.)

Balancing is an attempt to concentrate any ill conditioning of the eigenvector matrix into a diagonal scaling. Balancing usually cannot turn a nonsymmetric matrix into a symmetric matrix; it only attempts to make the norm of each row equal to the norm of the corresponding column. Furthermore, the diagonal scale factors are limited to powers of two so they do not introduce any roundoff error.

MATLAB's eigenvalue function,  $ei\ g(A)$ , automatically balances A before computing its eigenvalues. Turn off the balancing with  $ei\ g(A,\ '\ nobal\ ance'\ )$ .

### **Examples**

This example shows the basic idea. The matrix A has large elements in the upper right and small elements in the lower left. It is far from being symmetric.

Balancing produces a diagonal D matrix with elements that are powers of two and a balanced matrix B that is closer to symmetric than A.

To see the effect on eigenvectors, first compute the eigenvectors of A.

Note that all three vectors have the first component the largest. This indicates V is badly conditioned; in fact cond(V) is 1. 7484e+05. Next, look at the eigenvectors of B.

Now the eigenvectors are well behaved and cond(V) is 31. 9814. The ill conditioning is concentrated in the scaling matrix; cond(D) is 8192.

This example is small and not really badly scaled, so the computed eigenvalues of A and B agree within roundoff error; balancing has little effect on the computed results.

### **Algorithm**

bal ance is built into the MATLAB interpreter. It uses the algorithm in [1] originally published in Algol, but popularized by the Fortran routines BALANC and BALBAK from EISPACK.

Successive similarity transformations via diagonal matrices are applied to A to produce B. The transformations are accumulated in the transformation matrix D.

The eig function automatically uses balancing to prepare its input matrix.

#### Limitations

Balancing can destroy the properties of certain matrices; use it with some care. If a matrix contains small elements that are due to roundoff error, balancing may scale them up to make them as significant as the other elements of the original matrix.

#### **Diagnostics**

If A is not a square matrix:

Matrix must be square.

#### See Also

condei g Condition number with respect to eigenvalues ei g Eigenvalues and eigenvectors

hess Hessenberg form of a matrix

schur Schur decomposition

#### References

[1] Parlett, B. N. and C. Reinsch, "Balancing a Matrix for Calculation of Eigenvalues and Eigenvectors," *Handbook for Auto. Comp.*, Vol. II, Linear Algebra, 1971,pp. 315-326.

## base2dec

**Purpose** Base to decimal number conversion

**Syntax** d = base2dec('strn', base)

**Description** d = base2dec('strn', base) converts the string number strn of the specified

base into its decimal (base 10) equivalent. base must be an integer between 2 and 36. If 'strn' is a character array, each row is interpreted as a string in the

specified base.

**Examples** The expression base2dec('212', 3) converts 212<sub>3</sub> to decimal, returning 23.

See Also dec2base

Bessel functions of the third kind (Hankel functions)

Syntax

H = besselh(nu, K, Z)
H = besselh(nu, Z)
H = besselh(nu, 1, Z, 1)
H = besselh(nu, 2, Z, 1)
[H, i err] = besselh(...)

**Definitions** 

The differential equation

$$z^{2}\frac{d^{2}y}{dz^{2}} + z\frac{dy}{dz} - (z^{2} + v^{2})y = 0$$

where v is a nonnegative constant, is called *Bessel's equation*, and its solutions are known as *Bessel functions*.  $J_v(z)$  and  $J_{-v}(z)$  form a fundamental set of solutions of Bessel's equation for noninteger v.  $Y_v(z)$  is a second solution of Bessel's equation—linearly independent of  $J_v(z)$ —defined by:

$$Y_{\nu}(z) = \frac{J_{\nu}(z)\cos(\nu\pi) - J_{-\nu}(z)}{\sin(\nu\pi)}$$

The relationship between the Hankel and Bessel functions is:

$$H1_{v}(z) = J_{v}(z) + i Y_{v}(z)$$
  
 $H2_{v}(z) = J_{v}(z) - i Y_{v}(z)$ 

Description

 ${
m H}={
m bessel}\,{
m h}({
m nu},{
m K},{
m Z})\,\,$  for  ${
m K}=1$  or 2 computes the Hankel functions  $H1_{
m v}(z)$  or  $H2_{
m v}(z)$  for each element of the complex array Z. If  ${
m nu}$  and Z are arrays of the same size, the result is also that size. If either input is a scalar, it is expanded to the other input's size. If one input is a row vector and the other is a column vector, the result is a two-dimensional table of function values.

H = besselh(nu, Z) uses K = 1.

H = bessel h(nu, 1, Z, 1) scales  $H1_{v}(z)$  by  $\exp(-i*z)$ .

H = besselh(nu, 2, Z, 1) scales  $H2_{v}(z)$  by exp(+i\*z).

# besselh

[H, ierr] = besselh() also returns an array of error flags:		
ierr = 1	Illegal arguments.	
ierr = 2	Overflow. Return Inf.	
ierr = 3	Some loss of accuracy in argument reduction.	
ierr = 4	Unacceptable loss of accuracy, Z or nu too large.	
ierr = 5	No convergence. Return NaN.	

**Modified Bessel functions** 

**Syntax** 

I = besseli(nu, Z) Modified Bessel function of the 1st kind K = besselk(nu, Z) Modified Bessel function of the 3rd kind

E = besseli(nu, Z, 1)

K = bessel k(nu, Z, 1)

[I, ierr] = besseli(...)

[K, ierr] = besselk(...)

**Definitions** 

The differential equation

$$z^{2}\frac{\frac{d^{2}y}{dz^{2}}}+z\frac{dy}{dz}-(z^{2}+v^{2})y=0$$

where v is a nonnegative constant, is called the *modified Bessel's equation*, and its solutions are known as *modified Bessel functions*.

 $I_{
m v}(z)$  and  $I_{
m -v}(z)$  form a fundamental set of solutions of the modified Bessel's equation for noninteger v.  $K_{
m v}(z)$  is a second solution, independent of  $I_{
m v}(z)$ .

 $I_{\nu}(z)$  and  $K_{\nu}(z)$  are defined by:

$$I_{\nu}(z) = \left(\frac{z}{2}\right)^{\nu} \sum_{k=0}^{\infty} \frac{\left(\frac{z^{2}}{4}\right)^{k}}{k! \ \Gamma(\nu+k+1)}, \quad \text{where } \Gamma(a) = \int_{0}^{\infty} e^{-t} t^{a-1} dt$$

$$K_{\rm v}(z) = \left(\frac{\pi}{2}\right) \frac{I_{\rm -v}(z) - I_{\rm v}(z)}{\sin(v\pi)}$$

Description

 $I=bessel\ i\ (nu,Z)\ computes\ modified\ Bessel\ functions\ of\ the\ first\ kind,$   $I_{\nu}(z),\ for\ each\ element\ of\ the\ array\ Z.$  The order nu need not be an integer, but must be real. The argument Z can be complex. The result is real where Z is positive.

If nu and Z are arrays of the same size, the result is also that size. If either input is a scalar, it is expanded to the other input's size. If one input is a row vector and the other is a column vector, the result is a two-dimensional table of function values.

# besseli, besselk

K = bessel k(nu, Z) computes modified Bessel functions of the second kind,  $K_v(z)$ , for each element of the complex array Z.

E = besseli(nu, Z, 1) computes besseli(nu, Z) . \*exp(-Z).

K = bessel k(nu, Z, 1) computes bessel k(nu, Z) . \*exp(-Z).

[I, ierr] = besseli(...) and [K, ierr] = besselk(...) also return an array of error flags.

i err = 1 Illegal arguments.

i err = 2 Overflow. Return Inf.

i err = 3 Some loss of accuracy in argument reduction.

i err = 4 Unacceptable loss of accuracy, Z or nu too large.

i err = 5 No convergence. Return NaN.

### **Algorithm**

The bessel i and bessel k functions use a Fortran MEX-file to call a library developed by D. E. Amos [3] [4].

#### See Also

airy Airy functions besselj, bessely Bessel functions

#### References

- [1] Abramowitz, M. and I.A. Stegun, *Handbook of Mathematical Functions*, National Bureau of Standards, Applied Math. Series #55, Dover Publications, 1965, sections 9.1.1, 9.1.89 and 9.12, formulas 9.1.10 and 9.2.5.
- [2] Carrier, Krook, and Pearson, *Functions of a Complex Variable: Theory and Technique*, Hod Books, 1983, section 5.5.
- [3] Amos, D. E., "A Subroutine Package for Bessel Functions of a Complex Argument and Nonnegative Order," *Sandia National Laboratory Report*, SAND85-1018, May, 1985.
- [4] Amos, D. E., "A Portable Package for Bessel Functions of a Complex Argument and Nonnegative Order," *Trans. Math. Software*, 1986.

Bessel functions

Syntax

J = bessel j (nu, Z) Bessel function of the 1st kind Y = bessel y(nu, Z) Bessel function of the 2nd kind

[J,ierr] = besselj(nu, Z) [Y,ierr] = bessely(nu, Z)

**Definition** 

The differential equation

$$z^{2}\frac{d^{2}y}{dz^{2}} + z\frac{dy}{dz} - (z^{2} + v^{2})y = 0$$

where v is a nonnegative constant, is called *Bessel's equation*, and its solutions are known as *Bessel functions*.

 $J_{\rm v}(z)$  and  $J_{\rm -v}(z)$  form a fundamental set of solutions of Bessel's equation for noninteger v.

 $Y_{\rm v}(z)$  is a second solution of Bessel's equation—linearly independent of  $J_{\rm v}(z)$  — defined by:

$$Y_{\nu}(z) = \frac{J_{\nu}(z)\cos(\nu\pi) - J_{-\nu}(z)}{\sin(\nu\pi)}$$

Description

 $J=bessel j\ (nu,Z)\ computes$  Bessel functions of the first kind,  $J_v(z)$ , for each element of the complex array Z. The order nu need not be an integer, but must be real. The argument Z can be complex. The result is real where Z is positive.

If nu and Z are arrays of the same size, the result is also that size. If either input is a scalar, it is expanded to the other input's size. If one input is a row vector and the other is a column vector, the result is a two-dimensional table of function values.

Y = bessel y(nu, Z) computes Bessel functions of the second kind,  $Y_{\nu}(z)$ , for real, nonnegative order nu and argument Z.

# besselj, bessely

[J, ierr] = besselj(nu, Z) and [Y, ierr] = bessely(nu, Z) also return an array of error flags.

i err = 1 Illegal arguments.

i err = 2 Overflow. Return I nf.

i err = 3 Some loss of accuracy in argument reduction.

i err = 4 Unacceptable loss of accuracy, Z or nu too large.

i err = 5 No convergence. Return NaN.

#### Remarks

The Bessel functions are related to the Hankel functions, also called Bessel functions of the third kind:

$$H_{V}^{(1)}(z) = J_{V}(z) + i Y_{V}(z)$$

$$H_{V}^{(2)}(z) = J_{V}(z) - i Y_{V}(z)$$

where  $J_{\nu}(z)$  is bessel j , and  $Y_{\nu}(z)$  is bessel y. The Hankel functions also form a fundamental set of solutions to Bessel's equation (see bessel h).

## **Examples**

besselj (3:9, (0:.2:10)) generates the entire table on page 398 of Abramowitz and Stegun, *Handbook of Mathematical Functions*..

# **Algorithm**

The bessel j and bessel y functions use a Fortran MEX-file to call a library developed by D. E. Amos [3] [4].

## **See Also**

ai ry Airy functions bessel i , bessel k Modified Bessel functions

#### References

[1] Abramowitz, M. and I.A. Stegun, *Handbook of Mathematical Functions*, National Bureau of Standards, Applied Math. Series #55, Dover Publications, 1965, sections 9.1.1, 9.1.89 and 9.12, formulas 9.1.10 and 9.2.5.

[2] Carrier, Krook, and Pearson, *Functions of a Complex Variable: Theory and Technique*, Hod Books, 1983, section 5.5.

- [3] Amos, D. E., "A Subroutine Package for Bessel Functions of a Complex Argument and Nonnegative Order," *Sandia National Laboratory Report*, SAND85-1018, May, 1985.
- [4] Amos, D. E., "A Portable Package for Bessel Functions of a Complex Argument and Nonnegative Order," *Trans. Math. Software*, 1986.

# beta, betainc, betain

**Purpose** 

**Beta functions** 

**Syntax** 

B = beta(Z, W)

I = betainc(X, Z, W)

L = betaln(Z, W)

**Definition** 

The beta function is:

$$B(z, w) = \int_0^1 t^{z-1} (1-t)^{w-1} dt = \frac{\Gamma(z)\Gamma(w)}{\Gamma(z+w)}$$

where  $\Gamma(z)$  is the gamma function. The incomplete beta function is:

$$I_X(z, w) = \frac{1}{B(z, w)} \int_0^x t^{z-1} (1-t)^{w-1} dt$$

**Description** 

 $B = \mathrm{beta}(Z, W)$  computes the beta function for corresponding elements of the complex arrays Z and W. The arrays must be the same size (or either can be scalar).

I = betainc(X, Z, W) computes the incomplete beta function. The elements of X must be in the closed interval [0,1].

 $L = betal\, n(Z,W) \ computes \ the \ natural \ logarithm \ of \ the \ beta \ function, \\ log(beta(Z,W)), \ without \ computing \ beta(Z,W). \ Since \ the \ beta \ function \ can \\ range \ over \ very \ large \ or \ very \ small \ values, \ its \ logarithm \ is \ sometimes \ more \\ useful.$ 

# **Examples**

```
format rat
beta((0:10)',3)
ans =

1/0
1/3
1/12
1/30
1/60
1/105
1/168
1/252
1/360
1/495
1/660
```

In this case, with integer arguments,

```
beta(n, 3)
= (n-1)!*2!/(n+2)!
= 2/(n*(n+1)*(n+2))
```

is the ratio of fairly small integers and the rational format is able to recover the exact result.

For x = 510, betal n(x, x) = -708. 8616, which, on a computer with IEEE arithmetic, is slightly less than  $l \circ g(real \circ n)$ . Here beta(x, x) would underflow (or be denormal).

# **Algorithm**

```
beta(z, w) = exp(gammal n(z) + gammal n(w) - gammal n(z+w))
betal n(z, w) = gammal n(z) + gammal n(w) - gammal n(z+w)
```

**BiConjugate Gradients method** 

### **Syntax**

```
x = bicg(A, b)
bicg(A, b, tol)
bicg(A, b, tol, maxit)
bicg(A, b, tol, maxit, M)
bicg(A, b, tol, maxit, M1, M2)
bicg(A, b, tol, maxit, M1, M2, x0)
x = bicg(A, b, tol, maxit, M1, M2, x0)
[x, flag] = bicg(A, b, tol, maxit, M1, M2, x0)
[x, flag, relres] = bicg(A, b, tol, maxit, M1, M2, x0)
[x, flag, relres, iter] = bicg(A, b, tol, maxit, M1, M2, x0)
[x, flag, relres, iter, resvec] = bicg(A, b, tol, maxit, M1, M2, x0)
```

### Description

 $x=bi\,cg(A,b)$  attempts to solve the system of linear equations  $A^*x=b\,for\,x$ . The coefficient matrix A must be square and the right hand side (column) vector b must have length n, where A is n-by-n. bi cg will start iterating from an initial estimate that by default is an all zero vector of length n. Iterates are produced until the method either converges, fails, or has computed the maximum number of iterations. Convergence is achieved when an iterate x has relative residual  $norm(b-A^*x)/norm(b)$  less than or equal to the tolerance of the method. The default tolerance is 1e-6. The default maximum number of iterations is the minimum of n and 20. No preconditioning is used.

bi cg(A, b, tol) specifies the tolerance of the method, tol.

bi cg(A, b, tol, maxit) additionally specifies the maximum number of iterations, maxit.

bi cg(A, b, tol, maxit, M) and bi cg(A, b, tol, maxit, M1, M2) use left preconditioner M or M = M1\*M2 and effectively solve the system i nv(M)\*A\*x = i nv(M)\*b for x. If M1 or M2 is given as the empty matrix ([]), it is considered to be the identity matrix, equivalent to no preconditioning at all. Since systems of equations of the form M\*y = r are solved using backslash within bi cg, it is wise to factor preconditioners into their LU factors first. For example, replace bi cg(A, b, tol, maxit, M) with:

```
[M1, M2] = lu(M);
bicg(A, b, tol, maxit, M1, M2).
```

bi cg(A, b, tol, maxit, M1, M2, x0) specifies the initial estimate x0. If x0 is given as the empty matrix ([]), the default all zero vector is used.

x = bi cg(A, b, tol, maxit, M1, M2, x0) returns a solution x. If bi cg converged, a message to that effect is displayed. If bi cg failed to converge after the maximum number of iterations or halted for any reason, a warning message is printed displaying the relative residual norm(b-A\*x)/norm(b) and the iteration number at which the method stopped or failed.

[x, flag] = bi cg(A, b, tol, maxit, M1, M2, x0) returns a solution x and a flag that describes the convergence of bi cg:

Flag	Convergence		
0	bi cg converged to the desired tolerance tol within maxi t iterations without failing for any reason.		
1	bi cg iterated maxit times but did not converge.		
2	One of the systems of equations of the form $M^*y = r$ involving the preconditioner was ill-conditioned and did not return a useable result when solved by $\setminus$ (backslash).		
3	The method stagnated. (Two consecutive iterates were the same.)		
4	One of the scalar quantities calculated during bi $\operatorname{cg}$ became too small or too large to continue computing.		

Whenever  ${\tt fl}$  ag is not 0, the solution x returned is that with minimal norm residual computed over all the iterations. No messages are displayed if the  ${\tt fl}$  ag output is specified.

[x, flag, relres] = bi cg(A, b, tol, maxit, M1, M2, x0) also returns the relative residual norm(b-A\*x) /norm(b). If flag is 0, then relres  $\leq$  tol.

[x, flag, rel res, i ter] = bi cg(A, b, tol, maxi t, M1, M2, x0) also returns the iteration number at which x was computed. This always satisfies  $0 \le i$  ter  $\le$  maxi t.

[x, flag, rel res, i ter, resvec] = bi cg(A, b, tol, maxit, M1, M2, x0) also returns a vector of the residual norms at each iteration, starting from resvec(1) = norm(b-A\*x0). If flag is 0, resvec is of length i ter+1 and resvec(end)  $\leq$  tol\*norm(b).

### **Examples**

Start with A = west 0479 and make the true solution the vector of all ones.

```
load west0479
A = west0479
b = sum(A, 2)
```

We could accurately solve A\*x = b using backslash since A is not so large.

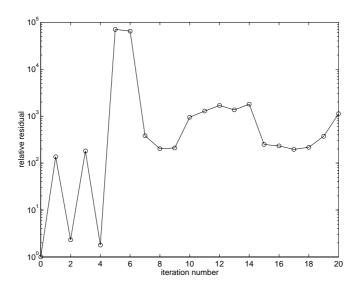
```
x = A \ b
norm(b-A*x) / norm(b) =
6.8476e-18
```

Now try to solve A\*x = b with bi cg.

```
[x, flag, relres, iter, resvec] = bicg(A, b)
flag =
1
relres =
1
iter =
0
```

The value of flag indicates that bicg iterated the default 20 times without converging. The value of iter shows that the method behaved so badly that the initial all zero guess was better than all the subsequent iterates. The value of rel res supports this: rel res = norm(b-A\*x)/norm(b) = norm(b)/norm(b) = 1.

The plot semilogy (0: 20, resvec/norm(b), '-o') below confirms that the unpreconditioned method oscillated rather wildly.



Try an incomplete LU factorization with a drop tolerance of  $1\mathrm{e}{-5}$  for the preconditioner.

```
[L1, U1] = luinc(A, 1e-5)

nnz(A) =

1887

nnz(L1) =

5562

nnz(U1) =

4320
```

A warning message indicates a zero on the main diagonal of the upper triangular U1. Thus it is singular. When we try to use it as a preconditioner:

```
[x, flag, rel res, iter, resvec] = bicg(A, b, 1e-6, 20, L1, U1)
flag =
2
rel res =
1
iter =
0
resvec =
7.0557e+005
```

the method fails in the very first iteration when it tries to solve a system of equations involving the singular U1 with backslash. It is forced to return the initial estimate since no other iterates were produced.

Try again with a slightly less sparse preconditioner:

```
[L2, U2] = luinc(A, 1e-6)

nnz(L2) =

6231

nnz(U2) =

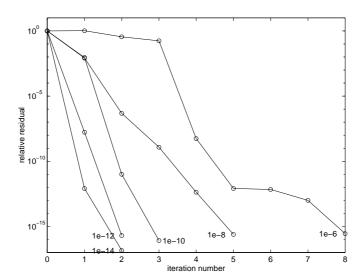
4559
```

This time there is no warning message. All entries on the main diagonal of U2 are nonzero

```
[x, flag, rel res, iter, resvec] = bicg(A, b, 1e-15, 10, L2, U2)
flag =
0
rel res =
2.8664e-16
iter =
8
```

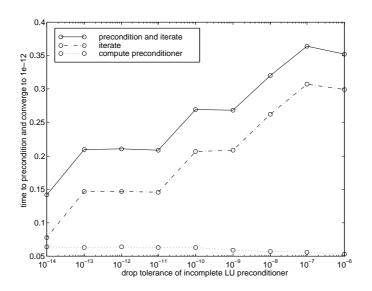
and bi cg converges to within the desired tolerance at iteration number 8. Decreasing the value of the drop tolerance increases the fill-in of the incomplete factors but also increases the accuracy of the approximation to the original matrix. Thus, the preconditioned system becomes closer to  $i \, nv(U) \, *i \, nv(L) \, *L*U*x = i \, nv(U) \, *i \, nv(L) \, *b$ , where L and U are the true LU factors, and closer to being solved within a single iteration.

The next graph shows the progress of bi cg using six different incomplete LU factors as preconditioners. Each line in the graph is labelled with the drop tolerance of the preconditioner used in bi cg.



This does not give us any idea of the time involved in creating the incomplete factors and then computing the solution. The following graph plots drop tolerance of the incomplete LU factors against the time to compute the preconditioner, the time to iterate once the preconditioner has been computed, and their sum, the total time to solve the problem. The time to produce the factors does not increase very quickly with the fill-in, but it does slow down the average time for an iteration. Since fewer iterations are performed, the total time to solve the

problem decreases. west0479 is quite a small matrix, only 139-by-139, and preconditioned bi cg still takes longer than backslash.



See Also	bi cgstab	BiConjugate Gradients Stabilized method
	cgs	Conjugate Gradients Squared method
	gmres	Generalized Minimum Residual method (with restarts)
	l ui nc	Incomplete LU matrix factorizations
	pcg	Preconditioned Conjugate Gradients method
	qmr	Quasi-Minimal Residual method
	\	Matrix left division

**References** Templates for the Solution of Linear Systems: Building Blocks for Iterative Methods, SIAM, Philadelphia, 1994.

**BiConjugate Gradients Stabilized method** 

### **Syntax**

```
x = bicgstab(A, b)
bicgstab(A, b, tol)
bicgstab(A, b, tol, maxit)
bicgstab(A, b, tol, maxit, M)
bicgstab(A, b, tol, maxit, M1, M2)
bicgstab(A, b, tol, maxit, M1, M2, x0)
x = bicgstab(A, b, tol, maxit, M1, M2, x0)
[x, flag] = bicgstab(A, b, tol, maxit, M1, M2, x0)
[x, flag, relres] = bicgstab(A, b, tol, maxit, M1, M2, x0)
[x, flag, relres, iter] = bicgstab(A, b, tol, maxit, M1, M2, x0)
[x, flag, relres, iter, resvec] = bicgstab(A, b, tol, maxit, M1, M2, x0)
```

### Description

 $x = bi \, cgstab(A,b)$  attempts to solve the system of linear equations  $A^*x = b$  for x. The coefficient matrix A must be square and the right hand side (column) vector b must have length n, where A is n-by-n.  $bi \, cgstab$  will start iterating from an initial estimate that by default is an all zero vector of length n. Iterates are produced until the method either converges, fails, or has computed the maximum number of iterations. Convergence is achieved when an iterate x has relative residual  $norm(b-A^*x) / norm(b)$  less than or equal to the tolerance of the method. The default tolerance is 1e-6. The default maximum number of iterations is the minimum of n and 20. No preconditioning is used.

bi cgstab(A, b, tol) specifies the tolerance of the method, tol.

 $bi \ cgstab(A, b, tol, maxit)$  additionally specifies the maximum number of iterations, maxit.

bi cgstab(A, b, tol, maxi t, M) and bi cgstab(A, b, tol, maxi t, M1, M2) use left preconditioner M or M = M1 \*M2 and effectively solve the system i nv(M) \*A\*x = i nv(M) \*b for x. If M1 or M2 is given as the empty matrix ([]), it is considered to be the identity matrix, equivalent to no preconditioning at all. Since systems of equations of the form M\*y = r are solved using backslash within bi cgstab,

it is wise to factor preconditioners into their LU factors first. For example, replace bi cgstab(A,b,tol,maxit,M) with:

```
[M1, M2] = lu(M);
bicgstab(A, b, tol, maxit, M1, M2).
```

bi cgstab(A, b, tol, maxit, M1, M2, x0) specifies the initial estimate x0. If x0 is given as the empty matrix ([]), the default all zero vector is used.

 $x = bi \, cgstab \, (A, \, b, \, tol \, , \, maxi \, t, \, M1, \, M2, \, x0)$  returns a solution x. If bi cgstab converged, a message to that effect is displayed. If bi cgstab failed to converge after the maximum number of iterations or halted for any reason, a warning message is printed displaying the relative residual norm(b-A\*x) / norm(b) and the iteration number at which the method stopped or failed.

[x, flag] = bi cgstab(A, b, tol, maxit, M1, M2, x0) returns a solution x and a flag that describes the convergence of bi cgstab:

Flag	Convergence		
0	bicgstab converged to the desired tolerance tol within maxit iterations without failing for any reason.		
1	bi cgstab iterated maxit times but did not converge.		
2	One of the systems of equations of the form $M^*y = r$ involving the preconditioner was ill-conditioned and did not return a useable result when solved by \ (backslash).		
3	The method stagnated. (Two consecutive iterates were the same.)		
4	One of the scalar quantities calculated during bi cgstab became too small or too large to continue computing.		

Whenever  ${\tt fl}$  ag is not 0, the solution x returned is that with minimal norm residual computed over all the iterations. No messages are displayed if the  ${\tt fl}$  ag output is specified.

[x, flag, relres] = bicgstab(A, b, tol, maxit, M1, M2, x0) also returns the relative residual norm(b-A\*x)/norm(b). If flag is 0, then relres  $\leq$  tol.

[x, flag, rel res, i ter] = bi cgstab(A, b, tol, maxi t, M1, M2, x0) also returns the iteration number at which x was computed. This always satisfies  $0 \le i$  ter  $\le \max i$  t. i ter may be an integer or an integer + 0.5, since bi cgstab may converge half way through an iteration.

[x, flag, rel res, i ter, resvec] = bi cgstab(A, b, tol, maxi t, M1, M2, x0) also returns a vector of the residual norms at each iteration, starting from resvec(1) = norm(b-A\*x0). If flag is 0, resvec is of length 2\*i ter+1, whether i ter is an integer or not. In this case, resvec(end)  $\leq$  tol \*norm(b).

## **Example**

```
load west0479
A = west0479
b = sum(A, 2)
[x, flag] = bicgstab(A, b)
```

flag is 1 since bi cgstab will not converge to the default tolerance 1e-6 within the default 20 iterations.

```
[L1, U1] = luinc(A, 1e-5)

[x1, flag1] = bicgstab(A, b, 1e-6, 20, L1, U1)
```

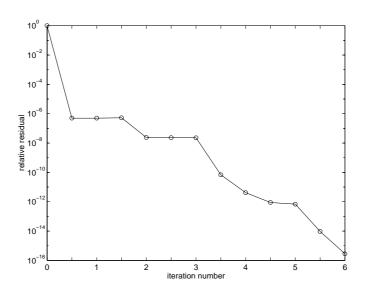
fl ag1 is 2 since the upper triangular U1 has a zero on its diagonal so bi cgst ab fails in the first iteration when it tries to solve a system such as U1\*y = r with backslash.

```
[L2, U2] = luinc(A, 1e-6)
[x2, flag2, relres2, iter2, resvec2] = bicgstab(A, b, 1e-15, 10, L2, U2)
```

flag2 is 0 since bi cgstab will converge to the tolerance of 2. 9e-16 (the value of rel res2) at the sixth iteration (the value of i ter2) when preconditioned by the incomplete LU factorization with a drop tolerance of 1e-6. resvec2(1) = norm(b) and resvec2(7) = norm(b-A\*x2). You may follow the progress of bi cgstab by plotting the relative residuals at the half way point and end of

# bicgstab

each iteration starting from the intial estimate (iterate number 0) with semilogy(0: 0.5: i ter2, resvec2/norm(b), '-o')



#### See Also

bi cg
cgs
Conjugate Gradients method
gmres
Generalized Minimum Residual method (with restarts)
l ui nc
pcg
Preconditioned Conjugate Gradients method
qmr
Quasi-Minimal Residual method
Matrix left division

#### References

van der Vorst, H. A., *BI-CGSTAB: A fast and smoothly converging variant of BI-CG for the solution of nonsymmetric linear systems*, SIAM J. Sci. Stat. Comput., March 1992, Vol. 13, No. 2, pp. 631-644.

Templates for the Solution of Linear Systems: Building Blocks for Iterative Methods, SIAM, Philadelphia, 1994.

**Purpose** Binary to decimal number conversion

Syntax bin2dec(binarystr)

**Description** bi n2dec(bi narystr) interprets the binary string bi narystr and returns the

equivalent decimal number.

**Examples** bi n2dec('010111') returns 23.

See Also  $\operatorname{dec}2\operatorname{bi} n$ 

# bitand

Purpose Bit-wise AND

**Syntax** C = bitand(A, B)

**Description** C = bitand(A, B) returns the bit-wise AND of two nonnegative integer argu-

ments A and B. To ensure the operands are integers, use the ceil, fix, floor,

and round functions.

**Examples** The five-bit binary representations of the integers 13 and 27 are 01101 and

11011, respectively. Performing a bit-wise AND on these numbers yields

01001, or 9.

C = bitand(13, 27)

C =

9

**See Also** bitcmp Complement bits

bi tget Get bit

bi tmax Maximum floating-point integer

bi tor Bit-wise OR bi tset Set bit

bitshift Bit-wise shift bitxor Bit-wise XOR

**Purpose** Complement bits

**Syntax** C = bitcmp(A, n)

**Description** C = bitcmp(A, n) returns the bit-wise complement of A as an n-bit

floating-point integer (flint).

**Example** With eight-bit arithmetic, the ones' complement of 01100011 (99, decimal) is

10011100 (156, decimal).

C = bitcmp(99, 8)

C =

156

**See Also** bit and Bit-wise AND

bitget Get bit

bitmax Maximum floating-point integer

bitor Bit-wise OR bitset Set bit

bitshift Bit-wise shift bitxor Bit-wise XOR

# bitget

Purpose Get bit

Syntax C = bitget(A, bit)

**Description** C = bitget(A, bit) returns the value of the bit at position bit in A. Operand

A must be a nonnegative integer, and  $bi\ t$  must be a number between 1 and the number of bits in the floating-point integer (flint) representation of A (52 for IEEE flints). To ensure the operand is an integer, use the ceil, fix, floor, and

round functions.

**Example** The dec2bi n function converts decimal numbers to binary. However, you can also use the bitget function to show the binary representation of a decimal

number. Just test successive bits from most to least significant:

See Also bit and Bit-wise AND bit cmp Complement bits

bi tmax Maximum floating-point integer

bi tor Bit-wise OR
bi tset Set bit
bi tshi ft Bit-wise shift
bi txor Bit-wise XOR

**Purpose** Maximum floating-point integer

**Syntax** bitmax

**Description** bitmax returns the maximum unsigned floating-point integer for your

computer. It is the value when all bits are set. On IEEE machines, this is the value  $2^{53}-1$ .

See Also Bit-wise AND bi tand

> Complement bits bitcmp

bitget Get bit bitor Bit-wise OR Set bit bitset Bit-wise shift

bi tshi ft bi txor Bit-wise XOR

# bitor

Purpose Bit-wise OR

Syntax C = bitor(A, B)

**Description** C = bitor(A, B) returns the bit-wise OR of two nonnegative integer argu-

ments A and B. To ensure the operands are integers, use the ceil, fix, floor,

and round functions.

**Examples** The five-bit binary representations of the integers 13 and 27 are 01101 and

11011, respectively. Performing a bit-wise OR on these numbers yields 11111,

or 31.

C = bitor(13, 27)

C =

31

See Also bit and Bit-wise AND

bitcmp Complement bits

bi tget Get bit

bi tmax Maximum floating-point integer

bi tset Set bit

bitshift Bit-wise shift bitxor Bit-wise XOR

Purpose Set bit

Syntax C = bitset(A, bit)C = bitset(A, bit, v)

**Description** C = bitset(A, bit) sets bit position bit in A to 1 (on). A must be a nonnegative

integer and  $bi\ t$  must be a number between 1 and the number of bits in the floating-point integer (flint) representation of A (52 for IEEE flints). To ensure the operand is an integer, use the ceil, fix, floor, and round functions.

C = bitset(A, bit, v) sets the bit at position bit to the value v, which must be either 0 or 1.

**Examples** Setting the fifth bit in the five-bit binary representation of the integer 9 (01001) yields 11001, or 25.

C = bitset(9, 5)

C =

25

See Also bit and Bit-wise AND

bitcmp Complement bits

bitget Get bit

bit max Maximum floating-point integer

bitor Bit-wise OR bitshift Bit-wise shift bitxor Bit-wise XOR

# bitshift

Purpose Bit-wise shift

Syntax C = bitshift(A, n)

**Description** C = bitshift(A, n) returns the value of A shifted by n bits. If n>0, this is same

as a multiplication by  $2^n$  (left shift). If n<0, this is the same as a division by  $2^n$  (right shift). A must be a nonnegative integer, which you can ensure by using

the ceil, fix, floor, and round functions.

**Examples** Shifting 1100 (12, decimal) to the left two bits yields 110000 (48, decimal).

C = bitshift(12, 2)

C =

48

See Also bit and Bit-wise AND

bitcmp Complement bits

bi tget Get bit

bi t max Maximum floating-point integer

bi tor Bit-wise OR bi tset Set bit

bi txor Bit-wise XOR

Purpose Bit-wise XOR

**Syntax** C = bitxor(A, B)

**Description** C = bitxor(A, B) returns the bit-wise XOR of the two arguments A and B. Both

A and B must be integers. You can ensure this by using the ceil, fix, floor,

and round functions.

**Examples** The five-bit binary representations of the integers 13 and 27 are 01101 and

 $11011, respectively. \ Performing \ a \ bit-wise \ XOR \ on \ these \ numbers \ yields \ 10110,$ 

or 22.

C = bitxor(13, 27)

C = 22

**See Also** bit and Bit-wise AND

bitcmp Complement bits

bitget Get bit

bit max Maximum floating-point integer

bitor Bit-wise OR bitset Set bit

bitshift Bit-wise shift

# blanks

**Purpose** A string of blanks

Syntax bl anks(n)

**Description** blanks(n) is a string of n blanks.

**Examples** blanks is useful with the display function. For example,

di sp(['xxx' bl anks(20) 'yyy'])

displays twenty blanks between the strings ' xxx' and ' yyy'.

 $di \, sp(bl \, anks(n)')$  moves the cursor down n lines.

See Also cl c Clear command window

home Send the cursor home

format See compact option for suppression of blank lines

**Purpose** Break out of flow control structures

Syntax break

**Description** break terminates the execution of for and while loops. In nested loops, break

exits from the innermost loop only.

**Examples** The indented statements are repeatedly executed until nonpositive n is entered.

```
while 1
    n = input('Enter n. n <= 0 quits. n = ')
    if n <= 0, break, end
    r = rank(magic(n))
end
disp('That''s all.')</pre>
```

**See Also** end Terminate for, while, and if statements and indicate

the last index

error Display error messages

for Repeat statements a specific number of times

if Conditionally execute statements return Return to the invoking function

switch Switch among several cases based on expression while Repeat statements an indefinite number of times

# builtin

**Purpose** Execute builtin function from overloaded method

**Syntax** builtin(function, x1, ..., xn)

[y1, ..., yn] = builtin(function, x1, ..., xn)

**Description** builtin is used in methods that overload builtin functions to execute the orig-

inal builtin function. If function is a string containing the name of a builtin

function, then:

builtin(function, x1,..., xn) evaluates that function at the given argu-

ments.

 $[y1, \ldots, yn] = builtin(function, x1, \ldots, xn)$  returns multiple output argu-

ments.

**Remarks** builtin(...) is the same as feval (...) except that it calls the original builtin

version of the function even if an overloaded one exists. (For this to work you

must never overload builtin.)

**See Also** feval Function evaluation

# builtin

# calendar

### **Purpose**

Calendar

# **Syntax**

c = cal endar

c = cal endar(d)

c = cal endar(y, m)

cal endar(...)

# **Description**

c = cal endar returns a 6-by-7 matrix containing a calendar for the current month. The calendar runs Sunday (first column) to Saturday.

 $c = cal \, endar(d)$ , where d is a serial date number or a date string, returns a calendar for the specified month.

 $c = cal \, endar(y, m)$ , where y and m are integers, returns a calendar for the specified month of the specified year.

cal endar(...) displays the calendar on the screen.

## **Examples**

The command:

cal endar (1957, 10)

reveals that the Space Age began on a Friday (on October 4, 1957, when Sputnik 1 was launched).

0ct 1957						
S	M	Tu	W	Th	F	S
0	0	1	2	3	<u>4</u>	5
6	7	8	9	10	11	12
13	14	15	16	17	18	19
20	21	22	23	24	25	26
27	28	29	30	31	0	0
0	0	0	0	0	0	0

See Also

datenum

Serial date number

Transform Cartesian coordinates to polar or cylindrical

**Syntax** 

$$[THETA, RH0, Z] = cart2pol(X, Y, Z)$$
  
 $[THETA, RH0] = cart2pol(X, Y)$ 

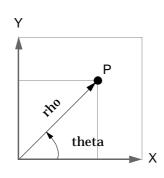
Description

[THETA, RHO, Z] = cart2pol (X, Y, Z) transforms three-dimensional Cartesian coordinates stored in corresponding elements of arrays X, Y, and Z, into cylindrical coordinates. THETA is a counterclockwise angular displacement in radians from the positive x-axis, RHO is the distance from the origin to a point in the x-y plane, and Z is the height above the x-y plane. Arrays X, Y, and Z must be the same size (or any can be scalar).

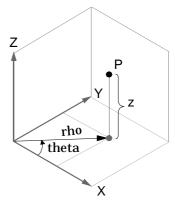
[THETA, RHO] = cart2pol(X, Y) transforms two-dimensional Cartesian coordinates stored in corresponding elements of arrays X and Y into polar coordinates.

Algorithm

The mapping from two-dimensional Cartesian coordinates to polar coordinates, and from three-dimensional Cartesian coordinates to cylindrical coordinates is:



Two-Dimensional Mapping theta = atan2(y, x)rho =  $sqrt(x.^2 + y.^2)$ 



Three-Dimensional Mapping theta = atan2(y, x) rho = sqrt(x.^2 + y.^2) z = z

# cart2pol

See Also	cart2sph	Transform Cartesian coordinates to spherical
	pol 2cart	Transform polar or cylindrical coordinates to Cartesian
	sph2cart	Transform spherical coordinates to Cartesian

Transform Cartesian coordinates to spherical

**Syntax** 

[THETA, PHI, R] = cart2sph(X, Y, Z)

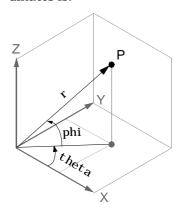
Description

[THETA, PHI, R] = cart2sph(X, Y, Z) transforms Cartesian coordinates stored in corresponding elements of arrays X, Y, and Z into spherical coordinates. Azimuth THETA and elevation PHI are angular displacements in radians measured from the positive x-axis, and the x-y plane, respectively; and R is the distance from the origin to a point.

Arrays X, Y, and Z must be the same size.

**Algorithm** 

The mapping from three-dimensional Cartesian coordinates to spherical coordinates is:



theta = atan2(y, x)phi =  $atan2(z, sqrt(x.^2 + y.^2))$ r =  $sqrt(x.^2+y.^2+z.^2)$ 

See Also

cart2pol pol2cart sph2cart Transform Cartesian coordinates to polar or cylindrical Transform polar or cylindrical coordinates to Cartesian Transform spherical coordinates to Cartesian

Case switch

### Description

case is part of the switch statement syntax, which allows for conditional execution.

A particular case consists of the case statement itself, followed by a case expression, and one or more statements.

A case is executed only if its associated case expression (case\_expr) is the first to match the switch expression (switch\_expr).

# **Examples**

The general form of the switch statement is:

```
switch switch_expr
    case case_expr
    statement,..., statement
    case {case_expr1, case_expr2, case_expr3,...}
    statement,..., statement
...
    otherwise
        statement,..., statement
end
```

See switch for more details.

#### See Also

switch

Switch among several cases based on expression

Concatenate arrays

**Syntax** 

$$C = cat(dim, A, B)$$

$$C = cat(dim, A1, A2, A3, A4...)$$

Description

C = cat(dim, A, B) concatenates the arrays A and B along dim.

C = cat(dim, A1, A2, A3, A4, ...) concatenates all the input arrays (A1, A2, A3, A4, and so on) along dim.

cat(2, A, B) is the same as [A, B] and cat(1, A, B) is the same as [A; B].

Remarks

When used with comma separated list syntax,  $cat(dim, C\{:\})$  or cat(dim, C. field) is a convenient way to concatenate a cell or structure array containing numeric matrices into a single matrix.

**Examples** 

Given,

$$A = B = 1 2 5 6 3 4 7 8$$

concatenating along different dimensions produces:



$$C = cat(1, A, B)$$

$$C = cat(2, A, B)$$

$$C = cat(3, A, B)$$

The commands

$$A = magic(3); B = pascal(3);$$
  
 $C = cat(4, A, B);$ 

produce a 3-by-3-by-1-by-2 array.

See Also

[] (Special characters) Build arrays num2cell Convert a numeric array into a cell array

**Purpose** Change working directory

Syntax cd

cd directory

cd ...

**Description** cd, by itself, prints out the current directory.

cd di rectory sets the current directory to the one specified. On UNIX plat-

forms, the character ~ is interpreted as the user's root directory.

cd .. changes to the directory above the current one.

**Examples** UNIX: cd /usr/local/matlab/toolbox/demos

DOS: cd C: MATLAB\DEMOS

VMS: cd DISK1: [MATLAB. DEMOS]

Macintosh: cd Toolbox: Demos

To specify a Macintosh directory name that includes spaces, enclose the name

in single quotation marks, as in 'Toolbox: New M-Files'.

See Also dir Directory listing

path Control MATLAB's directory search path

what Directory listing of M-files, MAT-files, and MEX-files

Convert complex diagonal form to real block diagonal form

**Syntax** 

$$[V, D] = cdf2rdf(V, D)$$

**Description** 

If the eigensystem [V, D] = eig(X) has complex eigenvalues appearing in complex-conjugate pairs, cdf2rdf transforms the system so D is in real diagonal form, with 2-by-2 real blocks along the diagonal replacing the complex pairs originally there. The eigenvectors are transformed so that

$$X = V*D/V$$

continues to hold. The individual columns of V are no longer eigenvectors, but each pair of vectors associated with a 2-by-2 block in D spans the corresponding invariant vectors.

**Examples** 

The matrix

has a pair of complex eigenvalues.

$$[V, D] = eig(X)$$

## cdf2rdf

Converting this to real block diagonal form produces

[V, D] = cdf2rdf(V, D)

**Algorithm** 

The real diagonal form for the eigenvalues is obtained from the complex form using a specially constructed similarity transformation.

See Also

ei g Eigenvalues and eigenvectors rsf2csf Convert real Schur form to complex Schur form Purpose Round toward infinity

Syntax B = ceil(A)

**Description** B = ceil(A) rounds the elements of A to the nearest integers greater than or

equal to A. For complex A, the imaginary and real parts are rounded indepen-

dently.

**Examples** a =

Columns 1 through 4

-1. 9000 -0. 2000 3. 4000 5. 6000

Columns 5 through 6

7. 0000 2. 4000 + 3. 6000i

ceil(a)

ans =

Columns 1 through 4

Columns 5 through 6

7. 0000 3. 0000 + 4. 0000i

**See Also** fix Round toward zero

floor Round toward minus infinity round Round to nearest integer

### Create cell array

### **Syntax**

```
c = cell(n)
c = cell(m, n)
c = cell([m n])
c = cell([m, n, p, ...)
c = cell([m n p ...])
c = cell(size(A))
```

### Description

c = cell(n) creates an n-by-n cell array of empty matrices. An error message appears if n is not a scalar.

c = cell(m, n) or c = cell([m, n]) creates an m-by-n cell array of empty matrices. Arguments m and n must be scalars.

c = cell(m, n, p, ...) or c = cell([m n p ...]) creates an m-by-n-by-p-... cell array of empty matrices. Arguments m, n, p,... must be scalars.

 $c = \text{cel}\,l\,(\text{si}\,ze(A))$  creates a cell array the same size as A containing all empty matrices.

## **Examples**

[]

[]

A = ones(2, 2)

## See Also

ones	Create an array of all ones
rand	Uniformly distributed random numbers and arrays
randn	Normally distributed random numbers and arrays
zeros	Create an array of all zeros

**Purpose** Cell array to structure array conversion

**Syntax** s = cell2struct(c, fields, dim)

**Description** 

 $s = cell \, 2 \, struct \, (c, \, fiel \, ds, \, dim)$  converts the cell array c into the structure s by folding the dimension  $dim \, of \, c$  into fields of s. The length of c along the specified dimension  $(size(c, \, dim))$  must match the number of fields names in  $fiel \, ds$ . Argument  $fiel \, ds$  can be a character array or a cell array of strings.

**Examples** 

```
c = {'tree', 37. 4, 'birch'};
f = {'category', 'height', 'name'};
s = cell2struct(c, f, 2)
s =
    category: 'tree'
    height: 37. 4000
    name: 'birch'
```

See Also

field names of a structure

struct2cell Structure to cell array conversion

# celldisp

**Purpose** 

Display cell array contents.

**Syntax** 

celldisp(C)

Description

celldisp(c) recursively displays the contents of a cell array.

**Example** 

Use  $\operatorname{cel} l \operatorname{di} \operatorname{sp}$  to display the contents of a 2-by-3 cell array:

 $\label{eq:continuous} \begin{array}{lll} C \ = \ \{ \ [1\ 2] \ 'Tony' \ 3+4i \ ; \ [1\ 2; 3\ 4] \ -5 \ 'abc' \ \}; \\ cell di \ sp(C) \end{array}$ 

 $C\{1, 1\} =$ 

1 2

 $C\{2, 1\} =$ 

1 2 3 4

 $C\{1, 2\} =$ 

Tony

 $C\{2, 2\} =$ 

-5

 $C\{1, 3\} =$ 

3. 0000+ 4. 0000i

 $C\{2, 3\} =$ 

abc

See Also

cellplot

Graphically display the structure of cell arrays  $% \left\{ \left( 1\right) \right\} =\left\{ \left($ 

#### **Purpose** Graphically display the structure of cell arrays

#### Syntax

```
cellplot(c)
cellplot(c, 'legend')
handles = cellplot(...)
```

### **Description**

cellplot(c) displays a figure window that graphically represents the contents of c. Filled rectangles represent elements of vectors and arrays, while scalars and short text strings are displayed as text.

cellplot(c, 'legend') also puts a legend next to the plot.

handles = cellplot(c) displays a figure window and returns a vector of surface handles.

#### Limitations

The cellplot function can display only two-dimensional cell arrays.

#### **Examples**

Consider a 2-by-2 cell array containing a matrix, a vector, and two text strings:

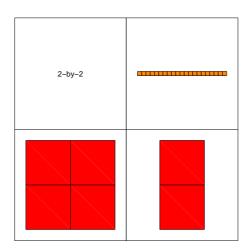
```
c{1, 1} = '2-by-2';

c{1, 2} = 'eigenvalues of eye(2)';

c{2, 1} = eye(2);

c{2, 2} = eig(eye(2));
```

The command cellplot(c) produces:



## cellstr

**Purpose** Create cell array of strings from character array

**Syntax** c = cellstr(S)

**Description** c = cellstr(S) places each row of the character array S into separate cells of

c. Use the string function to convert back to a string matrix.

**Examples** Given the string matrix

S = abc defg hi

The command c = cellstr(S) returns the 3-by-1 cell array:

c =
 'abc'
 'defg'
 'hi'

See Also i scellstr True for cell array of strings

strings MATLAB string handling

Conjugate Gradients Squared method

#### **Syntax**

```
x = cgs(A, b)
cgs(A, b, tol)
cgs(A, b, tol, maxit)
cgs(A, b, tol, maxit, M)
cgs(A, b, tol, maxit, M1, M2)
cgs(A, b, tol, maxit, M1, M2, x0)
x = cgs(A, b, tol, maxit, M1, M2, x0)
[x, flag] = cgs(A, b, tol, maxit, M1, M2, x0)
[x, flag, relres] = cgs(A, b, tol, maxit, M1, M2, x0)
[x, flag, relres, iter] = cgs(A, b, tol, maxit, M1, M2, x0)
[x, flag, relres, iter, resvec] = cgs(A, b, tol, maxit, M1, M2, x0)
```

#### Description

x = cgs(A, b) attempts to solve the system of linear equations A\*x = b for x. The coefficient matrix A must be square and the right hand side (column) vector b must have length n, where A is n-by-n. cgs will start iterating from an initial estimate that by default is an all zero vector of length n. Iterates are produced until the method either converges, fails, or has computed the maximum number of iterations. Convergence is achieved when an iterate x has relative residual norm(b-A\*x) / norm(b) less than or equal to the tolerance of the method. The default tolerance is 1e-6. The default maximum number of iterations is the minimum of n and n0. No preconditioning is used.

cgs(A, b, tol) specifies the tolerance of the method, tol.

 $cgs(A,\,b,\,tol\,,\,maxi\,t)~$  additionally specifies the maximum number of iterations, maxi t.

cgs(A, b, tol, maxit, M) and cgs(A, b, tol, maxit, M1, M2) use left preconditioner Mor M = M1\*M2 and effectively solve the system i nv(M) \*A\*x = i nv(M) \*b for x. If M1 or M2 is given as the empty matrix ([]), it is considered to be the identity matrix, equivalent to no preconditioning at all. Since systems of equations of the form M\*y = r are solved using backslash within cgs, it is wise to factor preconditioners into their LU factors first. For example, replace cgs(A, b, tol, maxit, M) with:

```
[M1, M2] = lu(M);

cgs(A, b, tol, maxit, M1, M2).
```

cgs(A, b, tol, maxit, M1, M2, x0) specifies the initial estimate x0. If x0 is given as the empty matrix ([]), the default all zero vector is used.

x = cgs(A, b, tol, maxit, M1, M2, x0) returns a solution x. If cgs converged, a message to that effect is displayed. If cgs failed to converge after the maximum number of iterations or halted for any reason, a warning message is printed displaying the relative residual norm(b-A\*x) / norm(b) and the iteration number at which the method stopped or failed.

[x, flag] = cgs(A, b, tol, maxit, M1, M2, x0) returns a solution x and a flag that describes the convergence of cgs:

Flag	Convergence
0	cgs converged to the desired tolerance tol within maxit iterations without failing for any reason.
1	cgs iterated maxit times but did not converge.
2	One of the systems of equations of the form $M*y = r$ involving the preconditioner was ill-conditioned and did not return a useable result when solved by $\setminus$ (backslash).
3	The method stagnated. (Two consecutive iterates were the same.)
4	One of the scalar quantities calculated during cgs became too small or too large to continue computing.

Whenever  ${\tt fl}$  ag is not 0, the solution x returned is that with minimal norm residual computed over all the iterations. No messages are displayed if the  ${\tt fl}$  ag output is specified.

[x, flag, rel res] = cgs(A, b, tol, maxi t, M1, M2, x0) also returns the relative residual norm(b-A\*x) /norm(b). If flag is 0, then rel res  $\leq$  tol.

[x, flag, rel res, i ter] = cgs(A, b, tol, maxit, M1, M2, x0) also returns the iteration number at which x was computed. This always satisfies  $0 \le i \text{ ter} \le \text{maxit}$ .

[x, flag, rel res, i ter, resvec] = cgs(A, b, tol, maxi t, M1, M2, x0) also returns a vector of the residual norms at each iteration, starting from resvec(1) = norm(b-A\*x0). If flag is 0, resvec is of length i ter+1 and resvec(end)  $\leq$  tol\*norm(b).

#### **Examples**

```
load west0479
A = west0479
b = sum(A, 2)
[x, flag] = cgs(A, b)
```

fl ag is 1 since cgs will not converge to the default tolerance  $1\mathrm{e}{-6}$  within the default 20 iterations.

```
[L1, U1] = luinc(A, 1e-5)

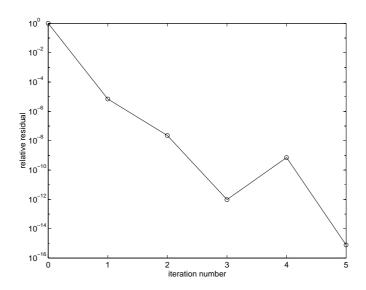
[x1, flag1] = cgs(A, b, 1e-6, 20, L1, U1)
```

fl ag1 is 2 since the upper triangular U1 has a zero on its diagonal so cgs fails in the first iteration when it tries to solve a system such as U1\*y = r for y with backslash.

```
[L2, U2] = luinc(A, 1e-6)
[x2, flag2, relres2, iter2, resvec2] = cgs(A, b, 1e-15, 10, L2, U2)
```

fl ag2 is 0 since cgs will converge to the tolerance of 7. 9e-16 (the value of rel res2) at the fifth iteration (the value of i ter2) when preconditioned by the incomplete LU factorization with a drop tolerance of 1e-6. resvec2(1) = norm(b) and resvec2(6) = norm(b-A\*x2). You may follow the progress of cgs

by plotting the relative residuals at each iteration starting from the initial estimate (iterate number 0) with semil ogy(0: i ter2, res2/norm(b), '-o').



#### See Also

bi cg	BiConjugate Gradients method
bi cgstab	BiConjugate Gradients Stabilized method
gmres	Generalized Minimum Residual method (with restarts)
l ui nc	Incomplete LU matrix factorizations
pcg	Preconditioned Conjugate Gradients method
qmr	Quasi-Minimal Residual method
\	Matrix left division

#### References

Sonneveld, Peter, *CGS: A fast Lanczos-type solver for nonsymmetric linear systems*, SIAM J. Sci. Stat. Comput., January 1989, Vol. 10, No. 1, pp. 36-52

Templates for the Solution of Linear Systems: Building Blocks for Iterative Methods, SIAM, Philadelphia, 1994.

Create character array (string)

#### Syntax

```
S = char(X)
S = char(C)
S = char(t1, t2. t3...)
```

#### Description

S = char(X) converts the array X that contains positive integers representing character codes into a MATLAB character array (the first 127 codes are ASCII). The actual characters displayed depend on the character set encoding for a given font. The result for any elements of X outside the range from 0 to 65535 is not defined (and may vary from platform to platform). Use doubl e to convert a character array into its numeric codes.

S = char(C) when C is a cell array of strings, places each element of C into the rows of the character array s. Use cellstr to convert back.

 $S = \operatorname{char}(t1, t2, t3, \ldots)$  forms the character array S containing the text strings  $T1, T2, T3, \ldots$  as rows, automatically padding each string with blanks to form a valid matrix. Each text parameter, Ti, can itself be a character array. This allows the creation of arbitarily large character arrays. Empty strings are significant.

#### Remarks

Ordinarily, the elements of A are integers in the range 32:127, which are the printable ASCII characters, or in the range 0:255, which are all 8-bit values. For noninteger values, or values outside the range 0:255, the characters printed are determined by fix(rem(A, 256)).

#### **Examples**

To print a 3-by-32 display of the printable ASCII characters:

```
ascii = char(reshape(32:127,32,3)') ascii = ! " # $ % & ' ( ) *+ , - . / 0 1 2 3 4 5 6 7 8 9 : ; < = > ? @ A B C D E F G H I J K L M N 0 P Q R S T U V W X Y Z [ \ ] ^ _ ' a b c d e f g h i j k l m n o p q r s t u v w x y z { | } ~
```

## char

## See Also

get, set, and text in the online  $\mathit{MATLAB}$  Function Reference , and:

cellstr Create cell array of strings from character array

doubl eConvert to double precisionstri ngsMATLAB string handling

strvcat Vertical concatenation of strings

Cholesky factorization

**Syntax** 

$$R = \text{chol}(X)$$
  
 $[R, p] = \text{chol}(X)$ 

Description

The chol function uses only the diagonal and upper triangle of X. The lower triangular is assumed to be the (complex conjugate) transpose of the upper. That is, X is Hermitian.

R = chol(X), where X is positive definite produces an upper triangular R so that R' \* R = X. If X is not positive definite, an error message is printed.

[R,p]= chol(X), with two output arguments, never produces an error message. If X is positive definite, then p is 0 and R is the same as above. If X is not positive definite, then p is a positive integer and R is an upper triangular matrix of order q=p-1 so that R'\*R=X(1:q,1:q).

### **Examples**

The binomial coefficients arranged in a symmetric array create an interesting positive definite matrix.

```
n = 5:
X = pascal(n)
X =
    1
          1
               1
                     1
                           1
    1
          2
               3
                     4
                           5
          3
    1
               6
                    10
                          15
    1
          4
              10
                    20
                          35
    1
          5
              15
                    35
                          70
```

It is interesting because its Cholesky factor consists of the same coefficients, arranged in an upper triangular matrix.

## chol

Destroy the positive definiteness (and actually make the matrix singular) by subtracting 1 from the last element.

Now an attempt to find the Cholesky factorization fails.

## **Algorithm**

chol uses the algorithm from the LINPACK subroutine ZP0FA. For a detailed description of the use of the Cholesky decomposition, see Chapter 8 of the *LINPACK Users' Guide*.

#### References

[1] Dongarra, J.J., J.R. Bunch, C.B. Moler, and G.W. Stewart, *LINPACK Users' Guide*, SIAM, Philadelphia, 1979.

**Incomplete Cholesky factorizations** 

#### **Syntax**

cholinc(X, '0')
R = cholinc(X, '0')
[R, p] = cholinc(X, '0')
R = cholinc(X, droptol)
R = cholinc(X, options)

### Description

chol i nc(X, '0') produces the incomplete Cholesky factorization of a real symmetric positive definite sparse matrix with 0 level of fill-in. chol i nc(X, '0') produces an upper triangular matrix. The lower triangle of X is assumed to be the transpose of the upper (X is symmetric).

 $R = \operatorname{chol} i \operatorname{nc}(X, '0')$  returns an upper triangular matrix which has the same sparsity pattern as the upper triangle of X. The product R' \*R agrees with X over its sparsity pattern. The positive definiteness of X is not sufficient to guarantee the existence of the incomplete factor, and, in this case, an error message is printed.

[R,p]= cholinc(X, '0') never produces an error message. If the incomplete factor exists, then p=0 and R is the upper triangular factor. If the calculation of R breaks down due to a zero or negative pivot, then p is a positive integer and R is an upper triangular matrix of size q-by-n where q=p-1. The sparsity pattern of R is the same as the q-by-n upper triangle of R and the R-by-R agrees with R over the sparsity pattern of its first R rows and columns R (1: R) and R (1: R).

 $R = \operatorname{chol} \operatorname{inc}(X,\operatorname{droptol})$  computes the incomplete Cholesky factorization of any sparse matrix using a drop tolerance. droptol must be a non-negative scalar.  $\operatorname{chol} \operatorname{inc}(X,\operatorname{droptol})$  produces an approximation to the complete Cholesky factor returned by  $\operatorname{chol}(X)$ . For increasingly smaller values of the drop tolerance, this approximation improves, until the drop tolerance is 0, at which time the complete Cholesky factorization is produced, as in  $\operatorname{chol}(X)$ .

The off-diagonal entries R(i,j) which are smaller in magnitude than the local drop tolerance, which is given by dropt ol \*norm(X(:,j))/R(i,i), are dropped from the factor. The diagonal entries are preserved even if they are too small in an attempt to avoid a singular factor.

 $R = \operatorname{chol} \operatorname{inc}(X, \operatorname{options})$  specifies a structure with up to three fields which may be used in any combination: droptol, mi chol, rdi ag. Additional fields are ignored.

dropt of is the drop tolerance of the incomplete factorization.

If mi chol is 1, chol i nc produces the modified incomplete Cholesky factorization which subtracts the dropped elements in any column from the diagonal element of the upper triangular factor. The default value is 0.

If rdi ag is 1, any zeros on the diagonal of the upper triangular factor are replaced by the square root of the product of the drop tolerance and the norm of that column of X,  $\operatorname{sqrt}(\operatorname{droptol}*\operatorname{norm}(X(:,j)))$ . The default is 0. Note that the thresh option available in the incomplete LU factorization (see l ui nc) is not here as it is always set to 0. There are never any row interchanges during the formation of the incomplete Cholesky factor.

R = cholinc(X, droptol) and R = cholinc(X, options) return an upper triangular matrix in R. The product R' \*R is an approximation to the matrix X.

#### Remarks

These incomplete factorizations may be useful as preconditioners for solving large sparse systems of linear equations. A single 0 on the diagonal of the upper triangular factor makes it singular. The incomplete factorization with a drop tolerance prints a warning message if the upper triangular factor has zeros on the diagonal. Similarly, using the rdi ag option to replace a zero diagonal only gets rid of the symptoms of the problem, but it does not solve it. The preconditioner may not be singular, but it probably is not useful, and a warning message is printed.

#### **Examples**

Start with a symmetric positive definite matrix, S.

```
S = del sq(numgrid('C', 15));
```

S is the two-dimensional, five-point discrete negative Lapacian on the grid generated by numgri  $d(\ C'\ ,\ 15)$  .

Compute the Cholesky factorization and the incomplete Cholesky factorization of level 0 to compare the fill-in. Make S singular by zeroing out a diagonal entry and compute the (partial) incomplete Cholesky factorization of level 0.

```
C = chol(S);

R0 = chol(S, '0');

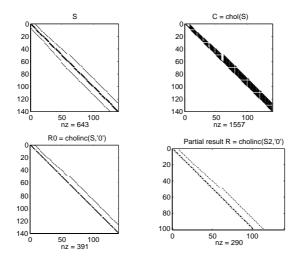
S2 = S; S2(101, 101) = 0;

[R, p] = cholinc(S2, '0');
```

There is fill-in within the bands of S in the complete Cholesky factor, but none in the incomplete Cholesky factor. The incomplete factorization of the singular S2 stopped at row p=101 resulting in a 100-by-139 partial factor.

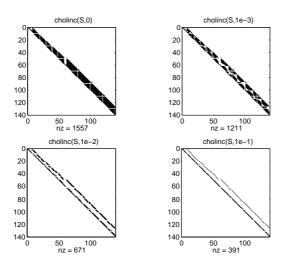
```
D1 = (R0' *R0). *spones(S)-S;
D2 = (R' *R). *spones(S2)-S2;
```

D1 has elements of the order of eps, showing that R0 $^{\circ}$  \*R0 agrees with S over its sparsity pattern. D2 has elements of the order of eps over its first 100 rows and first 100 columns, D2(1: 100, :) and D2(:, 1: 100).

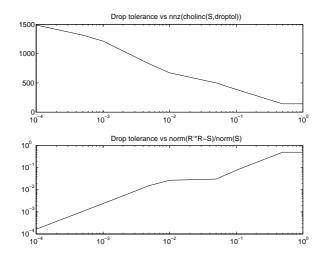


The first subplot below shows that cholinc(S,0), the incomplete Cholesky factor with a drop tolerance of 0, is the same as the Cholesky factor of S.

Increasing the drop tolerance increases the sparsity of the incomplete factors, as seen below.



Unfortunately, the sparser factors are poor approximations, as is seen by the plot of drop tolerance versus norm(R' \*R-S, 1) / norm(S, 1) in the next figure.



Limitations

chol i nc works on square matrices only. For chol i nc(X, '0'), X must be real.

Algorithm

R = cholinc(X, droptol) is obtained from  $[L, U] = l \, \text{uinc}(X, \text{options})$ , where options. droptol = droptol and options. thresh = 0. The rows of the upper-triangular U are scaled by the square root of the diagonal in that row, and this scaled factor becomes R.

R = cholinc(X, options) is produced in a similar manner, except the rdi ag option translates into the udi ag option and the milu option takes the value of the michol option.

chol i nc(X, '0') is based on the "KJI" variant of the Cholesky factorization. Updates are made only to positions which are nonzero in the upper triangle of X.

See Also

chol Cholesky factorization

luinc Incomplete LU matrix factorizations

pcg Preconditioned Conjugate Gradients method

References

Saad, Yousef, Iterative Methods for Sparse Linear Systems, PWS Publishing

Company, 1996, Chapter 10 - Preconditioning Techniques.

Create object or return class of object

Syntax

```
str = class(object)
```

obj = class(s, 'class\_name')

obj = class(s, 'class\_name', parent1, parent2...)

Description

str = class(object) returns a string specifying the class of object.

The possible object classes are:

cel l Multidimensional cell array

doubl e Multidimensional double precision array

sparse Two-dimensional real (or complex) sparse array

char Array of alphanumeric characters

struct Structure

' class\_name' User-defined object class

obj = class(s, 'class\_name') creates an object of class 'class\_name' using structure s as a template. This syntax is only valid in a function named class\_name. m in a directory named @class\_name (where 'class\_name' is the same as the string passed into class).

**NOTE** On VMS, the method directory is named #cl ass\_name.

obj = class(s, 'class\_name', parent1, parent2,...) creates an object of class 'class\_name' using structure s as a template, and also ensures that the newly created object inherits the methods and fields of the parent objects parent1, parent2, and so on.

See Also

inferior to Inferior class relationship
isa Detect an object of a given class
superior to Superior class relationship

**Purpose** Remove items from memory

Syntax

cl ear

clear name

clear name1 name2 name3...

clear global name

clear keyword where keyword is one of:

mex global all

functions variables

Description

clear, by itself, clears all variables from the workspace.

clear name removes just the M-file or MEX-file function or variable name from the workspace. If name is global, it is removed from the current workspace, but left accessible to any functions declaring it global.

clear name1 name2 name3 removes name1, name2, and name3 from the workspace.

clear global name removes the global variable name.

clear keyword clears the indicated items:

clear functions Clears all the currently compiled M-functions from

memory.

 ${\it clear \ variables} \quad {\it Clears \ all \ variables} \ from \ the \ workspace.$ 

clear mex Clears all MEX-files from memory.

clear global Clears all global variables.

clear all Removes all variables, functions, and MEX-files from

memory, leaving the workspace empty.

Remarks

You can use wildcards (\*) to remove items selectively. For instance, clear my\* removes any variables whose names begin with the string "my." The function form of the syntax, clear ('name'), is also permitted.

## clear

**Limitations** clear doesn't affect the amount of memory allocated to the MATLAB process

under UNIX.

See Also pack Consolidate workspace memory

**Purpose** Current time as a date vector

Syntax c = clock

**Description** c = clock returns a 6-element date vector containing the current date and

time in decimal form:

c = [year month day hour minute seconds]

The first five elements are integers. The seconds element is accurate to several digits beyond the decimal point. The statement fix(clock) rounds to integer

display format.

See Also cputime CPU time in seconds

datenum Serial date number datevec Date components etime Elapsed time

ti c Start a stopwatch timer toc Read the stopwatch timer

### colmmd

**Purpose** 

Sparse column minimum degree permutation

Syntax

p = col mmd(S)

**Description** 

 $p = col \ mmd(S)$  returns the column minimum degree permutation vector for the sparse matrix S. For a nonsymmetric matrix S, this is a column permutation p such that S(:,p) tends to have sparser LU factors than S.

The col mmd permutation is automatically used by  $\setminus$  and / for the solution of nonsymmetric and symmetric indefinite sparse linear systems.

Use spparms to change some options and parameters associated with heuristics in the algorithm.

**Algorithm** 

The minimum degree algorithm for symmetric matrices is described in the review paper by George and Liu [1]. For nonsymmetric matrices, MATLAB's minimum degree algorithm is new and is described in the paper by Gilbert, Moler, and Schreiber [2]. It is roughly like symmetric minimum degree for A' \*A, but does not actually form A' \*A.

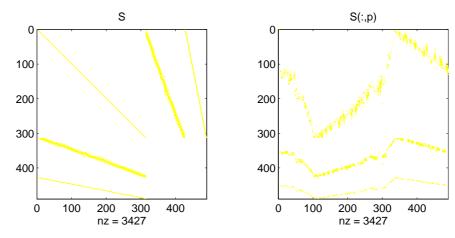
Each stage of the algorithm chooses a vertex in the graph of A'\*A of lowest degree (that is, a column of A having nonzero elements in common with the fewest other columns), eliminates that vertex, and updates the remainder of the graph by adding fill (that is, merging rows). If the input matrix S is of size m-by-n, the columns are all eliminated and the permutation is complete after n stages. To speed up the process, several heuristics are used to carry out multiple stages simultaneously.

**Examples** 

The Harwell-Boeing collection of sparse matrices includes a test matrix ABB313. It is a rectangular matrix, of order 313-by-176, associated with least squares adjustments of geodesic data in the Sudan. Since this is a least squares problem, form the augmented matrix (see spaugment), which is square and of order 489. The spy plot shows that the nonzeros in the original matrix are concentrated in two stripes, which are reflected and supplemented with a scaled identity in the augmented matrix. The col mmd ordering scrambles this

structure. (Note that this example requires the Harwell-Boeing collection of software.)

```
load('abb313.mat')
S = spaugment(A);
p = col mmd(S);
spy(S)
spy(S(:,p))
```

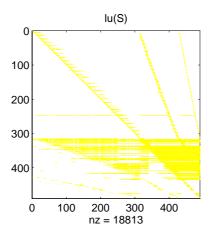


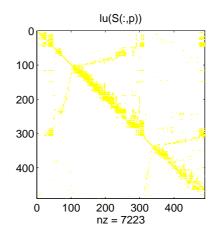
Comparing the spy plot of the LU factorization of the original matrix with that of the reordered matrix shows that minimum degree reduces the time and

## colmmd

storage requirements by better than a factor of 2.6. The nonzero counts are 18813 and 7223, respectively.

```
spy(lu(S))
spy(lu(S(:,p)))
```





#### See Also

\	Backslash or matrix left division
col perm	Sparse column permutation based on nonzero count
lu	LU matrix factorization
spparms	Set parameters for sparse matrix routines
symmmd	Sparse symmetric minimum degree ordering
symrcm	Sparse reverse Cuthill-McKee ordering

#### References

[1] George, Alan and Liu, Joseph, "The Evolution of the Minimum Degree Ordering Algorithm," *SIAM Review*, 1989, 31:1-19,.

[2] Gilbert, John R., Cleve Moler, and Robert Schreiber, "Sparse Matrices in MATLAB: Design and Implementation," *SIAM Journal on Matrix Analysis and Applications* 13, 1992, pp. 333-356.

Sparse column permutation based on nonzero count

**Syntax** 

j = colperm(S)

Description

 $j = col \, perm(S)$  generates a permutation vector j such that the columns of S(:,j) are ordered according to increasing count of nonzero entries. This is sometimes useful as a preordering for LU factorization; in this case use lu(S(:,j)).

If S is symmetric, then  $j = \text{col}\,\text{perm}(S)$  generates a permutation j so that both the rows and columns of S(j,j) are ordered according to increasing count of nonzero entries. If S is positive definite, this is sometimes useful as a preordering for Cholesky factorization; in this case use chol (S(j,j)).

**Algorithm** 

The algorithm involves a sort on the counts of nonzeros in each column.

**Examples** 

The n-by-n arrowhead matrix

```
A = [ones(1, n); ones(n-1, 1) speye(n-1, n-1)]
```

has a full first row and column. Its LU factorization,  $l\,u(A)$  , is almost completely full. The statement

```
j = colperm(A)
```

returns  $j = [2:n \ 1]$ . So A(j,j) sends the full row and column to the bottom and the rear, and lu(A(j,j)) has the same nonzero structure as A itself.

On the other hand, the Bucky ball example, B = bucky,

has exactly three nonzero elements in each row and column, so  $j = col \, perm(B)$  is the identity permutation and is no help at all for reducing fill-in with subsequent factorizations.

See Also

chol Cholesky factorization

col mmd Sparse minimum degree ordering

lu LU matrix factorization

symrcm Sparse reverse Cuthill-McKee ordering

## compan

**Purpose** 

Companion matrix

**Syntax** 

A = compan(u)

**Description** 

A = compan(u) returns the corresponding companion matrix whose first row is -u(2:n)/u(1), where u is a vector of polynomial coefficients. The eigenvalues of compan(u) are the roots of the polynomial.

**Examples** 

The polynomial  $(x-1)(x-2)(x+3) = x^3 - 7x + 6$  has a companion matrix given by

The eigenvalues are the polynomial roots:

This is also roots(u).

See Also

ei g Eigenvalues and eigenvectors
pol y Polynomial with specified roots
pol yval Polynomial evaluation
roots Polynomial roots

**Purpose** Identify the computer on which MATLAB is running

[str, maxsize] = computer

**Description** str = computer returns a string with the computer type on which MATLAB is running.

[str, maxsize] = computer returns the integer maxsize, which contains the maximum number of elements allowed in an array with this version of MATLAB.

The list of supported computers changes as new computers are added and others become obsolete.

String	Computer
SUN4	Sun4 SPARC workstation
S0L2	Solaris 2 SPARC workstation
PCWI N	MS-Windows
MAC2	All Macintosh
HP700	HP 9000/700
ALPHA	DEC Alpha
AXP_VMSG	Alpha VMS G_float
AXP_VMSI EEE	Alpha VMS IEEE
VAX_VMSD	VAX/VMS D_float

# computer

String	Computer
VAX_VMSG	VAX/VMS G_float
LNX86	Linux Intel
SGI	Silicon Graphics (R4000)
SGI 64	Silicon Graphics (R8000)
I BM_RS	IBM RS6000 workstation

### See Also

i si eee, i suni x, i svms

**Purpose** Condition number with respect to inversion

**Syntax** c = cond(X)

c = cond(X, p)

Description

The *condition number* of a matrix measures the sensitivity of the solution of a system of linear equations to errors in the data. It gives an indication of the accuracy of the results from matrix inversion and the linear equation solution. Values of cond(X) and cond(X, p) near 1 indicate a well-conditioned matrix.

c = cond(X) returns the 2-norm condition number, the ratio of the largest singular value of X to the smallest.

c = cond(X, p) returns the matrix condition number in p-norm:

norm(X, p) \* norm(inv(X), p)

If <i>p</i> is	Then $cond(X, p)$ returns the
1	1-norm condition number
2	2-norm condition number
'fro'	Frobenius norm condition number
i nf	Infinity norm condition number

**Algorithm** 

The algorithm for cond (when p = 2) uses the singular value decomposition, svd.

See Also

Condition number with respect to eigenvalues
1-norm matrix condition number estimate
Vector and matrix norms
Rank of a matrix
Singular value decomposition

References

[1] Dongarra, J.J., J.R. Bunch, C.B. Moler, and G.W. Stewart, *LINPACK Users' Guide*, SIAM, Philadelphia, 1979.

## condeig

**Purpose** Condition number with respect to eigenvalues

**Syntax** c = condeig(A)

[V, D, s] = condeig(A)

**Description** c = condeig(A) returns a vector of condition numbers for the eigenvalues of

A. These condition numbers are the reciprocals of the cosines of the angles

between the left and right eigenvectors.

[V, D, s] = condei g(A) is equivalent to: [V, D] = ei g(A); s = condei g(A);.

Large condition numbers imply that A is near a matrix with multiple eigen-

values.

**See Also** bal ance Improve accuracy of computed eigenvalues

cond Condition number with respect to inversion

ei g Eigenvalues and eigenvectors

**Purpose** 1-norm matrix condition number estimate

**Syntax** c = condest(A)

[c, v] = condest(A)

**Description** c = condest (A) uses Higham's modification of Hager's method to estimate

the condition number of a matrix. The computed c is a lower bound for the

condition of A in the 1-norm.

[c, v] = condest(A) estimates the condition number and also computes a

vector v such that ||Av|| = ||A|| ||v|| / c.

Thus, v is an approximate null vector of A if c is large.

This function handles both real and complex matrices. It is particularly useful

for sparse matrices.

See Also cond Condition number with respect to inversion

normest 2-norm estimate

**Reference** [1] Higham, N.J. "Fortran Codes for Estimating the One-Norm of a Real or

Complex Matrix, with Applications to Condition Estimation." ACM Trans.

Math. Soft., 14, 1988, pp. 381-396.

# conj

**Purpose** Complex conjugate

**Syntax** ZC = conj(Z)

**Description** ZC = conj(Z) returns the complex conjugate of the elements of Z.

**Algorithm** If Z is a complex array:

conj(Z) = real(Z) - i\*imag(Z)

**See Also** i, j Imaginary unit  $(\sqrt{-1})$ 

i mag Imaginary part of a complex number

real Real part of a complex number

Convolution and polynomial multiplication

**Syntax** 

w = conv(u, v)

**Description** 

w = conv(u, v) convolves vectors u and v. Algebraically, convolution is the same operation as multiplying the polynomials whose coefficients are the elements of u and v.

**Definition** 

Let  $m = l \operatorname{ength}(u)$  and  $n = l \operatorname{ength}(v)$ . Then w is the vector of length m+n-1 whose kth element is

$$w(k) = \sum_{j} u(j) v(k+1-j)$$

The sum is over all the values of j which lead to legal subscripts for u(j) and v(k+1-j), specifically j = max(1, k+1-n): min(k, m). When m = n, this gives

```
 \begin{aligned} & w(1) &= u(1) * v(1) \\ & w(2) &= u(1) * v(2) + u(2) * v(1) \\ & w(3) &= u(1) * v(3) + u(2) * v(2) + u(3) * v(1) \\ & \dots \\ & w(n) &= u(1) * v(n) + u(2) * v(n-1) + \dots + u(n) * v(1) \\ & \dots \\ & w(2*n-1) &= u(n) * v(n) \end{aligned}
```

**Algorithm** 

The convolution theorem says, roughly, that convolving two sequences is the same as multiplying their Fourier transforms. In order to make this precise, it is necessary to pad the two vectors with zeros and ignore roundoff error. Thus, if

```
X = fft([x zeros(1, length(y)-1)]) and Y = fft([y zeros(1, length(x)-1)])
then conv(x, y) = ifft(X. *Y)
```

See Also

convmtx, xconv2, xcorr, in the Signal Processing Toolbox, and:

deconv
filter

Deconvolution and polynomial division
Filter data with an infinite impulse response (IIR) or
finite impulse response (FIR) filter

Two-dimensional convolution

### Syntax

```
C = conv2(A, B)
C = conv2(hcol, hrow, A)
C = conv2(..., 'shape')
```

# Description

C = conv2(A, B) computes the two-dimensional convolution of matrices A and B. If one of these matrices describes a two-dimensional FIR filter, the other matrix is filtered in two dimensions.

The size of C in each dimension is equal to the sum of the corresponding dimensions of the input matrices, minus one. That is, if the size of A is [ma, na] and the size of B is [mb, nb], then the size of C is [ma+mb-1, na+nb-1].

C = conv2(hcol, hrow, A) convolves A separably with hcol in the column direction and hrow in the row direction, hcol and hrow should both be vectors.

C = conv2(..., 'shape') returns a subsection of the two-dimensional convolution, as specified by the *shape* parameter:

full Returns the full two-dimensional convolution (default).

same Returns the central part of the convolution of the same size as A.

valid Returns only those parts of the convolution that are computed without the zero-padded edges. Using this option, C has size [ma-mb+1, na-nb+1] when size(A) > size(B).

# **Examples**

In image processing, the Sobel edge finding operation is a two-dimensional convolution of an input array with the special matrix

```
s = [1 \ 2 \ 1; \ 0 \ 0 \ 0; \ -1 \ -2 \ -1];
```

These commands extract the horizontal edges from a raised pedestal:

```
A = zeros(10);
A(3:7,3:7) = ones(5);
H = conv2(A,s);
mesh(H)
```

These commands display first the vertical edges of A, then both horizontal and vertical edges.

```
V = conv2(A, s');

mesh(V)

mesh(sqrt(H.^2+V.^2))
```

# See Also

conv Convolution and polynomial multiplication deconv Deconvolution and polynomial division

filter2 Two-dimensional digital filtering

xcorr2 Two-dimensional cross-correlation (see Signal

Processing Toolbox)

# convhull

**Purpose** 

Convex hull

**Syntax** 

K = convhull(x, y)K = convhull(x, y, TRI)

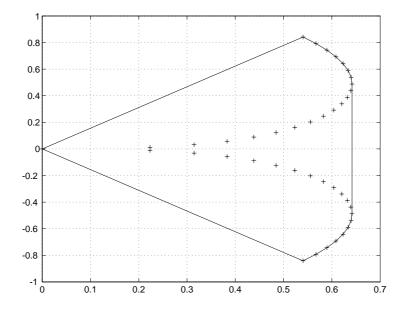
**Description** 

K = convhull(x, y) returns indices into the x and y vectors of the points on the convex hull.

K = convhull(x, y, TRI) uses the triangulation (as obtained from del aunay) instead of computing it each time.

**Examples** 

```
xx = -1:.05:1; yy = abs(sqrt(xx));
[x, y] = pol2cart(xx, yy);
k = convhull(x, y);
plot(x(k), y(k), 'r-', x, y, 'b+')
```



See Also

del aunay pol yarea voronoi Delauney triangulation Area of polygon Voronoi diagram **Purpose** N-dimensional convolution

**Syntax** C = convn(A, B)

C = convn(A, B, 'shape')

**Description** C = convn(A, B) computes the N-dimensional convolution of the arrays A and

B. The size of the result is size(A) + size(B) - 1.

C = convn(A, B, 'shape') returns a subsection of the N-dimensional convolution, as specified by the *shape* parameter:

• 'full' returns the full N-dimensional convolution (default).

• 'same' returns the central part of the result that is the same size as A.

• 'valid' returns only those parts of the convolution that can be computed without assuming that the array A is zero-padded. The size of the result is

 $\max(\operatorname{size}(A) - \operatorname{size}(B) + 1, 0)$ .

See Also Convolution and polynomial multiplication

conv2 Two-dimensional convolution

# corrcoef

**Purpose** Correlation coefficients

Syntax S = corrcoef(X)
S = corrcoef(x, y)

**Description** S = corrcoef(X) returns a matrix of correlation coefficients calculated from an input matrix whose rows are observations and whose columns are variables. The matrix S = corrcoef(X) is related to the covariance matrix C = cov(X) by

$$S(i,j) = \frac{C(i,j)}{\sqrt{C(i,i)C(j,j)}}$$

corrcoef(X) is the zeroth lag of the covariance function, that is, the zeroth lag of xcov(x, 'coeff') packed into a square array.

S = corrcoef(x, y) where x and y are column vectors is the same as  $corrcoef([x \ y])$ .

**See Also** xcorr, xcov in the Signal Processing Toolbox, and:

cov Covariance matrix

mean Average or mean value of arrays

std Standard deviation

Cosine and hyperbolic cosine

**Syntax** 

$$Y = cos(X)$$
  
 $Y = cosh(X)$ 

**Description** 

The cos and cosh functions operate element-wise on arrays. The functions' domains and ranges include complex values. All angles are in radians.

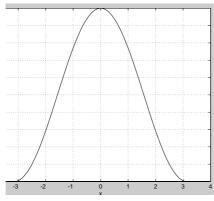
Y = cos(X) returns the circular cosine for each element of X.

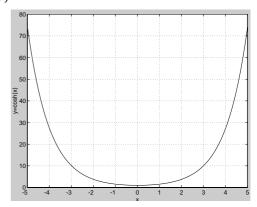
Y = cosh(X) returns the hyperbolic cosine for each element of X.

**Examples** 

Graph the cosine function over the domain  $-\pi \le x \le \pi$ , and the hyperbolic cosine function over the domain  $-5 \le x \le 5$ .

$$x = -pi : 0.01: pi; plot(x, cos(x))$$
  
 $x = -5: 0.01: 5; plot(x, cosh(x))$ 





The expression  $\cos(pi/2)$  is not exactly zero but a value the size of the floating-point accuracy, eps, because pi is only a floating-point approximation to the exact value of  $\pi$ .

**Algorithm** 

$$\cos(x+iy) = \cos(x)\cosh(y) - i\sin(x)\sin(y)$$

$$\cos(z) = \frac{e^{iz} + e^{-iz}}{2}$$

$$\cosh(z) = \frac{e^z + e^{-z}}{2}$$

See Also

acos, acosh

Inverse cosine and inverse hyperbolic cosine

# cot, coth

**Purpose** 

Cotangent and hyperbolic cotangent

**Syntax** 

$$Y = \cot(X)$$
  
 $Y = \coth(X)$ 

**Description** 

The  $\cot$  and  $\coth$  functions operate element-wise on arrays. The functions' domains and ranges include complex values. All angles are in radians.

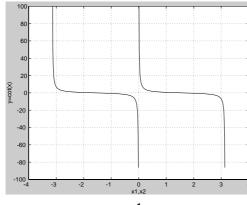
 $Y = \cot(X)$  returns the cotangent for each element of X.

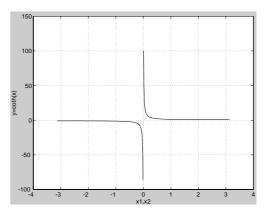
Y = coth(X) returns the hyperbolic cotangent for each element of X.

**Examples** 

Graph the cotangent and hyperbolic cotangent over the domains  $-\pi < x < 0$  and  $0 < x < \pi$ .

$$x1 = -pi + 0.01: 0.01: -0.01; x2 = 0.01: 0.01: pi -0.01;$$
  
 $pl ot(x1, cot(x1), x2, cot(x2))$   
 $pl ot(x1, coth(x1), x2, coth(x2))$ 





**Algorithm** 

$$\cot(z) = \frac{1}{\tan(z)}$$

$$\coth(z) = \frac{1}{\tanh(z)}$$

See Also

acot, acoth

 $Inverse\ cotangent\ and\ inverse\ hyperbolic\ cotangent$ 

Covariance matrix

**Syntax** 

$$C = cov(X)$$
  
 $C = cov(x, y)$ 

Description

C = cov(x) where x is a vector returns the variance of the vector elements. For matrices where each row is an observation and each column a variable, cov(x) is the covariance matrix. di ag(cov(x)) is a vector of variances for each column, and  $sqrt(di \, ag(cov(x)))$  is a vector of standard deviations.

C = cov(x, y), where x and y are column vectors of equal length, is equivalent to  $cov([x \ y])$ .

Remarks

cov removes the mean from each column before calculating the result.

The covariance function is defined as

$$cov(x_1, x_2) = E[(x_1 - \mu_1)(x_2 - \mu_2)]$$

where E is the mathematical expectation and  $\mu_i = Ex_i$ .

**Examples** 

Consider  $A = \begin{bmatrix} -1 & 1 & 2 & ; & -2 & 3 & 1 & ; & 4 & 0 & 3 \end{bmatrix}$ . To obtain a vector of variances for each column of A:

Compare vector v with covariance matrix C:

The diagonal elements C(i,i) represent the variances for the columns of A. The off-diagonal elements C(i,j) represent the covariances of columns i and j.

See Also

xcorr, xcov in the Signal Processing Toolbox, and:

corrcoef Correlation coefficients
mean Average or mean value of arrays

std Standard deviation

# cplxpair

### **Purpose**

Sort complex numbers into complex conjugate pairs

### **Syntax**

B = cpl xpai r(A)

B = cpl xpai r(A, tol)

B = cpl xpai r(A, [], dim)

B = cpl xpai r(A, tol, dim)

# Description

 $B = cpl \, xpai \, r(A)$  sorts the elements along different dimensions of a complex array, grouping together complex conjugate pairs.

The conjugate pairs are ordered by increasing real part. Within a pair, the element with negative imaginary part comes first. The purely real values are returned following all the complex pairs. The complex conjugate pairs are forced to be exact complex conjugates. A default tolerance of 100\*eps relative to abs(A(i)) determines which numbers are real and which elements are paired complex conjugates.

If A is a vector,  $\operatorname{cpl} \operatorname{xpai} r(A)$  returns A with complex conjugate pairs grouped together.

If A is a matrix, cpl xpai r(A) returns A with its columns sorted and complex conjugates paired.

If A is a multidimensional array, cpl xpai r(A) treats the values along the first non-singleton dimension as vectors, returning an array of sorted elements.

B = cpl xpai r(A, tol) overrides the default tolerance.

B = cpl xpai r(A, [], dim) sorts A along the dimension specified by scalar dim

 $B = cpl \ xpai \ r(A, tol, dim)$  sorts A along the specified dimension and overrides the default tolerance.

# **Diagnostics**

If there are an odd number of complex numbers, or if the complex numbers cannot be grouped into complex conjugate pairs within the tolerance, cpl xpai r generates the error message:

Complex numbers can't be paired.

Purpose Elapsed CPU time

Syntax cputime

**Description** cputime returns the total CPU time (in seconds) used by MATLAB from the

time it was started. This number can overflow the internal representation and

wrap around.

**Examples** For example

t = cputime; surf(peaks(40)); e = cputime-t

e =

0.4667

returns the CPU time used to run surf(peaks(40)).

See Also clock Current time as a date vector

etime Elapsed time tic, toc Stopwatch timer

Vector cross product

### **Syntax**

W = cross(U, V)
W = cross(U, V, di m)

# **Description**

W = cross(U, V) returns the cross product of the vectors U and V. That is,  $W = U \times V$ . U and V are usually 3-element vectors. If U and V are multidimensional arrays, cross returns the cross product of U and V along the first dimension of length 3.

If U and V are arrays, cross(U, V) treats the first size 3 dimension of U and V as vectors, returning pages whose columns are cross products.

W = cross(U, V, dim) where U and V are multidimensional arrays, returns the cross product of U and V in dimension dim. U and V must have the same size, and both size(U, dim) and size(V, dim) must be 3.

### **Remarks**

To perform a dot (scalar) product of two vectors of the same size, use:

c = sum(a. \*b) or, if a and b are row vectors, c = a. '\*b.

# **Examples**

The cross and dot products of two vectors are calculated as shown:

```
a = [1 2 3]; b = [4 5 6];
c = cross(a, b)
c = 
    -3 6 -3
d = sum(a. *b)
d = 
    32
```

Cosecant and hyperbolic cosecant

**Syntax** 

$$Y = \csc(x)$$
  
 $Y = \operatorname{csch}(x)$ 

**Description** 

The  $_{\mbox{CSC}}$  and  $_{\mbox{CSCh}}$  functions operate element-wise on arrays. The functions' domains and ranges include complex values. All angles are in radians.

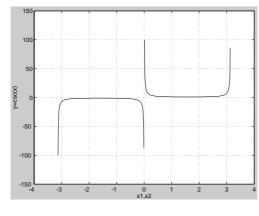
 $Y = \csc(x)$  returns the cosecant for each element of x.

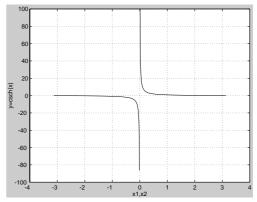
Y = csch(x) returns the hyperbolic cosecant for each element of x.

**Examples** 

Graph the cosecant and hyperbolic cosecant over the domains  $-\pi < x < 0 \,$  and  $0 < x < \pi$  .

$$x1 = -pi + 0.01$$
: 0.01: -0.01;  $x2 = 0.01$ : 0.01:  $pi - 0.01$ ;  $pl ot(x1, csc(x1), x2, csc(x2))$   $pl ot(x1, csch(x1), x2, csch(x2))$ 





**Algorithm** 

$$\csc(z) = \frac{1}{\sin(z)}$$

$$\operatorname{csch}(z) = \frac{1}{\sinh(z)}$$

See Also

acsc, acsch

Inverse cosecant and inverse hyperbolic cosecant

# cumprod

### **Purpose**

Cumulative product

### **Syntax**

B = cumprod(A)

B = cumprod(A, dim)

# **Description**

B = cumprod(A) returns the cumulative product along different dimensions of an array.

If A is a vector, cumprod(A) returns a vector containing the cumulative product of the elements of A.

If A is a matrix, cumprod(A) returns a matrix the same size as A containing the cumulative products for each column of A.

If A is a multidimensional array, cumprod(A) works on the first nonsingleton dimension.

B = cumprod(A, dim) returns the cumulative product of the elements along the dimension of A specified by scalar dim. For example, cumprod(A, 1) increments the first (row) index, thus working along the rows of A.

# **Examples**

$$cumprod(1:5) = [1 2 6 24 120]$$

$$A = [1 \ 2 \ 3; \ 4 \ 5 \ 6];$$

$$\begin{array}{cccc} 1 & 2 & 3 \\ 4 & 10 & 18 \end{array}$$

# See Also

cumsum Cumulative sum

prod Product of array elements sum Sum of array elements

**Cumulative sum** 

**Syntax** 

B = cumsum(A) B = cumsum(A, di m)

**Description** 

B = cumsum(A) returns the cumulative sum along different dimensions of an array.

If A is a vector, cumsum(A) returns a vector containing the cumulative sum of the elements of A.

If A is a matrix, cumsum(A) returns a matrix the same size as A containing the cumulative sums for each column of A.

If A is a multidimensional array, cumsum(A) works on the first nonsingleton dimension.

B = cumsum(A, di m) returns the cumulative sum of the elements along the dimension of A specified by scalar di m. For example, cumsum(A, 1) works across the first dimension (the rows).

**Examples** 

$$cumsum(1:5) = [1 \ 3 \ 6 \ 10 \ 15]$$

$$A = [1 \ 2 \ 3; \ 4 \ 5 \ 6];$$

See Also

sum Sum of array elements

prod Product of array elements

cumprod Cumulative product of elements

Cumulative trapezoidal numerical integration

### **Syntax**

Z = cumtrapz(Y)
Z = cumtrapz(X, Y)
Z = cumtrapz(... dim)

# Description

Z = cumtrapz(Y) computes an approximation of the cumulative integral of Y via the trapezoidal method with unit spacing. (This is similar to cumsum(Y), except that trapezoidal approximation is used.) To compute the integral with other than unit spacing, multiply Z by the spacing increment.

For vectors, cumtrapz(Y) is the cumulative integral of Y.

For matrices, cumtrapz(Y) is a row vector with the cumulative integral over each column.

For multidimensional arrays, cumtrapz(Y) works across the first nonsingleton dimension.

Z = cumtrapz(X, Y) computes the cumulative integral of Y with respect to X using trapezoidal integration. X and Y must be vectors of the same length, or X must be a column vector and Y an array.

If X is a column vector and Y an array whose first nonsingleton dimension is  $l \, ength(X)$ , cumtrapz(X,Y) operates across this dimension.

Z = cumtrapz(...dim) integrates across the dimension of Y specified by scalar dim. The length of X must be the same as size(Y, dim).

# **Example**

Example: If  $Y = [0 \ 1 \ 2; \ 3 \ 4 \ 5]$ 

#### and

# cumtrapz

See Also cumsum Cumulative sum

trapz Trapezoidal numerical integration

# cumtrapz

**Purpose** Current date string

Syntax str = date

**Description** str = date returns a string containing the date in dd-mmm-yyyy format.

See Also clock Current time as a date vector

datenum Serial date number now Current date and time

# datenum

## **Purpose**

Serial date number

### Syntax

N = datenum(str)

N = datenum(Y, M, D)

N = datenum(Y, M, D, H, MI, S)

# Description

The datenum function converts date strings and date vectors into serial date numbers. Date numbers are serial days elapsed from some reference date. By default, the serial day 1 corresponds to 1-Jan-0000.

N = datenum(str) converts the date string str into a serial date number.

**NOTE** The string str must be in one of the date formats 0, 1, 2, 6, 13, 14, 15, or 16 as defined by datestr.

N = datenum(Y, M, D) returns the serial date number for corresponding elements of the Y, M, and D (year, month, day) arrays. Y, M, and D must be arrays of the same size (or any can be a scalar). Values outside the normal range of each array are automatically "carried" to the next unit.

N = datenum(Y, M, D, H, MI, S) returns the serial date number for corresponding elements of the Y, M, D, H, MI, and S (year, month, hour, minute, and second) array values. Y, M, D, H, MI, and S must be arrays of the same size (or any can be a scalar).

# **Examples**

```
n = datenum('19-May-1995') returns n = 728798.
```

n = datenum(1994, 12, 19) returns n = 728647.

 $n \ = \ dat\,enum(\,1994,\,12,\,19,\,18,\,0,\,0) \ returns \, n \ = \ 7.\,\,2865e{+}05 \; .$ 

### See Also

datestr	Date string format
datevec	Date components
now	Current date and time

Date string format

**Syntax** 

str = datestr(D, dateform)

Description

str = datestr(D, dateform) converts each element of the array of serial date numbers (D) to a string. Optional argument dateform specifies the date format of the result, where dateform can be either a number or a string:

dateform (number)	dateform (string)	Example
0	' dd- mmm- yyyy HH: MM: SS'	01-Mar-1995 03:45
1	' dd- mmm- yyyy'	01-Mar-1995
2	'mm/dd/yy'	03/01/95
3	' mmm'	Mar
4	' m'	M
5	' mm'	3
6	'mm/dd'	03/01
7	' dd'	1
8	' ddd'	Wed
9	' d'	W
10	'yyyy'	1995
11	'yy'	95
12	'mmmyy'	Mar95
13	'HH: MM: SS'	15: 45: 17

dateform (number)	dateform (string)	Example
14	' HH: MM: SS PM'	03: 45: 17 PM
15	' HH: MM'	15: 45
16	' HH: MM PM'	03: 45 PM
17	' QQ- YY'	Q1-96
18	' QQ'	Q1

**NOTE** *dateform* numbers 0, 1, 2, 6, 13, 14, 15, and 16 produce a string suitable for input to datenum or datevec. Other date string formats will not work with these functions.

Time formats like 'h: m: s', 'h: m: s. s', 'h: m pm', ... may also be part of the input array D. If you do not specify dateform, the date string format defaults to

- 1, if D contains date information only (01-Mar-1995)
- 16, if D contains time information only (03:45 PM)
- 0, if D contains both date and time information (01-Mar-1995 03:45)

### See Also

date	Current date string
datenum	Serial date number
datevec	Date components

## Date components

```
C = datevec(A)
[Y, M, D, H, MI, S] = datevec(A)
```

### Description

C = datevec(A) splits its input into an n-by-6 array with each row containing the vector [Y, M, D, H, M, S]. The first five date vector elements are integers. Input A can either consist of strings of the sort produced by the datestr function, or scalars of the sort produced by the datenum and now functions.

[Y, M, D, H, M, S] = datevec(A) returns the components of the date vector as individual variables.

When creating your own date vector, you need not make the components integers. Any components that lie outside their conventional ranges affect the next higher component (so that, for instance, the anomalous June 31 becomes July 1). A zeroth month, with zero days, is allowed.

# **Examples**

Let

d = '12/24/1984' t = '725000.00',

Then datevec(d) and datevec(t) generate [1984 12 24 0 0 0].

#### See Also

cl ock
dat enum
Current time as date vector
Serial date number

datestr Date string format

# dbclear

**Purpose** 

Clear breakpoints

Syntax

dbcl ear

dbclear at *lineno* in *function* 

dbclear all in function

dbclear all

dbclear in mfilename

dbclear if keyword

where *keyword* is one of:

error nani nf i nfnan warni ng

Description

The at, i n, and i f keywords, familiar to users of the UNIX debugger dbx, are optional.

dbclear, by itself, clears the breakpoint(s) set by a corresponding dbstop command.

dbcl ear at *lineno* in *function* clears the breakpoint set at the specified line in the specified M-file. *function* must be the name of an M-file function or a MATLABPATH relative partial pathname.

dbclear all in function clears all breakpoints in the specified M-file.

dbclear all clears all breakpoints in all M-file functions, except for errors and warning breakpoints.

dbcl ear in *function* clears the breakpoint set at the first executable line in the specified M-file.

dbcl ear if keyword clears the indicated statement or breakpoint:

dbcl ear if error Clears the dbstop error statement, if set. If a

runtime error occurs after this command, MATLAB terminates the current operation and

returns to the base workspace.

dbcl ear if naninf Clears the dbstop naninf statement, if set.

dbcl ear if infnan Clears the dbst op infnan statement, if set.

dbcl ear if warning Clears warning breakpoints.

See Also dbcont 2-Resume execution

dbdown 2-Change local workspace context (down)

dbqui t 2-Quit debug mode

dbstack 2-Display function call stack

dbstatus 2-List all breakpoints

dbstep 2-Execute one or more lines from a breakpoint

dbstop 2-Set breakpoints in an M-file function

dbtype 2-List M-file with line numbers

dbup 2-Change local workspace context (up)

See also 2-partialpath.

# dbcont

**Purpose** Resume execution

Syntax dbcont

**Description** dbcont resumes execution of an M-file from a breakpoint. Execution continues

until either another breakpoint is encountered, an error occurs, or MATLAB

returns to the base workspace prompt.

See Also dbcl ear 2-Clear breakpoints

dbdown 2-Change local workspace context (down)

dbqui t 2-Quit debug mode

dbstack 2-Display function call stack

dbstatus 2-List all breakpoints

dbstep 2-Execute one or more lines from a breakpoint

dbstop 2-Set breakpoints in an M-file function

dbtype 2-List M-file with line numbers

Purpose Change local workspace context

Syntax dbdown

**Description** dbdown changes the current workspace context to the workspace of the called

M-file when a breakpoint is encountered. You must have issued the dbup command at least once before you issue this command. dbdown is the opposite

of dbup.

Multiple dbdown commands change the workspace context to each successively executed M-file on the stack until the current workspace context is the current breakpoint. It is not necessary, however, to move back to the current break-

point to continue execution or to step to the next line.

See Also dbcl ear 2-Clear breakpoints

dbcont 2-Resume execution dbqui t 2-Quit debug mode

dbstack 2-Display function call stack

dbstatus 2-List all breakpoints

dbstep 2-Execute one or more lines from a breakpoint

dbstop 2-Set breakpoints in an M-file function

dbtype 2-List M-file with line numbers

Numerical double integration

### **Syntax**

```
result = dbl quad('fun', i nmi n, i nmax, outmi n, outmax)
result = dbl quad('fun', i nmi n, i nmax, outmi n, outmax, tol, trace)
result = dbl quad('fun', i nmi n, i nmax, outmi n, outmax, tol, trace, order)
```

## Description

result = dbl quad('fun', i nmi n, i nmax, out mi n, out max) evaluates the double integral fun(i nner, outer) using the quad quadrature function. i nner is the inner variable, ranging from i nmi n to i nmax, and outer is the outer variable, ranging from out mi n to out max. The first argument 'fun' is a string representing the integrand function. This function must be a function of two variables of the form fout = fun(i nner, outer). The function must take a vector i nner and a scalar outer and return a vector fout that is the function evaluated at outer and each value of i nner.

result = dbl quad(' fun', i nmi n, i nmax, outmi n, outmax, tol, trace) passes tol and trace to the quad function. See the help entry for quad for a description of the tol and trace parameters.

 $result = dbl \, quad('fun', inmin, inmax, outmin, outmax, tol, trace, order) \\ passes tol and trace to the quad or quad8 function depending on the value of the string order. Valid values for order are 'quad' and 'quad8' or the name of any user-defined quadrature method with the same calling and return arguments as quad and quad8.$ 

# **Example**

result = dbl quad(' i ntegrnd' , pi , 2\*pi , 0, pi ) integrates the function y\*sin(x)+x\*cos(y), where x ranges from  $\pi$  to  $2\pi$ , and y ranges from 0 to  $\pi$ , assuming:

- x is the inner variable in the integration.
- y is the outer variable.
- the M-file integrnd. m is defined as:

```
function out = integrnd(x, y)
out = y*sin(x)+x*cos(y);
```

Note that i ntegrnd. m is valid when x is a vector and y is a scalar. Also, x must be the first argument to i ntegrnd. m since it is the inner variable.

# dblquad

See Also

2- quad, quad8

2-Numerical evaluation of integrals

# dbmex

**Purpose** Enable MEX-file debugging

Syntax dbmex on

dbmex off
dbmex stop
dbmex print

**Description** dbmex on enables MEX-file debugging. To use this option, first start MATLAB

from within a debugger by typing: matlab -Ddebugger, where debugger is the

name of the debugger.

dbmex off disables MEX-file debugging.

dbmex stop returns to the debugger prompt.

dbmex print displays MEX-file debugging information.

dbmex is not available on the Macintosh or the PC.

**See Also** dbstop 2-Set breakpoints in an M-file function

dbcl ear2-Clear breakpointsdbcont2-Resume execution

dbdown 2-Change local workspace context (down)

dbqui t 2-Quit debug mode

dbstack 2-Display function call stack

dbstatus 2-List all breakpoints

dbstep 2-Execute one or more lines from a breakpoint

dbtype 2-List M-file with line numbers

Purpose Quit debug mode

Syntax dbqui t

**Description** dbquit immediately terminates the debugger and returns control to the base

workspace prompt. The M-file being processed is not completed and no results

are returned.

All breakpoints remain in effect.

See Also dbcl ear 2-Clear breakpoints

dbcont 2-Resume execution

dbdown 2-Change local workspace context (down)

dbstack 2-Display function call stack

dbstatus 2-List all breakpoints

dbstep 2-Execute one or more lines from a breakpoint

dbstop 2-Set breakpoints in an M-file function

dbtype 2-List M-file with line numbers

# dbstack

**Purpose** Display function call stack

Syntax dbstack

[ST, I] = dbstack

Description

dbstack displays the line numbers and M-file names of the function calls that led to the current breakpoint, listed in the order in which they were executed. In other words, the line number of the most recently executed function call (at which the current breakpoint occurred) is listed first, followed by its calling function, which is followed by its calling function, and so on, until the topmost M-file function is reached.

[ST, I] = dbstack returns the stack trace information in an m-by-1 structure ST with the fields:

name function name

line function line number

The current workspace index is returned in I.

**Examples** 

>> dbstack

> In /usr/local/matlab/toolbox/matlab/cond.m at line 13

In test1.m at line 2 In test.m at line 3

See Also

dbcl ear 2-Clear breakpoints dbcont 2-Resume execution

dbdown 2-Change local workspace context (down)

dbqui t Quit debug mode dbstatus 2-List all breakpoints

dbstep 2-Execute one or more lines from a breakpoint

dbstop 2-Set breakpoints in an M-file function

dbtype 2-List M-file with line numbers

**Purpose** List all breakpoints

**Syntax** dbstatus

> dbstatus function s = dbstatus(...)

**Description** 

dbstatus, by itself, lists all breakpoints in effect including error, warning, and nani nf.

dbstatus function displays a list of the line numbers for which breakpoints are set in the specified M-file.

s = dbstatus(...)returns the breakpoint information in an m-by-1 structure with the fields:

function name name

line vector of breakpoint line numbers

cond condition string (error, warning, or naninf)

Use dbstatus class/function or dbstatus private/function or dbstatus *class*/pri vate/function to determine the status for methods, private functions, or private methods (for a class named class). In all of these forms you can further qualify the function name with a subfunction name as in dbstatus function/subfunction.

See Also

dbcl ear	2-Clear breakpoints
dbcont	2-Resume execution
dbdown	2-Change local workspace context (down)
dbqui t	2-Quit debug mode
dbstack	2-Display function call stack
dbstep	2-Execute one or more lines from a breakpoint
dbstop	2-Set breakpoints in an M-file function
dbtype	2-List M-file with line numbers
dbup	2-Change local workspace context (up)

# dbstep

**Purpose** Execute one or more lines from a breakpoint

Syntax dbstep

dbstep nlines dbstep in

**Description** This command allows you to debug an M-file by following its execution from the

current breakpoint. At a breakpoint, the dbstep command steps through execution of the current M-file one line at a time or at the rate specified by nl i nes.

dbstep, by itself, executes the next executable line of the current M-file. dbstep steps over the current line, skipping any breakpoints set in functions called by that line.

dbstep nlines executes the specified number of executable lines.

dbstep in steps to the next executable line. If that line contains a call to another M-file, execution resumes with the first executable line of the called file. If there is no call to an M-file on that line, dbstep in is the same as dbstep.

See Also dbcl ear 2-Clear breakpoints

dbcont 2-Resume execution

dbdown 2-Change local workspace context (down)

dbqui t 2-Quit debug mode

dbstack 2-Display function call stack

dbstatus List all breakpoints

dbstop 2-Set breakpoints in an M-file function

dbtype 2-List M-file with line numbers

**Purpose** Set breakpoints in an M-file function

**Syntax** dbstop at *lineno* in *function* 

dbstop in function

dbstop if keyword where keyword is one of:

error nani nf i nfnan warni ng

#### Description

The dbst op command sets up MATLAB's debugging mode. dbst op sets a breakpoint at a specified location in an M-file function or causes a break in case an error or warning occurs during execution. When the specified dbst op condition is met, the MATLAB prompt is displayed and you can issue any valid MATLAB command.

dbstop at *lineno* in *function* stops execution just prior to execution of that line of the specified M-file function. *function* must be the name of an M-file function or a MATLABPATH relative partial pathname.

dbstop in *function* stops execution before the first executable line in the M-file function when it is called.

dbstop if *keyword* stops execution under the specified conditions:

dbstop if error Stops execution if a runtime error occurs in any

M-file function. You can examine the local

workspace and sequence of function calls leading

to the error, but you cannot resume M-file

execution after a runtime error.

dbstop if naninf Stops execution when it detects Not-a-Number

(NaN) or Infinity (Inf).

dbstop if infnan Stops execution when it detects Not-a-Number

(NaN) or Infinity (Inf).

dbstop if warning Stops execution if a runtime warning occurs in

any M-file function.

Regardless of the form of the dbstop command, when a stop occurs, the line or error condition that caused the stop is displayed. To resume M-file function

execution, issue a dbcont command or step to another line in the file with the dbstep command.

Any breakpoints set by the first two forms of the dbst op command are cleared if the M-file function is edited or cleared.

The at, in, and if keywords, familiar to users of the UNIX debugger dbx, are optional.

# **Examples**

Here is a short example, printed with the dbtype command to produce line numbers.

```
dbtype buggy
1  function z = buggy(x)
2  n = length(x);
3  z = (1:n)./x;
```

The statement

```
dbstop in buggy
```

causes execution to stop at line 2, the first executable line. The command

```
dbstep
```

then advances to line 3 and allows the value of n to be examined.

The example function only works on vectors; it produces an error if the input  ${\bf x}$  is a full matrix. So the statements

```
dbstop if error
buggy(magic(3))

produce

Error using ==>./
Matrix dimensions must agree.
Error in ==> buggy.m
On line 3 ==> z = (1:n)./x;
```

Finally, if any of the elements of the input  ${\bf x}$  are zero, a division by zero occurs. For example, consider

```
dbstop if naninf buggy(0:2)
```

# which produces

```
Warning: Divide by zero
NaN/Inf debugging breakpoint hit on line 2.
Stopping at next line.
2  n = length(x);
3  z = (1:n)./x;
```

#### See Also

dbcl ear 2-Clear breakpoints dbcont 2-Resume execution

dbdown 2-Change local workspace context (down)

dbqui t 2-Quit debug mode

dbstack 2-Display function call stack

dbstatus List all breakpoints

dbstep 2-Execute one or more lines from a breakpoint

dbtype 2-List M-file with line numbers

dbup 2-Change local workspace context (up)

See also 2-partialpath.

# dbtype

**Purpose** List M-file with line numbers

**Syntax** dbtype function

dbtype function start: end

**Description** dbtype *function* displays the contents of the specified M-file function with

line numbers preceding each line. function must be the name of an M-file func-

tion or a MATLABPATH relative partial pathname.

dbtype function start: end displays the portion of the file specified by a

range of line numbers.

See Also dbcl ear 2-Clear breakpoints

dbcont 2-Resume execution

dbdown 2-Change local workspace context (down)

dbqui t 2-Quit debug mode

dbstack 2-Display function call stack

dbstatus List all breakpoints

dbstep 2-Execute one or more lines from a breakpoint

dbstop 2-Set breakpoints in an M-file function dbup 2-Change local workspace context (up)

See also 2-partialpath.

Purpose Change local workspace context

Syntax dbup

**Description** This command allows you to examine the calling M-file by using any other

MATLAB command. In this way, you determine what led to the arguments

being passed to the called function.

dbup changes the current workspace context (at a breakpoint) to the work-

space of the calling M-file.

Multiple dbup commands change the workspace context to each previous calling M-file on the stack until the base workspace context is reached. (It is not necessary, however, to move back to the current breakpoint to continue

execution or to step to the next line.)

See Also dbcl ear 2-Clear breakpoints

dbcont 2-Resume execution

dbdown 2-Change local workspace context (down)

dbqui t 2-Quit debug mode

dbstack 2-Display function call stack

dbstatus List all breakpoints

dbstep 2-Execute one or more lines from a breakpoint

dbstop 2-Set breakpoints in an M-file function

dbtype 2-List M-file with line numbers

Set up advisory link

#### Syntax

rc = ddeadv(channel, 'item', 'callback')

rc = ddeadv(channel, 'item', 'callback', 'upmtx')

rc = ddeadv(channel, 'item', 'callback', 'upmtx', format)

rc = ddeady(channel, 'item', 'callback', 'upmtx', format, timeout)

# Description

ddeady sets up an advisory link between MATLAB and a server application. When the data identified by the item argument changes, the string specified by the call back argument is passed to the eval function and evaluated. If the advisory link is a hot link, DDE modifies upmtx, the update matrix, to reflect the data in i tem.

If you omit optional arguments that are not at the end of the argument list, you must substitute the empty matrix for the missing argument(s).

# **Arguments**

Return code: 0 indicates failure. 1 indicates success. rc

Conversation channel from ddei ni t. channel

item String specifying the DDE item name for the advisory link.

Changing the data identified by item at the server triggers the

advisory link.

call back String specifying the callback that is evaluated on update

notification. Changing the data identified by i tem at the server

causes call back to get passed to the eval function to be

evaluated.

upmtx String specifying the name of a matrix that holds data sent (optional) with an update notification. If upmtx is included, changing

> item at the server causes upmtx to be updated with the revised data. Specifying upmtx creates a hot link. Omitting upmtx or specifying it as an empty string creates a warm link. If upmtx exists in the workspace, its contents are overwritten. If upmtx

does not exist, it is created.

format (optional)

Two-element array specifying the format of the data to be sent on update. The first element specifies the Windows clipboard format to use for the data. The only currently supported format is cf\_text, which corresponds to a value of 1. The second element specifies the type of the resultant matrix. Valid types are numeric (the default, which corresponds to a value of 0) and string (which corresponds to a value of 1). The default format array is [1 0].

ti meout (*optional*) Scalar specifying the time-out limit for this operation. ti meout is specified in milliseconds. (1000 milliseconds = 1 second). If advisory link is not established within ti meout milliseconds, the function fails. The default value of ti meout is three seconds.

# **Examples**

Set up a hot link between a range of cells in Excel (Row 1, Column 1 through Row 5, Column 5) and the matrix x. If successful, display the matrix:

```
rc = ddeadv(channel, 'r1c1: r5c5', 'disp(x)', 'x');
```

Communication with Excel must have been established previously with a ddei nit command.

#### See Also

ddeexec	Send string for execution
ddei ni t	Initiate DDE conversation
ddepoke	Send data to application
ddereq	Request data from application
ddeterm	Terminate DDE conversation
ddeunadv	Release advisory link

**Purpose** Send string for execution

**Syntax** rc = ddeexec(channel, 'command')

rc = ddeexec(channel, 'command', 'item')

rc = ddeexec(channel, 'command', 'item', timeout)

**Description** ddeexec sends a string for execution to another application via an established

DDE conversation. Specify the string as the command argument.

If you omit optional arguments that are not at the end of the argument list, you

must substitute the empty matrix for the missing argument(s).

Arguments rc Return code: 0 indicates failure, 1 indicates success.

channel Conversation channel from ddei ni t.

*command* String specifying the command to be executed.

*i tem* String specifying the DDE item name for execution. This

(optional) argument is not used for many applications. If your application

requires this argument, it provides additional information for

command. Consult your server documentation for more

information.

ti meout Scalar specifying the time-out limit for this operation. ti meout

(optional) is specified in milliseconds. (1000 milliseconds = 1 second). The

default value of timeout is three seconds.

**Examples** Given the channel assigned to a conversation, send a command to Excel:

rc = ddeexec(channel, '[formul a. goto("r1c1")]')

Communication with Excel must have been established previously with a

ddei ni t command.

**See Also** ddeadv Set up advisory link

ddei ni tInitiate DDE conversationddepokeSend data to applicationddereqRequest data from applicationddetermTerminate DDE conversation

ddeunadv Release advisory link

**Purpose** Initiate DDE conversation

**Syntax** channel = ddeinit('service', 'topic')

**Description** channel = ddei ni t (' servi ce', ' topi c') returns a channel handle assigned

to the conversation, which is used with other MATLAB DDE functions.

'service' is a string specifying the service or application name for the conver-

sation. ' $topi\ c$ ' is a string specifying the topic for the conversation.

**Examples** To initiate a conversation with Excel for the spreadsheet 'stocks. xls':

channel = ddei ni t('excel', 'stocks. xl s')

channel =

0.00

See Also ddeadv Set up advisory link

ddeexecSend string for executionddepokeSend data to application

ddereqRequest data from applicationddetermTerminate DDE conversation

ddeunadv Release advisory link

# ddepoke

#### **Purpose**

Send data to application

#### Syntax

```
rc = ddepoke(channel, 'item', data)
```

rc = ddepoke(channel, 'item', data, format)

rc = ddepoke(channel, 'item', data, format, timeout)

# Description

ddepoke sends data to an application via an established DDE conversation. ddepoke formats the data matrix as follows before sending it to the server application:

- String matrices are converted, element by element, to characters and the resulting character buffer is sent.
- Numeric matrices are sent as tab-delimited columns and carriage-return, line-feed delimited rows of numbers. Only the real part of nonsparse matrices are sent.

If you omit optional arguments that are not at the end of the argument list, you must substitute the empty matrix for the missing argument(s).

# **Arguments**

rc	Return code: 0 indicates failure, 1 indicates success.
----	--

channel Conversation channel from ddei ni t.

*i tem* String specifying the DDE item for the data sent. Item is the

server data entity that is to contain the data sent in the data

argument.

data Matrix containing the data to send.

format Scalar specifying the format of the data requested. The value (optional) indicates the Windows clipboard format to use for the data

transfer. The only format currently supported is cf\_text,

which corresponds to a value of 1.

ti meout Scalar specifying the time-out limit for this operation. ti meout (optional) is specified in milliseconds. (1000 milliseconds = 1 second). The

default value of timeout is three seconds.

**Examples** Assume that a conversation channel with Excel has previously been estab-

lished with ddei ni  $\ensuremath{\text{t.}}$  To send a 5-by-5 identity matrix to Excel, placing the data

in Row 1, Column 1 through Row 5, Column 5:

rc = ddepoke(channel, 'r1c1:r5c5', eye(5));

See Also ddeadv Set up advisory link

ddeexecSend string for executionddei ni tInitiate DDE conversationddereqRequest data from applicationddetermTerminate DDE conversation

ddeunadv Release advisory link

# ddereq

**Purpose** 

Request data from application

**Syntax** 

data = ddereq(channel, 'item')

data = ddereg(channel, 'item', format)

data = ddereq(channel, 'item', format, timeout)

**Description** 

ddereq requests data from a server application via an established DDE conversation. ddereq returns a matrix containing the requested data or an empty matrix if the function is unsuccessful.

If you omit optional arguments that are not at the end of the argument list, you must substitute the empty matrix for the missing argument(s).

**Arguments** 

data Matrix containing requested data, empty if function fails.

channel Conversation channel from ddei ni t.

*i tem* String specifying the server application's DDE item name for

the data requested.

format (optional)

Two-element array specifying the format of the data requested. The first element specifies the Windows clipboard format to

use. The only currently supported format is cf\_text, which corresponds to a value of 1. The second element specifies the type of the resultant matrix. Valid types are numeric (the default, which corresponds to 0) and string (which

corresponds to a value of 1). The default format array is [1 0].

timeout (optional)

Scalar specifying the time-out limit for this operation. timeout is specified in milliseconds. (1000 milliseconds = 1 second). The

default value of timeout is three seconds.

**Examples** 

Assume that we have an Excel spreadsheet stocks. xls. This spreadsheet contains the prices of three stocks in row 3 (columns 1 through 3) and the number of shares of these stocks in rows 6 through 8 (column 2). Initiate conversation with Excel with the command:

```
channel = ddeinit('excel', 'stocks. xls')
```

DDE functions require the rxcy reference style for Excel worksheets. In Excel terminology the prices are in r3c1: r3c3 and the shares in r6c2: r8c2.

To request the prices from Excel:

To request the number of shares of each stock:

See Also

ddeadvSet up advisory linkddeexecSend string for executionddei ni tInitiate DDE conversationddepokeSend data to applicationddetermTerminate DDE conversationddeunadvRelease advisory link

# ddeterm

**Purpose** Terminate DDE conversation

**Syntax** rc = ddeterm(channel)

**Description** rc = ddeterm(channel) accepts a channel handle returned by a previous call

to ddei nit that established the DDE conversation. ddeterm terminates this conversation. rc is a return code where 0 indicates failure and 1 indicates

success.

**Examples** To close a conversation channel previously opened with ddei nit:

rc = ddeterm(channel)

rc =

1.00

See Also ddeadv Set up advisory link

ddeexecSend string for executionddei ni tInitiate DDE conversationddepokeSend data to applicationddereqRequest data from application

ddeunadv Release advisory link

#### Purpose Release advisory link

#### **Syntax** rc = ddeunadv(channel, 'item')

rc = ddeunadv(channel, 'item', format)

rc = ddeunadv(channel, 'item', format, timeout)

## Description

ddeunadv releases the advisory link between MATLAB and the server application established by an earlier ddeadv call. The channel, *item*, and format must be the same as those specified in the call to ddeadv that initiated the link. If you include the timeout argument but accept the default format, you must specify format as an empty matrix.

#### **Arguments**

channel Conversation channel from ddei ni t.

*item* String specifying the DDE item name for the advisory link.

Changing the data identified by i tem at the server triggers the

advisory link.

format Two-element array. This must be the same as the format

(optional) argument for the corresponding ddeadv call.

ti meout Scalar specifying the time-out limit for this operation. ti meout

(optional) is specified in milliseconds. (1000 milliseconds = 1 second). The

default value of timeout is three seconds.

#### Example

To release an advisory link established previously with ddeadv:

```
rc = ddeadv(channel, 'r1c1:r5c5')
rc =
```

1.00

#### See Also

ddeadv	Set up advisory link
ddeexec	Send string for execution
ddei ni t	Initiate DDE conversation
ddepoke	Send data to application
ddereq	Request data from application
ddeterm	Release advisory link

Deal inputs to outputs

# **Syntax**

$$[Y1, Y2, Y3, ...] = deal(X)$$

$$[Y1, Y2, Y3, ...] = deal(X1, X2, X3, ...)$$

# Description

[Y1, Y2, Y3, ...] = deal(X) copies the single input to all the requested outputs. It is the same as Y1 = X, Y2 = X, Y3 = X, ...

$$[Y1, Y2, Y3, ...] = deal(X1, X2, X3, ...)$$
 is the same as  $Y1 = X1; Y2 = X2; Y3 = X3; ...$ 

# Remarks

deal is most useful when used with cell arrays and structures via comma separated list expansion. Here are some useful constructions:

[S. field] = deal(X) sets all the fields with the name field in the structure array S to the value X. If S doesn't exist, use [S(1:m). field] = deal(X).

 $[X{:}] = deal (A. field)$  copies the values of the field with name field to the cell array X. If X doesn't exist, use  $[X{1:m}] = deal (A. field)$ .

 $[Y1, Y2, Y3, ...] = deal(X{:})$  copies the contents of the cell array X to the separate variables Y1, Y2, Y3, ...

 $[Y1, Y2, Y3, \dots] = deal(S. field)$  copies the contents of the fields with the name field to separate variables  $Y1, Y2, Y3, \dots$ 

# **Examples**

Use deal to copy the contents of a 4-element cell array into four separate output variables.

```
C = \{rand(3) \ ones(3, 1) \ eye(3) \ zeros(3, 1)\};
[a, b, c, d] = deal(C{:})
a =
    0.9501
               0.4860
                         0.4565
    0. 2311
               0.8913
                         0.0185
    0.6068
               0.7621
                         0.8214
b =
    1
    1
    1
c =
    1
             0
         0
             0
    0
    0
         0
              1
d =
    0
    0
    0
```

Use  $\mbox{\it deal}\ to\mbox{\it obtain}$  the contents of all the name fields in a structure array:

```
A. name = 'Pat'; A. number = 176554;
A(2). name = 'Tony'; A(2). number = 901325;
[name1, name2] = deal(A(:). name)

name1 =
Pat
name2 =
Tony
```

Strip trailing blanks from the end of a string

# **Syntax**

```
str = deblank(str)

c = deblank(c)
```

# **Description**

The debl ank function is useful for cleaning up the rows of a character array.

str = deblank(str) removes the trailing blanks from the end of a character string str.

 $c = debl\,ank(c)$ , when c is a cell array of strings, applies  $debl\,ank$  to each element of c.

# **Examples**

```
A{1, 1} = 'MATLAB ';
A{1, 2} = 'SI MULI NK ';
A{2, 1} = 'Tool boxes ';
A{2, 2} = 'The MathWorks ';
A =

'MATLAB ' 'SI MULI NK '
'Tool boxes ' 'The MathWorks '

debl ank(A)
ans =

'MATLAB' 'SI MULI NK '
'Tool boxes' 'The MathWorks'
```

# dec2base

**Purpose** Decimal number to base conversion

**Syntax** str = dec2base(d, base)

str = dec2base(d, base, n)

**Description** str = dec2base(d, base) converts the nonnegative integer d to the specified

base.d must be a nonnegative integer smaller than 2^52, and base must be an

integer between 2 and 36. The returned argument str is a string.

str = dec2base(d, base, n) produces a representation with at least n digits.

**Examples** The expression dec2base(23, 2) converts 23<sub>10</sub> to base 2, returning the string

' 10111' .

See Also base2dec

**Purpose** Decimal to binary number conversion

**Syntax** str = dec2bin(d)

str = dec2bin(d, n)

**Description** str = dec2bin(d) returns the binary representation of d as a string. d must

be a nonnegative integer smaller than  $2^{52}$ .

str = dec2bin(d, n) produces a binary representation with at least n bits.

**Examples** dec2bi n(23) returns ' 10111'.

See Also bi n2dec 2-Binary to decimal number conversion

dec2hex 2-Decimal to hexadecimal number conversion

# dec2hex

**Purpose** Decimal to hexadecimal number conversion

**Syntax** str = dec2hex(d)

str = dec2hex(d, n)

**Description** str = dec2hex(d) converts the decimal integer d to its hexadecimal represen-

tation stored in a MATLAB string. d must be a nonnegative integer smaller than  $2^{52}$  .

str = dec2hex(d, n) produces a hexadecimal representation with at least n

digits.

**Examples** dec2hex(1023) is the string '3ff'.

See Also dec2bi n 2-Decimal to binary number conversion

> format 2-Control the output display format

hex2dec 2-IEEE hexadecimal to decimal number conversion

hex2num 2-Hexadecimal to double number conversion

Deconvolution and polynomial division

#### **Syntax**

$$[q, r] = deconv(v, u)$$

# Description

[q, r] = deconv(v, u) deconvolves vector u out of vector v, using long division. The quotient is returned in vector q and the remainder in vector r such that v = conv(u, q) + r.

If u and v are vectors of polynomial coefficients, convolving them is equivalent to multiplying the two polynomials, and deconvolution is polynomial division. The result of dividing v by u is quotient q and remainder r.

# **Examples**

If

$$u = [1 \ 2 \ 3 \ 4]$$
  
 $v = [10 \ 20 \ 30]$ 

the convolution is

Use deconvolution to recover u:

This gives a quotient equal to  $\boldsymbol{v}$  and a zero remainder.

# **Algorithm**

deconv uses the filter primitive.

#### See Also

convmtx, conv2, and filter in the Signal Processing Toolbox, and:

conv 2-Convolution and polynomial multiplication
resi due 2-Convert between partial fraction expansion and polynomial coefficients

Discrete Laplacian

**Syntax** 

L = del 2(U)

L = del 2(U, h)

L = del 2(U, hx, hy)

L = del 2(U, hx, hy, hz, ...)

**Definition** 

If the matrix U is regarded as a function u(x,y) evaluated at the point on a square grid, then  $4*del\ 2(U)$  is a finite difference approximation of Laplace's differential operator applied to u, that is:

$$I = \frac{\nabla^{2} u}{4} = \frac{1}{4} \left( \frac{d^{2} u}{dx^{2}} + \frac{d^{2} u}{dy^{2}} \right)$$

where:

$$l_{ij} = \frac{1}{4}(u_{i+1,j} + u_{i-1,j} + u_{i,j+1} + u_{i,j-1}) - u_{i,j}$$

in the interior. On the edges, the same formula is applied to a cubic extrapolation.

For functions of more variables u(x,y,z,...), del 2(U) is an approximation,

$$I = \frac{\nabla^2 u}{2N} = \frac{1}{2N} \left( \frac{d^2 u}{dx^2} + \frac{d^2 u}{dy^2} + \frac{d^2 u}{dz^2} + \dots \right)$$

where N is the number of variables in u.

Description

L = del 2(U) where U is a rectangular array is a discrete approximation of

$$I = \frac{\nabla^2 u}{4} = \frac{1}{4} \left( \frac{d^2 u}{dx^2} + \frac{d^2 u}{dy^2} \right)$$

The matrix L is the same size as U with each element equal to the difference between an element of U and the average of its four neighbors.

 $L = del \, 2(U)$  when U is an multidimensional array, returns an approximation of

$$\frac{\nabla^2 u}{2N}$$

where N is ndi ms(u).

L = del 2(U, h) where H is a scalar uses H as the spacing between points in each direction (h=1 by default).

 $L = del\ 2(U, hx, hy)$  when U is a rectangular array, uses the spacing specified by hx and hy. If hx is a scalar, it gives the spacing between points in the x-direction. If hx is a vector, it must be of length  $si\ ze(u, 2)$  and specifies the x-coordinates of the points. Similarly, if hy is a scalar, it gives the spacing between points in the y-direction. If hy is a vector, it must be of length  $si\ ze(u, 1)$  and specifies the y-coordinates of the points.

L = del 2(U, hx, hy, hz, ...) where U is multidimensional uses the spacing given by hx, hy, hz, ...

# **Examples**

The function

$$u(x,y) = x^2 + y^2$$

has

$$\nabla^2 u = 4$$

For this function, 4\*del 2(U) is also 4.

V V	= 4*del2	2(U)							
	4	4	4	4	4	4	4	4	4
	4	4	4	4	4	4	4	4	4
	4	4	4	4	4	4	4	4	4
	4	4	4	4	4	4	4	4	4
	4	4	4	4	4	4	4	4	4
	4	4	4	4	4	4	4	4	4
	4	4	4	4	4	4	4	4	4

See Also

diff gradi ent 2-Differences and approximate derivatives 2-Numerical gradient

Delaunay triangulation

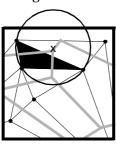
Syntax

TRI = del aunay(x, y)

TRI = del aunay(x, y, 'sorted')

**Definition** 

Given a set of data points, the *Delaunay triangulation* is a set of lines connecting each point to its natural neighbors. The Delaunay triangulation is related to the Voronoi diagram— the circle circumscribed about a Delaunay triangle has its center at the vertex of a Voronoi polygon.



Delaunay triangle

Voronoi polygon

Description

 $TRI = del\ aunay(x, y)$  returns a set of triangles such that no data points are contained in any triangle's circumscribed circle. Each row of the m-by-3 matrix TRI defines one such triangle and contains indices into the vectors x and y.

 $TRI = del \ aunay(x, y, 'sorted')$  assumes that the points x and y are sorted first by y and then by x and that duplicate points have already been eliminated.

Remarks

The Delaunay triangulation is used with: gri ddata (to interpolate scattered data), convhull, voronoi (to compute the voronoi diagram), and is useful by itself to create a triangular grid for scattered data points.

The functions dsearch and tsearch search the triangulation to find nearest neighbor points or enclosing triangles, respectively.

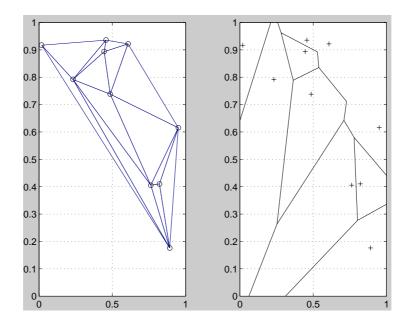
# **Examples**

This code plots the Delaunay triangulation for 10 randomly generated points.

```
rand('state', 0);
x = rand(1, 10);
y = rand(1, 10);
TRI = del aunay(x, y);
subpl ot(1, 2, 1),...
tri mesh(TRI, x, y, zeros(size(x))); view(2),...
axis([0 1 0 1]); hold on;
pl ot(x, y, 'o');
set(gca, 'box', 'on');
```

Compare the Voronoi diagram of the same points:

```
[vx, vy] = voronoi (x, y, TRI);
subpl ot (1, 2, 2), ...
pl ot (x, y, 'r+', vx, vy, 'b-'), ...
axi s([0 1 0 1])
```



See Also

convhul l

2-Convex hull

# delaunay

dsearch 2-Search for nearest point

gri ddata 2-Data gridding

tsearch 2-Search for enclosing Delaunay triangle

voronoi 2-Voronoi diagram

# delete

**Purpose** Delete files and graphics objects

Syntax delete filename

del ete(h)

**Description** del ete *filename* deletes the named file. Wildcards may be used.

 $\mbox{\tt del}\,\mbox{\tt ete}(h)$   $\mbox{\tt deletes}$  the graphics object with handle h. The function deletes the

object without requesting verification even if the object is a window.

Use the functional form of delete, such as delete('filename'), when the file-

name is stored in a string.

**See Also** ! Operating system command

dir 2-Directory listing

type 2-List file

Matrix determinant

**Syntax** 

d = det(X)

Description

d = det(X) returns the determinant of the square matrix X. If X contains only integer entries, the result d is also an integer.

Remarks

Using det(X) == 0 as a test for matrix singularity is appropriate only for matrices of modest order with small integer entries. Testing singularity using  $abs(det(X)) <= tol \, erance \, is \, not \, recommended \, as \, it \, is \, difficult \, to \, choose \, the \, correct \, tolerance. The function <math>cond(X)$  can check for singular and nearly singular matrices.

**Algorithm** 

The determinant is computed from the triangular factors obtained by Gaussian elimination  $% \left( 1\right) =\left( 1\right) +\left( 1\right) +\left$ 

**Examples** 

The statement  $A = [1 \ 2 \ 3; \ 4 \ 5 \ 6; \ 7 \ 8 \ 9]$ 

produces

This happens to be a singular matrix, so  $d = \det(A)$  produces d = 0. Changing A(3, 3) with A(3, 3) = 0 turns A into a nonsingular matrix. Now  $d = \det(A)$  produces d = 27.

See Also

\ Matrix left division (backslash)
\/ Matrix right division (slash)

cond 2-Condition number with respect to inversion condest 2-1-norm matrix condition number estimate

i nv 2-Matrix inverse

lu 2-LU matrix factorization rref 2-Reduced row echelon form

# diag

#### **Purpose**

Diagonal matrices and diagonals of a matrix

**Syntax** 

X = diag(v, k)

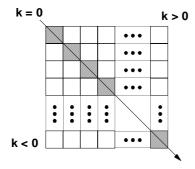
X = diag(v)

v = diag(X, k)

v = diag(X)

# Description

 $X=di\,ag(v,k)$  when v is a vector of n components, returns a square matrix X of order n+abs(k), with the elements of v on the kth diagonal. k=0 represents the main diagonal, k>0 above the main diagonal, and k<0 below the main diagonal.



X = di ag(v) puts v on the main diagonal, same as above with k = 0.

 $v = di \, ag(X, k)$  for matrix X, returns a column vector v formed from the elements of the kth diagonal of X.

 $v = di \, ag(X)$  returns the main diagonal of X, same as above with k = 0.

# **Examples**

diag(diag(X)) is a diagonal matrix.

sum(diag(X)) is the trace of X.

The statement

diag(-m: m) + diag(ones(2\*m, 1), 1) + diag(ones(2\*m, 1), -1)

produces a tridiagonal matrix of order 2\*m+1.

See Also

spdiags, tril, triu

**Purpose** Save session in a disk file

Syntax di ary

diary filename diary off diary on

**Description** The di ary command creates a log of keyboard input and system responses. The

output of di ary is an ASCII file, suitable for printing or for inclusion in reports

and other documents.

di ary, by itself, toggles di ary mode on and off.

di ary filename writes a copy of all subsequent keyboard input and most of the resulting output (but not graphs) to the named file. If the file already exists,

output is appended to the end of the file.

di ary off suspends the diary.

di ary on resumes diary mode using the current filename, or the default file-

name di ary if none has yet been specified.

**Remarks** The function form of the syntax, di ary('filename'), is also permitted.

**Limitations** You cannot put a diary into the files named of f and on.

Differences and approximate derivatives

**Syntax** 

Y = diff(X)Y = diff(X, n)

Y = diff(X, n, dim)

**Description** 

Y = diff(X) calculates differences between adjacent elements of X.

If X is a vector, then diff(X) returns a vector, one element shorter than X, of differences between adjacent elements:

$$[X(2)-X(1) X(3)-X(2) ... X(n)-X(n-1)]$$

If X is a matrix, then diff(X) returns a matrix of column differences:

$$[X(2: m, :) -X(1: m-1, :)]$$

In general,  $\operatorname{diff}(X)$  returns the differences calculated along the first non-singleton (si  $\operatorname{ze}(X,\operatorname{dim})>1$ ) dimension of X.

Y = diff(X, n) applies diff recursively n times, resulting in the nth difference. Thus, diff(X, 2) is the same as diff(diff(X)).

Y = diff(X, n, dim) is the nth difference function calculated along the dimension specified by scalar dim. If order n equals or exceeds the length of dimension dim, diff returns an empty array.

**Remarks** 

Since each iteration of diff reduces the length of X along dimension di m, it is possible to specify an order n sufficiently high to reduce di m to a singleton (si ze(X, di m) = 1) dimension. When this happens, diff continues calculating along the next nonsingleton dimension.

# **Examples**

The quantity diff(y). /diff(x) is an approximate derivative.

$$x = [1 \ 2 \ 3 \ 4 \ 5];$$
  
 $y = di ff(x)$   
 $y =$ 

$$1 \quad 1 \quad 1 \quad 1$$

$$z = di ff(x, 2)$$

$$z =$$

$$0 \quad 0 \quad 0$$

Given,

$$A = rand(1, 3, 2, 4);$$

diff(A) is the first-order difference along dimension 2. diff(A, 3, 4) is the third-order difference along dimension 4.

#### See Also

gradi ent Approximate gradient.

int Integrate (see Symbolic Toolbox).
prod 2-Product of array elements
sum 2-Sum of array elements

```
Purpose
                    Directory listing
Syntax
                    di r
                    dir dirname
                    names = dir
                    names = dir('dirname')
Description
                    dir, by itself, lists the files in the current directory.
                    dir dirname lists the files in the specified directory. Use pathnames,
                    wildcards, and any options available in your operating system.
                    names = dir('dirname') or names = dir returns the results in an m-by-1
                    structure with the fields:
                                     Filename
                    name
                                     Modification date
                     date
                     bytes
                                     Number of bytes allocated to the file
                    i sdi r
                                     1 if name is a directory; 0 if not
Examples
                       cd /Matlab/Toolbox/Local; dir
                       Contents. m matlabrc. m siteid. m userpath. m
                       names = dir
                       names =
                       4x1 struct array with fields:
                            name
                            date
                            bytes
                            i sdi r
See Also
                    !, cd, delete, type, what
```

**Purpose** Display text or array

**Description**  $\operatorname{disp}(X)$  displays an array, without printing the array name. If X contains a

text string, the string is displayed.

Another way to display an array on the screen is to type its name, but this

prints a leading "X =, " which is not always desirable.

**Examples** One use of di sp in an M-file is to display a matrix with column labels:

disp(' Corn Oats Hay') disp(rand(5,3))

which results in

Corn	0ats	Hay
0. 2113	0.8474	0. 2749
0. 0820	0. 4524	0. 8807
0. 7599	0.8075	0. 6538
0.0087	0. 4832	0. 4899
0.8096	0.6135	0. 7741

See Also format 2-Control the output display format

i nt2str 2-Integer to string conversion num2str 2-Number to string conversion rats 2-Rational fraction approximation sprintf 2-Write formatted data to a string

Read an ASCII delimited file into a matrix

**Syntax** 

M = dl mread(filename, delimiter)

M = dl mread(filename, delimiter, r, c)

M = dl mread(filename, delimiter, r, c, range)

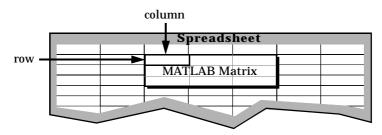
**Description** 

M = dl mread(filename, delimiter) reads data from the ASCII delimited format filename, using the delimiter delimiter. Use '\t' to specify a tab.

 $M = dl \, mread(fi \, l \, ename, \, del \, i \, mi \, ter, \, r, \, c)$  reads data from the ASCII delimited format  $fi \, l \, ename$ , using the delimiter  $del \, i \, mi \, ter$ , starting at file offset r and c. r and c are zero based so that r=0, c=0 specifies the first value in the file.

M = dl mread(filename, delimiter, r, c, range) imports an indexed or named range of ASCII-delimited data. To use the cell range, specify range by:

range = [UpperLeftRow UpperLeftColumn LowerRightRow
LowerRightColumn]



**Arguments** 

delimiter

The character separating individual matrix elements in the ASCII- format spreadsheet file. A comma (,) is the default delimiter.

r, c

The spreadsheet cell from which the upper-left-most matrix element is taken.

range A vector specifying a range of spreadsheet cells.

See Also

dl mwri te 2-Write a matrix to an ASCII delimited file wk1read 2-Read a Lotus123 WK1 spreadsheet file into a matrix

wk1write

2-Write a matrix to a Lotus123 WK1 spreadsheet file

**Purpose** Write a matrix to an ASCII delimited file

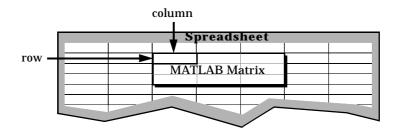
Syntax dl mwrite(filename, A, delimiter)

dl mwrite(filename, A, delimiter, r, c)

**Description** The dl mwrite command converts a MATLAB matrix into an ASCII-format file readable by spreadsheet programs.

dl mwrite(filename, A, delimiter) writes matrix A into the upper left-most cell of the ASCII-format spreadsheet file filename, and uses the delimiter to separate matrix elements. Specify '\t' to produce tab-delimited files. Any elements whose value is 0 will be omitted. For example, the array [1 0 2] will appear in a file as '1, 2' when the delimiter is a comma.

dl mwrite(filename, A, delimiter, r, c) writes A into filename, starting at spreadsheet cell r and c, with delimiter used to separate matrix elements.



**Arguments** delimiter The character separating individual matrix elements in the

ASCII- format spreadsheet file. A comma (,) is the default

delimiter.

r, c The spreadsheet cell into which the upper-left-most matrix

element is written.

See Also dl mread 2-Read an ASCII delimited file into a matrix

wk1read 2-Read a Lotus123 WK1 spreadsheet file into a matrix

wk1write 2-Write a matrix to a Lotus123 WK1 spreadsheet file

# dmperm

### **Purpose**

**Dulmage-Mendelsohn decomposition** 

### Syntax

```
p = dmperm(A)
[p, q, r] = dmperm(A)
[p, q, r, s] = dmperm(A)
```

# **Description**

If A is a reducible matrix, the linear system Ax = b can be solved by permuting A to a block upper triangular form, with irreducible diagonal blocks, and then performing block backsubstitution. Only the diagonal blocks of the permuted matrix need to be factored, saving fill and arithmetic in the blocks above the diagonal.

p=dmperm(A) returns a row permutation p so that if A has full column rank, A(p,:) is square with nonzero diagonal. This is also called a *maximum matching*.

[p,q,r] = dmperm(A) where A is a square matrix, finds a row permutation p and a column permutation q so that A(p,q) is in block upper triangular form. The third output argument r is an integer vector describing the boundaries of the blocks: The kth block of A(p,q) has indices r(k):r(k+1)-1.

[p, q, r, s] = dmperm(A), where A is not square, finds permutations p and q and index vectors r and s so that A(p, q) is block upper triangular. The blocks have indices (r(i): r(i+1)-1, s(i): s(i+1)-1).

In graph theoretic terms, the diagonal blocks correspond to strong Hall components of the adjacency graph of A.

**Purpose** Load hypertext documentation

Syntax doc

doc command

**Description** doc, by itself, loads hypertext-based reference documentation. You'll be

presented with an index of MATLAB's main categories of functions.

doc command loads documentation about a specific command or function.

**See Also** hel p Online help for MATLAB functions and M-files

type 2-List file

# double

**Purpose** Convert to double precision

Syntax doubl e(X)

**Description** doubl e(x) returns the double precision value for X. If X is already a double

precision array, double has no effect.

**Remarks** double is called for the expressions in for, if, and while loops if the expression

isn't already double precision. doubl e should be overloaded for any object when

it makes sense to convert it to a double precision value.

**Purpose** Search for nearest point

**Syntax** K = dsearch(x, y, TRI, xi, yi)

K = dsearch(x, y, TRI, xi, yi, S)

**Description** K = dsearch(x, y, TRI, xi, yi) returns the index of the nearest (x,y) point to

the point (xi,yi). dsearch requires a triangulation TRI of the points x,y

obtained from del aunay.

K = dsearch(x, y, TRI, xi, yi, S) uses the sparse matrix S instead of

computing it each time:

 $S = sparse(TRI(:, [1 \ 1 \ 2 \ 2 \ 3 \ 3]), TRI(:, [2 \ 3 \ 1 \ 3 \ 1 \ 2]), 1, nxy, nxy)$ 

where nxy = prod(size(x)).

See Also del aunay Delaunay triangulation

tsearch 2-Search for enclosing Delaunay triangle

voronoi 2-Voronoi diagram

Echo M-files during execution

### Syntax

echo on echo off echo

echo fcnname on echo fcnname off echo fcnname echo on all echo off all

### Description

The echo command controls the echoing of M-files during execution. Normally, the commands in M-files do not display on the screen during execution. Command echoing is useful for debugging or for demonstrations, allowing the commands to be viewed as they execute.

The echo command behaves in a slightly different manner for script files and function files. For script files, the use of echo is simple; echoing can be either on or of f, in which case any script used is affected:

echo on Turns on the echoing of commands in all script files.

echo off Turns off the echoing of commands in all script files.

echo Toggles the echo state.

With function files, the use of echo is more complicated. If echo is enabled on a function file, the file is interpreted, rather than compiled. Each input line is then displayed as it is executed. Since this results in inefficient execution, use echo only for debugging.

echo fcnname on Turns on echoing of the named function file.

echo fcnname off Turns off echoing of the named function file.

echo fcnname Toggles the echo state of the named function file.

echo on all Set echoing on for all function files.
echo off all Set echoing off for all function files.

#### See Also

function [ ]

Purpose Edit an M-file

Syntax edi t

edit fun

edit *file.ext* edit *class/fun* edit private/*fun* 

edit class/private/fun

**Description** edit opens a new editor window.

edit fun opens the M-file fun. m in a text editor.

edit file. ext opens the specified text file.

edit class/fun, edit private/fun, or edit class/private/fun can be used to edit a method, private function, or private method (for the class named

cl ass.)

Eigenvalues and eigenvectors

# **Syntax**

```
d = eig(A)
[V, D] = eig(A)
[V, D] = eig(A, 'nobal ance')
d = eig(A, B)
[V, D] = eig(A, B)
```

# Description

d = eig(A) returns a vector of the eigenvalues of matrix A.

[V, D] = eig(A) produces matrices of eigenvalues (D) and eigenvectors (V) of matrix A, so that A\*V = V\*D. Matrix D is the *canonical form* of A—a diagonal matrix with A's eigenvalues on the main diagonal. Matrix V is the *modal matrix*—its columns are the eigenvectors of A.

The eigenvectors are scaled so that the norm of each is 1.0. Use [W, D] = eig(A'); W = W' to compute the *left eigenvectors*, which satisfy W\*A = D\*W.

[V,D] = eig(A, 'nobal ance') finds eigenvalues and eigenvectors without a preliminary balancing step. Ordinarily, balancing improves the conditioning of the input matrix, enabling more accurate computation of the eigenvectors and eigenvalues. However, if a matrix contains small elements that are really due to roundoff error, balancing may scale them up to make them as significant as the other elements of the original matrix, leading to incorrect eigenvectors. Use the nobal ance option in this event. See the bal ance function for more details.

d = ei g(A, B) returns a vector containing the generalized eigenvalues, if A and B are square matrices.

[V, D] = eig(A, B) produces a diagonal matrix D of generalized eigenvalues and a full matrix V whose columns are the corresponding eigenvectors so that A\*V = B\*V\*D. The eigenvectors are scaled so that the norm of each is 1.0.

#### Remarks

The eigenvalue problem is to determine the nontrivial solutions of the equation:

$$Ax = \lambda x$$

where A is an n-by-n matrix, x is a length n column vector, and  $\lambda$  is a scalar. The n values of  $\lambda$  that satisfy the equation are the *eigenvalues*, and the corresponding values of x are the *right eigenvectors*. In MATLAB, the function eig solves for the eigenvalues  $\lambda$ , and optionally the eigenvectors x.

The *generalized* eigenvalue problem is to determine the nontrivial solutions of the equation

$$Ax = \lambda Bx$$

where both A and B are n-by-n matrices and  $\lambda$  is a scalar. The values of  $\lambda$  that satisfy the equation are the *generalized eigenvalues* and the corresponding values of x are the *generalized right eigenvectors*.

If B is nonsingular, the problem could be solved by reducing it to a standard eigenvalue problem

$$B^{-1}Ax = \lambda x$$

Because B can be singular, an alternative algorithm, called the QZ method, is necessary.

When a matrix has no repeated eigenvalues, the eigenvectors are always independent and the eigenvector matrix V diagonalizes the original matrix A if applied as a similarity transformation. However, if a matrix has repeated eigenvalues, it is not similar to a diagonal matrix unless it has a full (independent) set of eigenvectors. If the eigenvectors are not independent then the original matrix is said to be defective. Even if a matrix is defective, the solution from eig satisfies A\*X = X\*D.

# **Examples**

The matrix

$$B = [3 -2 -. 9 \ 2 \cdot eps; -2 \ 4 \ -1 \ -eps; -eps/4 \ eps/2 \ -1 \ 0; -. 5 \ -. 5 \ .1 \ 1];$$

has elements on the order of roundoff error. It is an example for which the nobal ance option is necessary to compute the eigenvectors correctly. Try the statements

```
[VB, DB] = eig(B)

B*VB - VB*DB

[VN, DN] = eig(B, 'nobal ance')

B*VN - VN*DN
```

## **Algorithm**

For real matrices, ei g(X) uses the EISPACK routines BALANC, BALBAK, ORTHES, ORTRAN, and HQR2. BALANC and BALBAK balance the input matrix. ORTHES converts a real general matrix to Hessenberg form using orthogonal similarity transformations. ORTRAN accumulates the transformations used by ORTHES. HQR2 finds the eigenvalues and eigenvectors of a real upper Hessenberg matrix by the QR method. The EISPACK subroutine HQR2 is modified to make computation of eigenvectors optional.

When eig is used with two input arguments, the EISPACK routines QZHES, QZIT, QZVAL, and QZVEC solve for the generalized eigenvalues via the QZ algorithm. Modifications handle the complex case.

When  $\operatorname{ei} g$  is used with one complex argument, the solution is computed using the QZ algorithm as  $\operatorname{ei} g(X, \operatorname{eye}(X))$ . Modifications to the QZ routines handle the special case B = I.

For detailed descriptions of these algorithms, see the *EISPACK Guide*.

# **Diagnostics**

If the limit of 30n iterations is exhausted while seeking an eigenvalue:

Solution will not converge.

#### See Also

bal ance Improve accuracy of computed eigenvalues condeig Condition number with respect to eigenvalues

hess Hessenberg form of a matrix

qz QZ factorization for generalized eigenvalues

schur Schur decomposition

### References

[1] Smith, B. T., J. M. Boyle, J. J. Dongarra, B. S. Garbow, Y. Ikebe, V. C. Klema, and C. B. Moler, *Matrix Eigensystem Routines – EISPACK Guide*, Lecture Notes in Computer Science, Vol. 6, second edition, Springer-Verlag, 1976.

[2] Garbow, B. S., J. M. Boyle, J. J. Dongarra, and C. B. Moler, *Matrix Eigensystem Routines – EISPACK Guide Extension*, Lecture Notes in Computer Science, Vol. 51, Springer-Verlag, 1977.

[3] Moler, C. B. and G.W. Stewart, "An Algorithm for Generalized Matrix Eigenvalue Problems", *SIAM J. Numer. Anal.*, Vol. 10, No. 2, April 1973.

Find a few eigenvalues and eigenvectors

### **Syntax**

```
d = eigs(A)
d = eigs('Afun', n)
d = eigs(A, B, k, sigma, options)
d = eigs('Afun', n, B, k, sigma, options)
[V, D] = eigs(A, ...)
[V, D] = eigs('Afun', n, ...)
[V, D, flag] = eigs(A, ...)
[V, D, flag] = eigs('Afun', n, ...)
```

### Description

ei gs solves the eigenvalue problem  $A^*v = 1$  ambda $^*v$  or the generalized eigenvalue problem  $A^*v = 1$  ambda $^*B^*v$ . Only a few selected eigenvalues, or eigenvalues and eigenvectors, are computed, in contrast to eigenvalues and eigenvectors.

ei gs(A) or ei gs('Afun', n) solves the eigenvalue problem where the first input argument is either a square matrix (which can be full or sparse, symmetric or nonsymmetric, real or complex), or a string containing the name of an M-file which applies a linear operator to the columns of a given matrix. In the latter case, the second input argument must be n, the order of the problem. For example, ei gs('fft', ...) is much faster than ei gs(F, ...), where F is the explicit FFT matrix.

With one output argument, d is a vector containing k eigenvalues. With two output arguments, V is a matrix with k columns and D is a k-by-k diagonal matrix so that A\*V = V\*D or A\*V = B\*V\*D. With three output arguments, flag indicates whether or not the eigenvalues were computed to the desired tolerance. flag = 0 indicates convergence; flag = 1 indicates no convergence.

The remaining input arguments are optional and can be given in practically any order:

Argument	Value		
В	A matrix the same size as A. If B is not specified, B = eye(size(A)) is used.		
k	An integer, the number of eigenvalues desired. If k is not specified, $k = mi \ n(n, 6)$ eigenvalues are computed.		
si gma	A scalar shift or a two letter string. If si gma is not specified, the k eigenvalues largest in magnitude are computed. If si gma is 0, the k eigenvalues smallest in magnitude are computed. If si gma is a real or complex scalar, the <i>shift</i> , the k eigenvalues nearest si gma, are computed. If si gma is one of the following strings, it specifies the desired eigenvalues:		
	'lm' Largest Magnitude (the default)		
	<ul> <li>'sm' Smallest Magnitude (same as sigma = 0)</li> <li>'lr' Largest Real part</li> <li>'sr' Smallest Real part</li> <li>'be' Both Ends. Computes k/2 eigenvalues from each end of the spectrum (one more from the high end if k is odd.)</li> </ul>		

**Note 1.** If si gma is a scalar with no fractional part, k must be specified first. For example, ei gs(A, 2.0) finds the two largest magnitude eigenvalues, not the six eigenvalues closest to 2.0, as you may have wanted.

Note 2. If si gma is exactly an eigenvalue of A, eigs will encounter problems when it performs divisions of the form 1/(l ambda - si gma), where l ambda is an approximation of an eigenvalue of A. Restart with eigs(A, sigma2), where sigma2 is close to, but not equal to, sigma.

The opti ons structure specifies certain parameters in the algorithm.

Parameter	Description	Default Value
options.tol	Convergence tolerance norm(A*V-V*D) <= tol *norm(A)	1e–10 (symmetric) 1e–6 (nonsymmetric)
options.p	Dimension of the Arnoldi basis	2*k
options. maxi t	Maximum number of iterations	300
opti ons. di sp	Number of eigenvalues displayed at each iteration. Set to 0 for no intermediate output.	20
options.issym	Positive if Afun is symmetric	0
options. cheb	Positive if A is a string, si gma is 'lr','sr', or a shift, and polynomial acceleration should be applied.	0
options. v0	Starting vector for the Arnoldi factorization	rand(n, 1) 5

# **Remarks**

d = eigs(A, k) is not a substitute for

d = eig(full(A))

d = sort(d)

d = d(end-k+1:end)

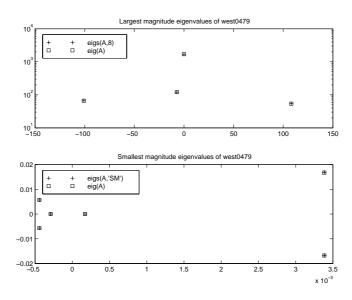
but is most appropriate for large sparse matrices. If the problem fits into memory, it may be quicker to use eig(full(A)).

# **Examples** Example 1:

west0479 is a real 479-by-479 sparse matrix with both real and pairs of complex conjugate eigenvalues. ei g computes all 479 eigenvalues. ei gs easily picks out the smallest and largest magnitude eigenvalues.

```
load west0479
d = eig(full(west0479))
dlm = eigs(west0479, 8)
dsm = eigs(west0479, 'sm')
```

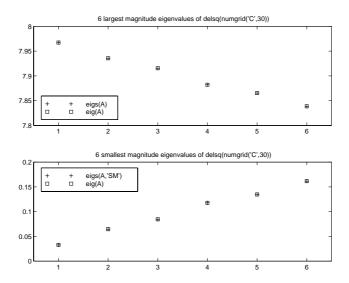
These plots show the eigenvalues of west 0479 as computed by eig and eigs. The first plot shows the four largest magnitude eigenvalues in the top half of the complex plane (but not their complex conjugates in the bottom half). The second subplot shows the six smallest magnitude eigenvalues.



### Example 2:

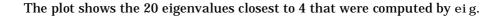
A = del sq(numgri d('C', 30)) is a symmetric positive definite matrix of size 632 with eigenvalues reasonably well-distributed in the interval (0 8), but with 18 eigenvalues repeated at 4. eig computes all 632 eigenvalues. eigs computes the six largest and smallest magnitude eigenvalues of A successfully with:

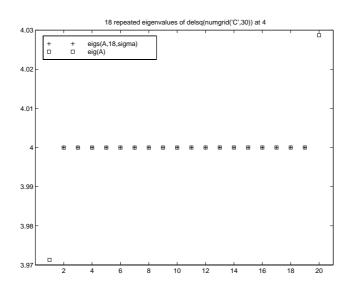
```
d = eig(full(A))
dlm = eigs(A)
dsm = eigs(A, 'sm')
```



However, the repeated eigenvalue at 4 must be handled more carefully. The call ei gs(A, 18, 4. 0) to compute 18 eigenvalues near 4.0 tries to find eigenvalues of A - 4.  $0^*\mathrm{I}$ . This involves divisions of the form  $1/(1\,\mathrm{ambda}-4.0)$ , where l ambda is an estimate of an eigenvalue of A. As l ambda gets closer to 4.0, eigs fails. We must use sigma near but not equal to 4 to find those 18 eigenvalues.

```
sigma = 4 - 1e-6
[V, D] = eigs(A, 18, sigma)
```





### See Also

ei g svds Eigenvalues and eigenvectors A few singular values

#### References

- [1] R. Radke, "A MATLAB Implementation of the Implicitly Restarted Arnoldi Method for Solving Large-Scale Eigenvalue Problems," Dept. of Computational and Applied Math, Rice University, Houston, Texas.
- [2] D. C. Sorensen, "Implicit Application of Polynomial Filters in a k-step Arnoldi Method," *SIAM Journal on Matrix Analysis and Applications*, volume 13, number 1, 1992, pp 357-385.
- [3] R. B. Lehoucq and D. C. Sorensen, "Deflation Techniques within an Implicitly Restarted Iteration," *SIAM Journal on Matrix Analysis and Applications*, volume 17, 1996, pp 789-821.

Jacobi elliptic functions

**Syntax** 

$$[SN, CN, DN] = ellipj(U, M)$$
  
 $[SN, CN, DN] = ellipj(U, M, tol)$ 

**Definition** 

The Jacobi elliptic functions are defined in terms of the integral:

$$u = \int_0^{\phi} \frac{d\theta}{(1 - m\sin^2\theta)^{\frac{1}{2}}}$$

Then

$$sn(u) = \sin\phi, \ cn(u) = \cos\phi, \ dn(u) = (1 - \sin^2\phi)^{\frac{1}{2}}, \ am(u) = \phi$$

Some definitions of the elliptic functions use the modulus k instead of the parameter m. They are related by:

$$k^2 = m = \sin^2 \alpha$$

The Jacobi elliptic functions obey many mathematical identities; for a good sample, see [1].

Description

[SN, CN, DN] = ellipj(U, M) returns the Jacobi elliptic functions SN, CN, and DN, evaluated for corresponding elements of argument U and parameter M. Inputs U and M must be the same size (or either can be scalar).

[SN, CN, DN] = ellipj(U, M, tol) computes the Jacobi elliptic functions to accuracy tol. The default is eps; increase this for a less accurate but more quickly computed answer.

Algorithm

 ${\tt ellipj}$  computes the Jacobi elliptic functions using the method of the arithmetic-geometric mean [1]. It starts with the triplet of numbers:

$$a_0 = 1, b_0 = (1 - m)^{\frac{1}{2}}, c_0 = (m)^{\frac{1}{2}}$$

# ellipj

ellipj computes successive iterates with:

$$a_{i} = \frac{1}{2}(a_{i-1} + b_{i-1})$$

$$b_{i} = (a_{i-1}b_{i-1})^{\frac{1}{2}}$$

$$c_{i} = \frac{1}{2}(a_{i-1} - b_{i-1})$$

Next, it calculates the amplitudes in radians using:

$$\sin(2\phi_{n-1} - \phi_n) = \frac{c_n}{a_n}\sin(\phi_n)$$

being careful to unwrap the phases correctly. The Jacobian elliptic functions are then simply:

$$sn(u) = \sin\phi_0$$

$$cn(u) = \cos\phi_0$$

$$dn(u) = (1 - m \cdot sn(u)^2)^{\frac{1}{2}}$$

Limitations

The ellipj function is limited to the input domain  $0 \le m \le 1$ . Map other values of Minto this range using the transformations described in [1], equations 16.10 and 16.11. U is limited to real values.

See Also

el l i pke

Complete elliptic integrals of the first and second kind

References

[1] Abramowitz, M. and I.A. Stegun, *Handbook of Mathematical Functions*, Dover Publications, 1965, 17.6.

Complete elliptic integrals of the first and second kind

**Syntax** 

$$[K, E] = ellipke(M, tol)$$

**Definition** 

The *complete* elliptic integral of the first kind [1] is:

$$K(m) = F(\pi/2|m),$$

where *F*, the elliptic integral of the first kind, is:

$$K(m) = \int_0^1 [(1-t^2)(1-mt^2)]^{\frac{-1}{2}} dt = \int_0^{\frac{\pi}{2}} (1-m\sin^2\theta)^{\frac{-1}{2}} d\theta$$

The complete elliptic integral of the second kind,

$$E(m) = E(K(m)) = E\langle \pi/2|m\rangle,$$

is:

$$E(m) = \int_0^1 (1 - t^2)^{\frac{1}{2}} (1 - mt^2)^{\frac{1}{2}} dt = \int_0^{\frac{\pi}{2}} (1 - m\sin^2\theta)^{\frac{1}{2}} d\theta$$

Some definitions of K and E use the modulus k instead of the parameter m. They are related by:

$$k^2 = m = \sin^2 \alpha$$

# ellipke

Description

K = ellipke(M) returns the complete elliptic integral of the first kind for the elements of M.

[K,E] = ellipke(M) returns the complete elliptic integral of the first and second kinds.

[K, E] = ellipke(M, tol) computes the Jacobian elliptic functions to accuracy tol. The default is eps; increase this for a less accurate but more quickly computed answer.

**Algorithm** 

ellipke computes the complete elliptic integral using the method of the arithmetic-geometric mean described in [1], section 17.6. It starts with the triplet of numbers:

$$a_0 = 1$$
,  $b_0 = (1 - m)^{\frac{1}{2}}$ ,  $c_0 = (m)^{\frac{1}{2}}$ 

el l i pke computes successive iterations of  $a_i$ ,  $b_i$ , and  $c_i$  with:

$$a_{i} = \frac{1}{2}(a_{i-1} + b_{i-1})$$

$$b_{i} = (a_{i-1}b_{i-1})^{\frac{1}{2}}$$

$$c_{i} = \frac{1}{2}(a_{i-1} - b_{i-1})$$

stopping at iteration n when  $cn \approx 0$ , within the tolerance specified by eps. The complete elliptic integral of the first kind is then:

$$K(m) = \frac{\pi}{2a_n}$$

Limitations

el l i pke is limited to the input domain  $0 \le m \le 1$ .

See Also

ellipj

Jacobi elliptic functions

References

[1] Abramowitz, M. and I.A. Stegun, *Handbook of Mathematical Functions*, Dover Publications, 1965, 17.6.

**Purpose** Conditionally execute statements

Syntax if expression

statements

else

statements

end

**Description** 

The  ${\it el}\ {\it se}\ command$  is used to delineate an alternate block of statements.

if expression statements

else

statements

end

The second set of *statements* is executed if the *expressi on* has any zero elements. The expression is usually the result of

expression rop expression

where *rop* is ==, <, >, <=, >=, or ~=.

See Also

break	Break out of flow control structures
el sei f	Conditionally execute statements

end Terminate for, while, and if statements and indicate

the last index

for Repeat statements a specific number of times

if Conditionally execute statements return Return to the invoking function

switch Switch among several cases based on expression while Repeat statements an indefinite number of times

## **Purpose** Conditionally execute statements

**Syntax** 

```
if expression
statements
elseif expression
statements
end
```

# **Description**

The el seif command conditionally executes statements.

```
if expression
statements
elseif expression
statements
end
```

The second block of *statements* executes if the first *expressi on* has any zero elements and the second *expressi on* has all nonzero elements. The expression is usually the result of

```
expressi on rop expressi on where rop is ==, <, >, <=, >=, or \sim=.
```

el se i f, with a space between the el se and the i f, differs from el sei f, with no space. The former introduces a new, nested, i f, which must have a matching end. The latter is used in a linear sequence of conditional statements with only one terminating end.

### The two segments

```
if A
if A
   x = a
                                 x = a
else
                             elseif B
   if B
                                 x = b
                             elseif C
      x = b
                                 x = c
   el se
       if C
                             el se
                                 x = d
          x = c
                             end
       el se
           x = d
       end
   end
end
```

produce identical results. Exactly one of the four assignments to x is executed, depending upon the values of the three logical expressions, A, B, and C.

## See Also

break	Break out of flow control structures
else	Conditionally execute statements
end	Terminate for, while, and if statements and indicate
	the last index
for	Repeat statements a specific number of times
i f	Conditionally execute statements
return	Return to the invoking function
switch	Switch among several cases based on expression
whi l e	Repeat statements an indefinite number of times

Terminate for, while, switch, and if statements or indicate last index

### **Syntax**

```
while expression% (Or if or for)
    statements
end
B = A(index: end, index)
```

# Description

end is used to terminate for, while, switch, and if statements. Without an end statement, for, while, switch, and if wait for further input. Each end is paired with the closest previous unpaired for, while, switch, or if and serves to delimit its scope.

The end command also serves as the last index in an indexing expression. In that context, end = (si ze(x, k)) when used as part of the kth index.

# **Examples**

This example shows end used with for and if. Indentation provides easier readability.

```
for i = 1:n

if a(i) == 0

a(i) = a(i) + 2;

end

end
```

Here, end is used in an indexing expression:

```
A = rand(5, 4)

B = A(end, 2: end)
```

break

In this example, B is a 1-by-3 vector equal to  $[A(5, 2) \ A(5, 3) \ A(5, 4)]$ .

Break out of flow control structures

### See Also

DI CUN	Bream out of how control structures
for	Repeat statements a specific number of times
i f	Conditionally execute statements
return	Return to the invoking function
switch	Switch among several cases based on expression
whi l e	Repeat statements an indefinite number of times

End of month **Purpose** 

**Syntax** E = eomday(Y, M)

**Description** E = eomday(Y, M) returns the last day of the year and month given by corre-

sponding elements of arrays Y and M.

**Examples** Because 1996 is a leap year, the statement eomday (1996, 2) returns 29.

To show all the leap years in this century, try:

```
y = 1900: 1999;
E = \text{eomday}(y, 2*\text{ones}(l \text{ ength}(y), 1)');
y(find(E==29))'
```

a

ans =						
	ns 1 throu	gh 6				
1	1904	1908	1912	1916	1920	1924
Col um	ns 7 throu	gh 12				
1	1928	1932	1936	1940	1944	1948
Col um	ns 13 thro	ugh 18				
1	1952	1956	1960	1964	1968	1972
Col um	ns 19 thro	ugh 24				
	1976	1980	1984	1988	1992	1996

See Also

datenum	Serial date number
datevec	Date components
weekday	Day of the week

# eps

**Purpose** Floating-point relative accuracy

Syntax eps

**Description** eps returns the distance from 1.0 to the next largest floating-point number.

The value  $\ensuremath{\mathsf{eps}}$  is a default tolerance for  $\ensuremath{\mathsf{pi}}$  nv and  $\ensuremath{\mathsf{rank}}$ , as well as several other

MATLAB functions. On machines with IEEE floating-point arithmetic,

eps =  $2^{(-52)}$ , which is roughly 2. 22e-16.

See Also real max Largest positive floating-point number

real min Smallest positive floating-point number

**Purpose** Error functions

**Syntax** Y = erf(X) Error function

Y = erfc(X) Complementary error function

Y = erfcx(X) Scaled complementary error function

X = erfinv(Y) Inverse of the error function

**Definition** The error function erf(X) is defined as the integral of the Gaussian distribution function from 0 to x:

$$erf(x) = \frac{2}{\sqrt{\pi}} \int_0^x e^{-t^2} dt$$

The complementary error function erfc(X) is defined as:

$$erfc(x) = \frac{2}{\sqrt{\pi}} \int_{x}^{\infty} e^{-t^2} dt = 1 - erf(x)$$

The scaled complementary error function erfcx(X) is defined as:

$$erfcx(x) = e^{x^2}erfc(x)$$

For large X,  $\operatorname{erfcx}(X)$  is approximately  $\left(\frac{1}{\sqrt{\pi}}\right)\frac{1}{X}$ .

**Description** Y = erf(X) returns the value of the error function for each element of real array X.

Y = erfc(X) computes the value of the complementary error function.

Y = erfcx(X) computes the value of the scaled complementary error function.

X = erfinv(Y) returns the value of the inverse error function for each element of Y. The elements of Y must fall within the domain -1 < Y < 1.

**Examples** erfinv(1) is Inf

erfinv(-1) is -I nf.

For abs(Y) > 1, erfinv(Y) is NaN.

### Remarks

The relationship between the error function and the standard normal probability distribution is:

```
x = -5: 0.1: 5;
standard_normal_cdf = (1 + (erf(x*sqrt(2))))./2;
```

# **Algorithms**

For the error functions, the MATLAB code is a translation of a Fortran program by W. J. Cody, Argonne National Laboratory, NETLIB/SPECFUN, March 19, 1990. The main computation evaluates near-minimax rational approximations from [1].

For the inverse of the error function, rational approximations accurate to approximately six significant digits are used to generate an initial approximation, which is then improved to full accuracy by two steps of Newton's method. The M-file is easily modified to eliminate the Newton improvement. The resulting code is about three times faster in execution, but is considerably less accurate.

### References

[1] Cody, W. J., "Rational Chebyshev Approximations for the Error Function," *Math. Comp.*, pgs. 631-638, 1969

**Purpose** Display error messages

**Syntax** error('error\_message')

**Description** error('error\_message') displays an error message and returns control to

the keyboard. The error message contains the input string *error\_message*.

The error command has no effect if *error\_message* is a null string.

**Examples** The error command provides an error return from M-files.

```
\begin{array}{ll} function \ foo(x,y) \\ if \ nargin \ \sim= \ 2 \\ & error('\, Wrong \ number \ of \ input \ arguments') \\ end \end{array}
```

The returned error message looks like:

```
» foo(pi)
??? Error using ==> foo
Wrong number of input arguments
```

See Also Set breakpoints in an M-file function

di sp Display text or array lasterr Last error message

warni ng Display warning message

# errortrap

**Purpose** Continue execution after errors during testing

Syntax errortrap on

errortrap off

**Description** errortrap on continues execution after errors when they occur. Execution

continues with the next statement in a top level script.

errortrap off (the default) stops execution when an error occurs.

**Purpose** Elapsed time

**Syntax** e = etime(t2, t1)

**Description** e = etime(t2, t1) returns the time in seconds between vectors t1 and t2. The

two vectors must be six elements long, in the format returned by clock:

T = [Year Month Day Hour Minute Second]

**Examples** Calculate how long a 2048-point real FFT takes.

**Limitations** As currently implemented, the etime function fails across month and year

boundaries. Since etime is an M-file, you can modify the code to work across

these boundaries if needed.

See Also clock Current time as a date vector

cputi me Elapsed CPU time tic, toc Stopwatch timer

Interpret strings containing MATLAB expressions

### **Syntax**

```
a = eval('expression')
[a1, a2, a3...] = eval('expression')
eval(string, catchstring)
```

### Description

a = eval ('expressi on') returns the value of expressi on, a MATLAB expression, enclosed in single quotation marks. Create 'expressi on' by concatenating substrings and variables inside square brackets.

[a1, a2, a3...] = eval('expression') evaluates and returns the results in separate variables. Use of this syntax is recommended over:

```
eval ('[a1, a2, a3...] = expression')
```

which hides information from the MATLAB parser and can produce unexpected behavior.

eval (*string*, *catchstring*) provides the ability to catch errors. It executes *string* and returns if the operation was successful. If the operation generates an error, *catchstring* is evaluated before returning. Use I asterr to obtain the error string produced by *string*.

# **Examples**

end

generates a sequence of 12 matrices named M1 through M12.

The next example runs a selected M-file script. Note that the strings making up the rows of matrix D must all have the same length.

```
D = ['odedemo'
    'quaddemo'
    'zerodemo'
    'fitdemo'];
n = input('Select a demo number: ');
eval(D(n,:))
```

## See Also

feval Function evaluation lasterr Last error message.

# evalin

**Purpose** Evaluate expression in workspace.

**Syntax** evalin(ws, 'expression')

[X, Y, Z, ...] = evalin(ws, 'expression')

evalin(ws, 'try', 'catch')

**Description** eval i n(ws, 'expression') evaluates expression in the context of the work-

space ws. ws can be either 'caller' or 'base'.

[X, Y, Z, ...] = eval in(ws, 'expression') returns output arguments from

the expression.

eval i n(ws, 'try', 'catch') tries to evaluate the try expression and if that

fails it evaluates the *catch* expression in the specified workspace.

eval i n is useful for getting values from another workspace while assi gni n is

useful for depositing values into another workspace.

**Limitation** eval in may not be used recursively to evaluate an expression, i.e., a sequence

of the form evalin('caller', 'evalin('caller', 'expression')')

doesn't work.

**See Also** assignin Assign variable in workspace.

eval Interpret strings containing MATLAB expressions

### **Purpose** Check if a variable or file exists

### **Syntax** a = exist('item')

ident = exist('item', kind)

#### **Description**

a = exist('item') returns the status of the variable or file item:

- 0 If i tem does not exist.
- 1 If the variable *i tem* exists in the workspace.
- 2 If *i tem* is an M-file or a file of unknown type.
- 3 If *i tem* is a MEX-file.
- 4 If *i tem* is a MDL-file.
- 5 If *i tem* is a built-in MATLAB function.
- 6 If *i tem* is a P-file.
- 7 If *i tem* is a directory.

 $\operatorname{exi}\operatorname{st}('item')$  or  $\operatorname{exi}\operatorname{st}('item.ext')$  returns 2 if item is on the MATLAB search path but the filename extension (ext) is not  $\operatorname{mdl}$ ,  $\operatorname{p}$ , or  $\operatorname{mex}$ . item may be a MATLABPATH relative partial pathname.

i dent = exi st('i tem', 'ki nd') returns logical true (1) if an item of the specified ki nd is found, and returns 0 otherwise. ki nd may be:

'var' Checks only for variables.

 $\begin{tabular}{ll} 'builtin' & Checks only for built-in functions. \\ \end{tabular}$ 

'file' Checks only for files.

'dir' Checks only for directories.

## **Examples**

exi st can check whether a MATLAB function is built-in or a file:

```
i dent = exist('plot')
i dent =
5
```

pl ot is a built-in function.

#### See Also

di r Directory listing

hel p Online help for MATLAB functions and M-files

lookfor Keyword search through all help entries

what Directory listing of M-files, MAT-files, and MEX-files

whi ch Locate functions and files

who List directory of variables in memory

See also partialpath.

Purpose Exponential

**Syntax**  $Y = \exp(X)$ 

**Description** The exp function is an elementary function that operates element-wise on

arrays. Its domain includes complex numbers.

Y =  $\exp(X)$  returns the exponential for each element of X. For complex z = x + i\*y, it returns the complex exponential:  $e^z = e^x(\cos(y) + i\sin(y))$ .

**Remark** Use expm for matrix exponentials.

See Also expm Matrix exponential

l og Natural logarithm

l og 10 Common (base 10) logarithm

expi nt Exponential integral

# expint

**Purpose** 

Exponential integral

**Syntax** 

$$Y = expint(X)$$

**Definitions** 

The exponential integral is defined as:

$$\int_{x}^{\infty} \frac{e^{-t}}{t} dt$$

Another common definition of the exponential integral function is the Cauchy principal value integral:

$$E_{i}(x) = \int_{-\infty}^{x} e^{-t} dt$$

which, for real positive x, is related to expi nt as follows:

$$expint(-x+i*0) = -Ei(x) - i*pi$$
  
 $Ei(x) = real(-expint(-x))$ 

**Description** 

Y = expint(X) evaluates the exponential integral for each element of X.

Algorithm

For elements of X in the domain [-38,2], expi nt uses a series expansion representation (equation 5.1.11 in [1]):

$$E_i(x) = -\gamma - \ln x - \sum_{n=1}^{\infty} \frac{(-1)^n x^n}{n \ n!}$$

For all other elements of X, expint uses a continued fraction representation (equation 5.1.22 in [1]):

$$E_n(z) = e^{-z} \left( \frac{1}{z+} \frac{n}{1+} \frac{1}{z+} \frac{n+1}{1+} \frac{2}{z+} \dots \right), |angle(z)| < \pi$$

References

[1] Abramowitz, M. and I. A. Stegun. *Handbook of Mathematical Functions*. Chapter 5, New York: Dover Publications, 1965.

Purpose

Matrix exponential

**Syntax** 

Y = expm(X)

**Description** 

 $Y = \exp(X)$  raises the constant e to the matrix power X. Complex results are produced if X has nonpositive eigenvalues.

Use exp for the element-by-element exponential.

**Algorithm** 

The expm function is built-in, but it uses the Padé approximation with scaling and squaring algorithm expressed in the file expm1. m.

A second method of calculating the matrix exponential uses a Taylor series approximation. This method is demonstrated in the file expm2. m. The Taylor series approximation is not recommended as a general-purpose method. It is often slow and inaccurate.

A third way of calculating the matrix exponential, found in the file expm3. m, is to diagonalize the matrix, apply the function to the individual eigenvalues, and then transform back. This method fails if the input matrix does not have a full set of linearly independent eigenvectors.

References [1] and [2] describe and compare many algorithms for computing expm(X). The built-in method, expm1, is essentially method 3 of [2].

**Examples** 

Suppose A is the 3-by-3 matrix

1	1	0
0	0	2
0	0	-1

then expm(A) is

2.7183	1. 7183	1. 0862
0	1.0000	1. 2642
0	0	0. 3679

while exp(A) is

2. 7183	2. 7183	1. 0000
1.0000	1. 0000	7. 3891
1.0000	1. 0000	0. 3679

Notice that the diagonal elements of the two results are equal; this would be true for any triangular matrix. But the off-diagonal elements, including those below the diagonal, are different.

See Also exp Exponential

funm Evaluate functions of a matrix

l ogm Matrix logarithm sqrtm Matrix square root

References [1] Golub, G. H. and C. F. Van Loan, *Matrix Computation*, p. 384, Johns

Hopkins University Press, 1983.

 $\label{eq:compute} \ensuremath{\text{[2]}}\ Moler,\,C.\,B.\ and\,C.\,F.\ Van\,Loan,\,\ensuremath{\text{``Nineteen Dubious Ways to Compute the}}$ 

Exponential of a Matrix," SIAM Review 20, 1979, pp. 801-836.

**Purpose** Identity matrix

**Syntax** Y = eye(n)

Y = eye(m, n)

Y = eye(size(A))

**Description** Y = eye(n) returns the n-by-n identity matrix.

 $Y = \exp(m, n) \text{ or } \exp([m \ n]) \text{ returns an } m\text{-by-n matrix with 1's on the diag-}$ 

onal and 0's elsewhere.

Y = eye(size(A)) returns an identity matrix the same size as A.

**Limitations** The identity matrix is not defined for higher-dimensional arrays. The assign-

ment y = eye([2, 3, 4]) results in an error.

**See Also** ones Create an array of all ones

rand Uniformly distributed random numbers and arrays randn Normally distributed random numbers and arrays

zeros Create an array of all zeros

# factor

**Purpose** Prime factors

**Syntax** f = factor(n)

f = factor(symb)

**Description** f = factor(n) returns a row vector containing the prime factors of n.

**Examples** f = factor(123)

f =

3 41

See Also i spri me True for prime numbers

pri mes Generate list of prime numbers

**Purpose** Close one or more open files

**Syntax** status = fclose(fid)

status = fclose('all')

**Description** status = fclose(fid) closes the specified file, if it is open, returning 0 if

successful and -1 if unsuccessful. Argument fid is a file identifier associated

with an open file (See fopen for a complete description).

status = fclose('all') closes all open files, (except standard input, output,

and error), returning 0 if successful and -1 if unsuccessful.

See Also Gerror Query MATLAB about errors in file input or output

fopen Open a file or obtain information about open files

fprintf Write formatted data to file
fread Read binary data from file
fscanf Read formatted data from file
fseek Set file position indicator
ftel Get file position indicator

fwrite Write binary data from a MATLAB matrix to a file

## feof

**Purpose** Test for end-of-file

**Syntax** eofstat = feof(fid)

**Description** eof stat = feof(fid) tests whether the end-of-file indicator is set for the file

with identifier fid. It returns 1 if the end-of-file indicator is set, or 0 if it is not.

(See fopen for a complete description of fid.)

The end-of-file indicator is set when there is no more input from the file.

**Purpose** Query MATLAB about errors in file input or output

#### **Syntax** message = ferror(fid)

message = ferror(fid, 'clear')
[message, errnum] = ferror(...)

#### **Description**

message = ferror(fid) returns the error message message. Argument fid is a file identifier associated with an open file (See fopen for a complete description).

message = ferror(fid, 'clear') clears the error indicator for the specified file.

[message, errnum] = ferror( $\dots$ ) returns the error status number errnum of the most recent file I/O operation associated with the specified file.

If the most recent I/O operation performed on the specified file was successful, the value of message is empty and ferror returns an errnum value of 0.

A nonzero errnum indicates that an error occurred in the most recent file I/O operation. The value of message is a string that may contain information about the nature of the error. If the message is not helpful, consult the C runtime library manual for your host operating system for further details.

#### See Also

fclose	Close one or more	open files
--------	-------------------	------------

fopen Open a file or obtain information about open files

fprintf Write formatted data to file fread Read binary data from file fscanf Read formatted data from file fseek Set file position indicator ftel Get file position indicator

fwrite Write binary data from a MATLAB matrix to a file

**Purpose** Function evaluation

**Syntax**  $[y_1, y_2, \dots] = \text{feval } (function, x_1, \dots, x_n)$ 

**Description**  $[y_1, y_2, ...] = feval (function, x_1, ..., x_n)$  If function is a string

containing the name of a function (usually defined by an M-file), then

feval (function, x1, ..., xn) evaluates that function at the given arguments.

**Examples** The statements:

$$[V, D] = feval('eig', A)$$
  
 $[V, D] = eig(A)$ 

are equivalent. feval is useful in functions that accept string arguments specifying function names. For example, the function:

```
function plotf(fun, x)
y = feval(fun, x);
plot(x, y)
```

can be used to graph other functions.

See Also assignin Assign value to variable in workspace

builtin Execute builtin function from overloaded method eval Interpret strings containing MATLAB expressions

eval i n Evaluate expression in workspace.

**Purpose** 

One-dimensional fast Fourier transform

**Syntax** 

**Definition** 

The functions X = fft(x) and x = ifft(X) implement the transform and inverse transform pair given for vectors of length N by:

$$X(k) = \sum_{j=1}^{N} x(j)\omega_{N}^{(j-1)(k-1)}$$

$$x(j) = (1/N)\sum_{k=1}^{N} X(k)\omega_{N}^{-(j-1)(k-1)}$$

where

$$\omega_N = e^{(-2\pi i)/N}$$

is an nth root of unity.

Description

Y = fft(X) returns the discrete Fourier transform of vector X, computed with a fast Fourier transform (FFT) algorithm.

If X is a matrix, fft returns the Fourier transform of each column of the matrix.

If X is a multidimensional array, fft operates on the first nonsingleton dimension.

Y = fft(X, n) returns the n-point FFT. If the length of X is less than n, X is padded with trailing zeros to length n. If the length of X is greater than n, the sequence X is truncated. When X is a matrix, the length of the columns are adjusted in the same manner.

Y = fft(X, [], dim) and Y = fft(X, n, dim) apply the FFT operation across the dimension dim.

#### Remarks

The fft function employs a radix-2 fast Fourier transform algorithm if the length of the sequence is a power of two, and a slower mixed-radix algorithm if it is not. See "Algorithm."

### **Examples**

A common use of Fourier transforms is to find the frequency components of a signal buried in a noisy time domain signal. Consider data sampled at 1000 Hz. Form a signal containing 50 Hz and 120 Hz and corrupt it with some zero-mean random noise:

```
t = 0: 0.001: 0.6;

x = sin(2*pi*50*t) +sin(2*pi*120*t);

y = x + 2*randn(size(t));

plot(y(1:50))
```

It is difficult to identify the frequency components by looking at the original signal. Converting to the frequency domain, the discrete Fourier transform of the noisy signal y is found by taking the 512-point fast Fourier transform (FFT):

```
Y = fft(y, 512);
```

The power spectral density, a measurement of the energy at various frequencies, is

```
Pyy = Y. * conj (Y) / 512;
```

Graph the first 257 points (the other 255 points are redundant) on a meaningful frequency axis.

```
f = 1000*(0:256)/512;
plot(f, Pyy(1:257))
```

This represents the frequency content of y in the range from DC up to and including the Nyquist frequency. (The signal produces the strong peaks.)

## Algorithm

When the sequence length is a power of two, a high-speed radix-2 fast Fourier transform algorithm is employed. The radix-2 FFT routine is optimized to perform a real FFT if the input sequence is purely real, otherwise it computes the complex FFT. This causes a real power-of-two FFT to be about 40% faster than a complex FFT of the same length.

When the sequence length is not an exact power of two, an alternate algorithm finds the prime factors of the sequence length and computes the mixed-radix discrete Fourier transforms of the shorter sequences.

The time it takes to compute an FFT varies greatly depending upon the sequence length. The FFT of sequences whose lengths have many prime factors is computed quickly; the FFT of those that have few is not. Sequences whose lengths are prime numbers are reduced to the raw (and slow) discrete Fourier transform (DFT) algorithm. For this reason it is generally better to stay with power-of-two FFTs unless other circumstances dictate that this cannot be done. For example, on one machine a 4096-point real FFT takes 2.1 seconds and a complex FFT of the same length takes 3.7 seconds. The FFTs of neighboring sequences of length 4095 and 4097, however, take 7 seconds and 58 seconds, respectively.

#### See Also

dftmtx, filter, freqz, specplot, and spectrum in the Signal Processing Toolbox, and:

fft2 Two-dimensional fast Fourier transform fftshift Rearrange the outputs of fft and fft2

ifft Inverse one-dimensional fast Fourier transform

**Purpose** Two-dimensional fast Fourier transform

**Syntax** Y = fft2(X)

Y = fft2(X, m, n)

**Description** Y = fft2(X) performs the two-dimensional FFT. The result Y is the same size

as X.

Y = fft2(X, m, n) truncates X, or pads X with zeros to create an m-by-n array

before doing the transform. The result is m-by-n.

**Algorithm** fft2(X) can be simply computed as

fft(fft(X).').'

This computes the one-dimensional FFT of each column X, then of each row of the result. The time required to compute fft2(X) depends strongly on the

number of prime factors in [m, n] = si ze(X). It is fastest when m and n are powers of 2.

fftshift Rearrange the outputs of fft and fft2

ifft2 Inverse two-dimensional fast Fourier transform

**Purpose** 

Multidimensional fast Fourier transform

**Syntax** 

```
Y = fftn(X)

Y = fftn(X, siz)
```

**Description** 

Y = fftn(X) performs the N-dimensional fast Fourier transform. The result Y is the same size as X.

Y = fftn(X, si z) pads X with zeros, or truncates X, to create a multidimensional array of size si z before performing the transform. The size of the result Y is si z.

**Algorithm** 

fftn(X) is equivalent to

```
Y = X;
for p = 1:length(size(X))
        Y = fft(Y,[],p);
end
```

This computes in-place the one-dimensional fast Fourier transform along each dimension of X. The time required to compute fftn(X) depends strongly on the number of prime factors of the dimensions of X. It is fastest when all of the dimensions are powers of 2.

See Also

fft	One-dimensional fast Fourier transform
fft2	Two-dimensional fast Fourier transform

ifftn Inverse multidimensional fast Fourier transform

## fftshift

**Purpose** Shift DC component of fast Fourier transform to center of spectrum

**Syntax** Y = fftshift(X)

**Description** Y = fftshift(X) rearranges the outputs of fft, fft2, and fftn by moving the

zero frequency component to the center of the array.

For vectors, fftshift(X) swaps the left and right halves of X. For matrices, fftshift(X) swaps quadrants one and three of X with quadrants two and four. For higher-dimensional arrays, fftshift(X) swaps "half-spaces" of X along

each dimension.

**Examples** For any matrix X

Y = fft2(X)

has Y(1, 1) = sum(sum(X)); the DC component of the signal is in the upper-left corner of the two-dimensional FFT. For

Z = fftshift(Y)

this DC component is near the center of the matrix.

**See Also** fft One-dimensional fast Fourier transform

fft2 Two-dimensional fast Fourier transform fftn Multidimensional fast Fourier transform

**Purpose** Return the next line of a file as a string without line terminator(s)

**Syntax** line = fgetl(fid)

**Description** line = fgetl(fid) returns the next line of the file with identifier fid. If

fget1 encounters the end of a file, it returns -1. (See fopen for a complete

description of fid.)

The returned string line does not include the line terminator(s) with the text

line (to obtain the line terminator(s), use fgets).

**See Also** fgets Return the next line of a file as a string with line termi-

nator(s)

# fgets

**Purpose** Return the next line of a file as a string with line terminator(s)

**Syntax** line = fgets(fid)

line = fgets(fid, nchar)

**Description** line = fgets(fid) returns the next line for the file with identifier fid. If

fgets encounters the end of a file, it returns –1. (See fopen for a complete

description of fid.)

The returned string line includes the line terminator(s) associated with the text line (to obtain the string without the line terminator(s), use fget1).

line = fgets(fid, nchar) returns at most nchar characters of the next line. No additional characters are read after the line terminator(s) or an end-of-file.

terminator(s)

**Purpose** Field names of a structure

**Syntax** names = fieldnames(s)

**Description** names = fieldnames(s) returns a cell array of strings containing the struc-

ture field names associated with the structure s.

**Examples** Given the structure:

```
mystr(1, 1).name = 'alice';
mystr(1, 1).ID = 0;
mystr(2, 1).name = 'gertrude';
mystr(2, 1).ID = 1
```

Then the command n = fi el dnames(mystr) yields

```
n =
'name'
'ID'
```

See Also

getfield Get field of structure array setfield Set field of structure array

# fileparts

**Purpose** Filename parts

**Syntax** [path, name, ext, ver] = fileparts(file)

**Description** [path, name, ext, ver] = fileparts(file) returns the path, filename, exten-

sion, and version for the specified file. ver will be nonemply only on VMS

systems. fileparts is platform dependent.

You can reconstruct the file from the parts using

fullfile(path, [name ext ver]).

**See Also** fullfile Build full filename from parts

### **Purpose**

Filter data with an infinite impulse response (IIR) or finite impulse response (FIR) filter

#### **Syntax**

```
y = filter(b, a, X)
[y, zf] = filter(b, a, X)
[y, zf] = filter(b, a, X, zi)
y = filter(b, a, X, zi, dim)
[...] = filter(b, a, X, [], dim)
```

### Description

The filter function filters a data sequence using a digital filter which works for both real and complex inputs. The filter is a *direct form II transposed* implementation of the standard difference equation (see "Algorithm").

y = filter(b, a, X) filters the data in vector X with the filter described by numerator coefficient vector b and denominator coefficient vector a. If a(1) is not equal to 1, filter normalizes the filter coefficients by a(1). If a(1) equals 0, filter returns an error.

If X is a matrix, filter operates on the columns of X. If X is a multidimensional array, filter operates on the first nonsingleton dimension.

[y, zf] = filter(b, a, X) returns the final conditions, zf, of the filter delays. Output zf is a vector of max(size(a), size(b)) or an array of such vectors, one for each column of X.

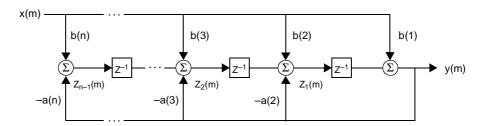
[y, zf] = filter(b, a, X, zi) accepts initial conditions and returns the final conditions, zi and zf respectively, of the filter delays. Input zi is a vector (or an array of vectors) of length max(length(a), length(b)) -1.

```
y = filter(b, a, X, zi, dim) and
```

[...] = filter(b, a, X, [], dim) operate across the dimension dim.

## **Algorithm**

The filter function is implemented as a direct form II transposed structure,



or

$$y(n) = b(1)*x(n) + b(2)*x(n-1) + ... + b(nb+1)*x(n-nb) - a(2)*y(n-1) - ... - a(na+1)*y(n-na)$$

where n-1 is the filter order, and which handles both FIR and IIR filters [1].

The operation of filter at sample m is given by the time domain difference equations

$$y(m) = b(1)x(m) + z_1(m-1)$$

$$z_1(m) = b(2)x(m) + z_2(m-1) - a(2)y(m)$$

$$\vdots = \vdots \qquad \vdots$$

$$z_{n-2}(m) = b(n-1)x(m) + z_{n-1}(m-1) - a(n-1)y(m)$$

$$z_{n-1}(m) = b(n)x(m) - a(n)y(m)$$

The input-output description of this filtering operation in the *z*-transform domain is a rational transfer function,

$$Y(z) = \frac{b(1) + b(2)z^{-1} + \dots + b(nb+1)z^{-nb}}{1 + a(2)z^{-1} + \dots + a(na+1)z^{-na}}X(z)$$

See Also

filtfilt in the Signal Processing Toolbox, and:

filter2

Two-dimensional digital filtering

References

[1] Oppenheim, A. V. and R.W. Schafer. *Discrete-Time Signal Processing*, Englewood Cliffs, NJ: Prentice-Hall, 1989, pp. 311–312.

**Purpose** 

Two-dimensional digital filtering

**Syntax** 

Y = filter2(h, X)

Y = filter2(h, X, shape)

Description

Y = filter2(h, X) filters the data in X with the two-dimensional FIR filter in the matrix h. It computes the result, Y, using two-dimensional correlation, and returns the central part of the correlation that is the same size as X.

Y = filter2(h, X, shape) returns the part of Y specified by the shape parameter. shape is a string with one of these values:

- 'full' returns the full two-dimensional correlation. In this case, Y is larger than X.
- 'same' (the default) returns the central part of the correlation. In this case, Y is the same size as X.
- 'valid' returns only those parts of the correlation that are computed without zero-padded edges. In this case, Y is smaller than X.

Remarks

Two-dimensional correlation is equivalent to two-dimensional convolution with the filter matrix rotated 180 degrees. See the Algorithm section for more information about how filter2 performs linear filtering.

**Algorithm** 

Given a matrix X and a two-dimensional FIR filter h, filter 2 rotates your filter matrix 180 degrees to create a convolution kernel. It then calls conv2, the two-dimensional convolution function, to implement the filtering operation.

filter2 uses conv2 to compute the full two-dimensional convolution of the FIR filter with the input matrix. By default, filter2 then extracts the central part of the convolution that is the same size as the input matrix, and returns this as the result. If the shape parameter specifies an alternate part of the convolution for the result, filter2 returns the appropriate part.

See Also

conv2 Two-dimensional convolution

filter Filter data with an infinite impulse response (IIR) or

finite impulse response (FIR) filter

### **Purpose**

Find indices and values of nonzero elements

### **Syntax**

## **Description**

k = find(X) returns the indices of the array x that point to nonzero elements. If none is found, find returns an empty matrix.

[i,j] = find(X) returns the row and column indices of the nonzero entries in the matrix X. This is often used with sparse matrices.

[i, j, v] = find(X) returns a column vector v of the nonzero entries in X, as well as row and column indices.

In general, find(X) regards X as X(:), which is the long column vector formed by concatenating the columns of X.

## **Examples**

 $[\,i\,,\,j\,,\,v\,]=f\,i\,nd(X\sim=0)\,$  produces a vector v with all 1s, and returns the row and column indices.

Some operations on a vector

```
x = [11 0 33 0 55]';
find(x)
ans =
    1
    3
    5

find(x == 0)
ans =
    2
    4
```

**See Also** 

The relational operators <, <=,>=,==,  $\sim=$ , and:

nonzeros sparse Nonzero matrix elements Create sparse matrix

## findstr

**Purpose** Find one string within another

**Syntax** k = findstr(str1, str2)

**Description** k = findstr(str1, str2) finds the starting indices of any occurrences of the

shorter string within the longer.

**Examples** str1 = 'Find the starting indices of the shorter string.';

str2 = 'the';

findstr(str1, str2)

ans =

6 30

See Also strcmp Compare strings

strmatch Find possible matches for a string

strncmp Compare the first n characters of two strings

**Purpose** Round towards zero

Syntax B = fix(A)

**Description** B = fix(A) rounds the elements of A toward zero, resulting in an array of inte-

gers. For complex A, the imaginary and real parts are rounded independently.

**Examples** a =

Columns 1 through 4

-1. 9000 -0. 2000 3. 4000 5. 6000

Columns 5 through 6

7. 0000 2. 4000 + 3. 6000i

fix(a)

ans =

Columns 1 through 4

-1.0000 0 3.0000 5.0000

Columns 5 through 6

7. 0000 2. 0000 + 3. 0000i

See Also ceil Round toward infinity

floor Round towards minus infinity round Round to nearest integer

# flipdim

**Purpose** Flip array along a specified dimension

**Syntax** B = flipdim(A, dim)

**Description** B = flipdim(A, dim) returns A with dimension dim flipped.

When the value of dim is 1, the array is flipped row-wise down. When dim is 2, the array is flipped columnwise left to right. flipdim(A, 1) is the same as  $(A_1, A_2, A_3, A_4, A_4, A_4, A_5)$  is the same as  $(A_1, A_2, A_4, A_4, A_5)$  is the same as

flipud(A), and flipdim(A, 2) is the same as fliplr(A).

**Examples** flipdim(A, 1) where

A =

1 4 2 5 3 6

produces

3 6 2 5 1 4

 $\begin{array}{ccc} \textbf{See Also} & & \text{fl\,i\,pl\,r} & & \text{Flip matrices left-right} \\ & & \text{fl\,i\,pud} & & \text{Flip matrices up-down} \\ \end{array}$ 

 $permute \hspace{1cm} Rearrange \ the \ dimensions \ of \ a \ multidimensional \ array$ 

rot 90 Rotate matrix 90°

**Purpose** Flip matrices left-right

Syntax B = fliplr(A)

**Description** B = fliplr(A) returns A with columns flipped in the left-right direction, that

is, about a vertical axis.

Examples A =

1 4 2 5 3 6

produces

4 1 5 2 6 3

**Limitations** Array A must be two dimensional.

**See Also** flipdim Flip array along a specified dimension

 $\begin{array}{ccc} \text{fli pud} & & \text{Flip matrices up-down} \\ \text{rot 90} & & \text{Rotate matrix } 90^{\circ} \end{array}$ 

# flipud

**Purpose** Flip matrices up-down

Syntax B = flipud(A)

**Description** B = flipud(A) returns A with rows flipped in the up-down direction, that is,

about a horizontal axis.

**Examples** A =

1 4 2 5 3 6

produces

3 6 2 5 1 4

**Limitations** Array A must be two dimensional.

**See Also** flipdim Flip array along a specified dimension

 $fl\,i\,pl\,r \hspace{1cm} Flip\ matrices\ left-right$ 

rot 90 Rotate matrix 90°

**Purpose** Round towards minus infinity

**Syntax** B = floor(A)

**Description** B = floor(A) rounds the elements of A to the nearest integers less than or

equal to A. For complex A, the imaginary and real parts are rounded indepen-

dently.

**Examples** a =

Columns 1 through 4

-1. 9000 -0. 2000 3. 4000 5. 6000

Columns 5 through 6

7. 0000 2. 4000 + 3. 6000i

floor(a)

ans =

Columns 1 through 4

-2. 0000 -1. 0000 3. 0000 5. 0000

Columns 5 through 6

7. 0000 2. 0000 + 3. 0000i

See Also ceil Round toward infinity fix Round towards zero

round Round to nearest integer

**Purpose** Count floating-point operations

Syntax f = flopsflops(0)

**Description** f = flops returns the cumulative number of floating-point operations.

flops(0) resets the count to zero.

**Examples** If A and B are real n-by-n matrices, some typical flop counts for different operations are:

Operation	Flop Count
A+B	n^2
A*B	2*n^3
A^100	99*(2*n^3)
lu(A)	(2/3)*n^3

#### MATLAB's version of the LINPACK benchmark is:

```
n = 100;
A = rand(n, n);
b = rand(n, 1);
flops(0)
tic;
x = A\b;
t = toc
megaflops = flops/t/1.e6
```

### **Algorithm**

It is not feasible to count all the floating-point operations, but most of the important ones are counted. Additions and subtractions are each one flop if real and two if complex. Multiplications and divisions count one flop each if the result is real and six flops if it is complex. Elementary functions count one if real and more if complex.

Minimize a function of one variable

### **Syntax**

```
x = fmin('fun', x1, x2)

x = fmin('fun', x1, x2, options)

x = fmin('fun', x1, x2, options, P1, P2, ...)

[x, options] = fmin(...)
```

### **Description**

x = fmin('fun', x1, x2) returns a value of x which is a local minimizer of fun(x) in the interval  $x_1 < x < x_2$ .

x = fmin('fun', x1, x2, options) does the same as the above, but uses options control parameters.

x = fmin(fun', x1, x2, options, P1, P2, ...) does the same as the above, but passes arguments to the objective function, fun(x, P1, P2, ...). Pass an empty matrix for options to use the default value.

[x, options] = fmin(...) returns, in options(10), a count of the number of steps taken.

## **Arguments**

x1, x2 Interval over which function is minimized.

P1, P2. . . Arguments to be passed to function.

fun A string containing the name of the function to be minimized.

opti ons

A vector of control parameters. Only three of the 18 components of options are referenced by fmin; Optimization Toolbox functions use the others. The three control options used by fmin are:

- options(1) If this is nonzero, intermediate steps in the solution are displayed. The default value of options(1) is 0.
- options(2) This is the termination tolerance. The default value is 1. e-4.
- options(14) This is the maximum number of steps. The default value is 500.

## **fmin**

## **Examples**

fmi n(' cos', 3, 4) computes  $\pi$  to a few decimal places.

fmi n( ' cos ' , 3, 4, [ 1, 1. e–12 ]) displays the steps taken to compute  $\pi$  to 12 decimal places.

To find the minimum of the function  $f(x) = x^3 - 2x - 5$  on the interval (0, 2), write an M-file called f. m.

function 
$$y = f(x)$$
  
 $y = x.^3-2*x-5$ ;

Then invoke fmin with

$$x = fmin('f', 0, 2)$$

The result is

$$x = 0.8165$$

The value of the function at the minimum is

$$y = f(x)$$
  
 $y = -6.0887$ 

## **Algorithm**

The algorithm is based on golden section search and parabolic interpolation. A Fortran program implementing the same algorithms is given in [1].

### See Also

 $\begin{array}{ll} \text{fmi ns} & \text{Minimize a function of several variables} \\ \text{fzero} & \text{Zero of a function of one variable} \\ \text{foptions in the Optimization Toolbox (or type help foptions)}. \end{array}$ 

### References

[1] Forsythe, G. E., M. A. Malcolm, and C. B. Moler, *Computer Methods for Mathematical Computations*, Prentice-Hall, 1976.

Minimize a function of several variables

### **Syntax**

```
x = fmins('fun', x0)
```

x = fmins('fun', x0, options)

x = fmins('fun', x0, options, [], P1, P2, ...)

[x, options] = fmins(...)

## Description

x = fmins('fun', x0) returns a vector x which is a local minimizer of fun(x) near  $x_0$ .

x = fmins('fun', x0, options) does the same as the above, but uses options control parameters.

x = fmins('fun', x0, options, [], P1, P2, ...) does the same as above, but passes arguments to the objective function, fun(x, P1, P2, ...). Pass an empty matrix for options to use the default value.

[x, options] = fmins(...) returns, in options(10), a count of the number of steps taken.

## **Arguments**

x0Starting vector.

P1, P2. . . Arguments to be passed to fun.

[] Argument needed to provide compatibility with fmi nu in the

Optimization Toolbox.

fun

A string containing the name of the objective function to be minimized. fun(x) is a scalar valued function of a vector variable.

options

A vector of control parameters. Only four of the 18 components of options are referenced by fmins; Optimization Toolbox functions use the others. The four control options used by fmins are:

- options(1) If this is nonzero, intermediate steps in the solution are displayed. The default value of options(1) is 0.
- options(2) and options(3) These are the termination tolerances for x and function(x), respectively. The default values are 1. e-4.
- options(14) This is the maximum number of steps. The default value is 500.

## **Examples**

A classic test example for multidimensional minimization is the Rosenbrock banana function:

$$f(x) = 100(x_2 - x_1^2)^2 + (1 - x_1)^2$$

The minimum is at (1, 1) and has the value 0. The traditional starting point is (-1, 2, 1). The M-file banana. m defines the function.

```
function f = banana(x)

f = 100*(x(2)-x(1)^2)^2+(1-x(1))^2;
```

The statements

```
[x, out] = fmins('banana', [-1.2, 1]);

x

out(10)
```

### produce

```
x =

1.0000 1.0000

ans =

165
```

This indicates that the minimizer was found to at least four decimal places in 165 steps.

Move the location of the minimum to the point  $[a, a^2]$  by adding a second parameter to banana. m.

```
function f = banana(x, a)
if nargin < 2, a = 1; end
f = 100*(x(2)-x(1)^2)^2+(a-x(1))^2;
```

Then the statement

```
[x, out] = fmins('banana', [-1.2, 1], [0, 1.e-8], [], sqrt(2));
```

sets the new parameter to  $\operatorname{sqrt}(2)$  and seeks the minimum to an accuracy higher than the default.

## **Algorithm**

The algorithm is the Nelder-Mead simplex search described in the two references. It is a direct search method that does not require gradients or other derivative information. If n is the length of x, a simplex in n-dimensional space is characterized by the n+1 distinct vectors which are its vertices. In two-space, a simplex is a triangle; in three-space, it is a pyramid.

At each step of the search, a new point in or near the current simplex is generated. The function value at the new point is compared with the function's values at the vertices of the simplex and, usually, one of the vertices is replaced by the new point, giving a new simplex. This step is repeated until the diameter of the simplex is less than the specified tolerance.

#### See Also

 $\begin{array}{ll} \text{fmi n} & \text{Minimize a function of one variable} \\ \text{foptions in the Optimization Toolbox (or type help foptions)} \,. \end{array}$ 

# **fmins**

## References

- [1] Nelder, J. A. and R. Mead, "A Simplex Method for Function Minimization," *Computer Journal*, Vol. 7, p. 308-313.
- [2] Dennis, J. E. Jr. and D. J. Woods, "New Computing Environments: Microcomputers in Large-Scale Computing," edited by A. Wouk, SIAM, 1987, pp. 116-122.

Open a file or obtain information about open files

### Syntax

```
fid = fopen(filename, permission)
[fid, message] = fopen(filename, permission, format)
fids = fopen('all')
[filename, permission, format] = fopen(fid)
```

### Description

If fopen successfully opens a file, it returns a file identifier fid, and the value of message is empty. The file identifier can be used as the first argument to other file input/output routines. If fopen does not successfully open the file, it returns a -1 value for fid. In that case, the value of message is a string that helps you determine the type of error that occurred.

Two fi ds are predefined and cannot be explicitly opened or closed:

- 1— Standard output, which is always open for appending (permi ssi on set to 'a'), and
- 2 Standard error, which is always open for appending (permi ssi on set to 'a').

fid = fopen(filename, permission) opens the file filename in the mode specified by permission and returns fid, the file identifier. filename may a MATLABPATH relative partial pathname. If the file is opened for reading and it is not found in the current working directory, fopen searches down MATLAB's search path.

*permi ssi on* is one of the strings:

' r'	Open the file for reading (default).
'r+'	Open the file for reading and writing.
' w'	Delete the contents of an existing file or create a new file, and open it for writing.
' w+'	Delete the contents of an existing file or create new file, and open it for reading and writing.
' W'	Write without automatic flushing; used with tape drives
' a'	Create and open a new file or open an existing file for writing, appending to the end of the file.

'a+' Create and open new file or open an existing file for reading and writing, appending to the end of the file.

'A' Append without automatic flushing; used with tape drives

Add a 't' to these strings, for example, 'rt', on systems that distinguish between text and binary files, to force the file to be opened in text mode. Under DOS and VMS, for example, you cannot read a text file unless you set the permission to 'rt'. Similarly, use a 'b' to force the file to be opened in binary mode (the default).

[fid, message] = fopen(filename, permission, format) opens a file as above, returning file identifier and message. In addition, you specify the numeric format with format, a string defining the numeric format of the file, allowing you to share files between machines of different formats. If you omit the format argument, the numeric format of the local machine is used. Individual calls to fread or fwrite can override the numeric format specified in a call to fopen. Permitted format strings are:

'native' or'n'	The numeric format of the machine you are currently running
'ieee-le' or $'l'$	IEEE floating point with little-endian byte ordering
'i eee-be' or 'b'	IEEE floating point with big-endian byte ordering
'vaxd' or 'd'	VAX D floating point and VAX ordering
'vaxg' or 'g'	VAX G floating point and VAX ordering
'cray' or 'c'	Cray floating point with big-endian byte ordering
'i eee-le. l64' or 'a'	IEEE floating point with little-endian byte ordering and 64-bit long data type
'i eee-be. l 64' or 's'	IEEE floating point with big-endian byte ordering and 64-bit long data type

fi ds = fopen('all') returns a row vector containing the file identifiers of all open files, not including 1 and 2 (standard output and standard error). The number of elements in the vector is equal to the number of open files.

 $[filename, permission, format] = fopen(fid) \ returns the full filename string, the permission string, and the format string associated with the specified file. An invalid fid returns empty strings for all output arguments. Both permission and format are optional.$ 

### See Also

fcl ose Close one or more open files

ferror Query MATLAB about errors in file input or output

fprintf Write formatted data to file fread Read binary data from file fscanf Read formatted data from file fseek Set file position indicator ftell Get file position indicator

fwrite Write binary data from a MATLAB matrix to a file

See also partialpath.

Repeat statements a specific number of times

### **Syntax**

```
for variable = expression
    statements
end
```

## Description

The general format is

```
for variable = expression
    statement
    ...
    statement
end
```

The columns of the *expressi* on are stored one at a time in the variable while the following statements, up to the end, are executed.

In practice, the *expressi on* is almost always of the form scal ar: scal ar, in which case its columns are simply scalars.

The scope of the for statement is always terminated with a matching end.

## **Examples**

Assume n has already been assigned a value. Create the Hilbert matrix, using zeros to preallocate the matrix to conserve memory:

```
\begin{array}{lll} a = zeros(n,n) & \text{\% Preallocate matrix} \\ for \ i = 1;n \\ & for \ j = 1;n \\ & a(i\,,j\,) = 1/(i\,+j\,-1)\,; \\ end \\ end \end{array}
```

Step s with increments of -0. 1

```
for s = 1.0: -0.1: 0.0, ..., end
```

Successively set e to the unit n-vectors:

```
for e = eye(n), \ldots, end
```

The line

```
for V = A, \ldots, end
```

has the same effect as

for 
$$j = 1: n, V = A(:,j); ..., end$$

except j is also set here.

See Also break Break out of flow control structures

end Terminate for, while, switch, and if statements and

indicate the last index

if Conditionally execute statements return Return to the invoking function

switch Switch among several cases based on expression while Repeat statements an indefinite number of times

## **format**

**Purpose** 

Control the output display format

**Syntax** 

MATLAB performs all computations in double precision. The  $\tt format$  command described below switches among different display formats.

## **Description**

Command	Result	Example	
format	Default. Same as short.		
format short	5 digit scaled fixed point	3. 1416	
format long	15 digit scaled fixed point	3. 14159265358979	
format short e	5 digit floating-point	3. 1416e+00	
format long e	15 digit floating-point	3. 141592653589793e+0 0	
format short g	Best of 5 digit fixed or floating	3. 1416	
format long g	Best of 15 digit fixed or floating	3. 14159265358979	
format hex	Hexadecimal	400921fb54442d18	
format bank	Fixed dollars and cents	3. 14	
format rat	Ratio of small integers	355/113	
format +	+,-, blank	+	
format compact	Suppresses excess line feeds.		
format loose	Add line feeds.		

## **Algorithms**

The command format + displays +, -, and blank characters for positive, negative, and zero elements. format hex displays the hexadecimal representation of a binary double-precision number. format rat uses a continued fraction algorithm to approximate floating-point values by ratios of small integers. See rat. m for the complete code.

See Also

fprintf, num2str, rat, sprintf, spy

Write formatted data to file

Syntax

```
count = fprintf(fid, format, A, ...)
fprintf(format, A, ...)
```

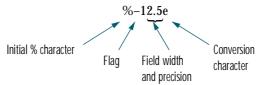
Description

count = fprintf(fid, format, A, ...) formats the data in the real part of matrix A (and in any additional matrix arguments) under control of the specified format string, and writes it to the file associated with file identifier fid. fprintf returns a count of the number of bytes written.

Argument fi d is an integer file identifier obtained from fopen. (It may also be 1 for standard output (the screen) or 2 for standard error. See fopen for more information.) Omitting fi d from fprintf's argument list causes output to appear on the screen, and is the same as writing to standard output (fi d = 1)

fprintf(format, A, ...) writes to standard output—the screen.

The *format* string specifies notation, alignment, significant digits, field width, and other aspects of output format. It can contain ordinary alphanumeric characters; along with escape characters, conversion specifiers, and other characters, organized as shown below:



For more information see "Tables" and "References".

# **fprintf**

### Remarks

The fprintf function behaves like its ANSI C language fprintf() namesake with certain exceptions and extensions. These include:

- 1 The following non-standard subtype specifiers are supported for conversion specifiers %0, %u, %x, and %X.
  - t The underlying C data type is a float rather than an unsigned integer.
  - b The underlying C data type is a double rather than an unsigned integer.

For example, to print a double-precision value in hexadecimal, use a format like '%bx'.

**2** The fpri nt f function is *vectorized* for the case when input matrix A is non-scalar. The format string is cycled through the elements of A (columnwise) until all the elements are used up. It is then cycled in a similar manner, without reinitializing, through any additional matrix arguments.

#### **Tables**

The following tables describe the non-alphanumeric characters found in format specification strings.

### **Escape Characters**

Character	Description
\n	New line
\t	Horizontal tab
\b	Backspace
\r	Carriage return
\f	Form feed
\\	Backslash
\" or "	Single quotation mark
%%	Percent character

Conversion characters specify the notation of the output.

## **Conversion Specifiers**

Specifier	Description
%с	Single character
%d	Decimal notation (signed)
%e	Exponential notation (using a lowercase e as in 3. 1415e+00)
%E	Exponential notation (using an uppercase E as in 3. 1415E+00)
%f	Fixed-point notation
%g	The more compact of %e or %f, as defined in [2]. Insignificant zeros do not print.
%G	Same as %g, but using an uppercase E
%o	Octal notation (unsigned)
%s	String of characters
%u	Decimal notation (unsigned)
% <b>x</b>	Hexadecimal notation (using lowercase letters a-f)
%X	Hexadecimal notation (using uppercase letters A–F)

Other characters can be inserted into the conversion specifier between the % and the conversion character.

## **Other Characters**

Character	Description	Example
A minus sign (–)	Left-justifies the converted argument in its field.	%–5. 2d
A plus sign (+)	Always prints a sign character (+ or -).	%+5. 2d
Zero (0)	Pad with zeros rather than spaces.	%05. 2d
Digits (field width)	A digit string specifying the minimum number of digits to be printed.	%6f
Digits (precision)	A digit string including a period (.) specifying the number of digits to be printed to the right of the decimal point.	%6. 2f

For more information about format strings, refer to the printf() and fprintf() routines in the documents listed in "References".

## **Examples**

### The statements

```
x = 0:.1:1;
y = [x; exp(x)];
fid = fopen('exp.txt','w');
fprintf(fid,'%6.2f %12.8f\n',y);
fclose(fid)
```

create a text file called exp. txt containing a short table of the exponential function:

```
0. 00 1. 00000000
0. 10 1. 10517092
...
1. 00 2. 71828183
```

#### The command

```
fprintf(\ 'A\ unit\ circle\ has\ circumference\ \%g.\ \ \ 'n'\ ,\ 2*pi)
```

### displays a line on the screen:

A unit circle has circumference 6.283186.

To insert a single quotation mark in a string, use two single quotation marks together. For example,

```
fprint(1, 'It''s Friday. \n')
```

displays on the screen:

```
It's Friday.
```

The commands

```
B = [8.8 \ 7.7; 8800 \ 7700]
fprintf(1, 'X is %6.2f meters or %8.3f mm\n', 9.9,9900, B)
```

display the lines:

```
X is 9.90 meters or 9900.000 mm
X is 8.80 meters or 8800.000 mm
X is 7.70 meters or 7700.000 mm
```

Explicitly convert MATLAB double-precision variables to integral values for use with an integral conversion specifier. For instance, to convert signed 32-bit data to hexadecimal format:

```
a = [6 \ 10 \ 14 \ 44];
fprintf('\%9X\n', a + (a<0)*2^32)
           A
           \mathbf{E}
          2C
```

#### See Also

fclose	Close one or more open files
ferror	Query MATLAB about errors in file input or output
fopen	Open a file or obtain information about open files
fscanf	Read formatted data from file
fseek	Set file position indicator
ftell	Get file position indicator

#### References

- [1] Kernighan, B.W. and D.M. Ritchie, The C Programming Language, Second Edition, Prentice-Hall, Inc., 1988.
- [2] ANSI specification X3.159-1989: "Programming Language C," ANSI, 1430 Broadway, New York, NY 10018.

Read binary data from file

**Syntax** 

[A, count] = fread(fid, size, precision)
[A, count] = fread(fid, size, precision, skip)

Description

[A, count] = fread(fid, size, precision) reads binary data from the specified file and writes it into matrix A. Optional output argument count returns the number of elements successfully read. fid is an integer file identifier obtained from fopen.

si ze is an optional argument that determines how much data is read. If si ze is not specified, fread reads to the end of the file. Valid options are:

n Reads n elements into a column vector.

inf Reads to the end of the file, resulting in a column vector containing the same number of elements as are in the file.

[m, n] Reads enough elements to fill an m-by-n matrix, filling in elements in column order, padding with zeros if the file is too small to fill the matrix.

If fread reaches the end of the file and the current input stream does not contain enough bits to write out a complete matrix element of the specified precision, fread pads the last byte or element with zero bits until the full value is obtained. If an error occurs, reading is done up to the last full value.

precision is a string representing the numeric precision of the values read, precision controls the number of bits read for each value and the interpretation of those bits as an integer, a floating-point value, or a character. The precision string may contain a positive integer repetition factor of the form 'n\*' which prepends one of the strings above, like '40\*uchar'. If precision is not specified, the default is 'uchar' (8-bit unsigned character) is assumed. See "Remarks" for more information.

[A, count] = fread(fi d, si ze, precision, ski p) includes an optional ski p argument that specifies the number of bytes to skip after each read. This is useful for extracting data in noncontiguous fields from fixed length records. If precision is a bit format like 'bitN' or 'ubitN', ski p is specified in bits.

#### Remarks

Numeric precisions can differ depending on how numbers are represented in your computer's architecture, as well as by the type of compiler used to produce executable code for your computer.

The tables below give C-compliant, platform-independent numeric precision string formats that you should use whenever you want your code to be portable.

For convenience, MATLAB accepts some C and Fortran data type equivalents for the MATLAB precisions listed. If you are a C or Fortran programmer, you may find it more convenient to use the names of the data types in the language with which you are most familiar.

MATLAB	C or Fortran	Interpretation
'char'	' char*1'	Character; 8 bits
'schar'	'signed char'	Signed character; 8 bits
'uchar'	'unsigned char'	Unsigned character; 8 bits
' i nt8'	'integer*1'	Integer; 8 bits
' i nt 16'	'integer*2'	Integer; 16 bits
' i nt 32'	'integer*4'	Integer; 32 bits
' i nt 64'	'integer*8'	Integer; 64 bits
' ui nt8'	'integer*1'	Unsigned integer; 8 bits
' ui nt 16'	'integer*2'	Unsigned integer; 16 bits
' ui nt32'	'integer*4'	Unsigned integer; 32 bits
' ui nt64'	'integer*8'	Unsigned integer; 64 bits
' fl oat 32'	' real *4'	Floating-point; 32 bits
' fl oat 64'	' real *8'	Floating-point; 64 bits

If you always work on the same platform and don't care about portability, these platform-dependent numeric precision string formats are also available:

MATLAB	C or Fortran	Interpretation
'short'	'short'	Integer; 16 bits
'int'	'int'	Integer; 32 bits
' l ong'	' l ong'	Integer; 32 or 64 bits
'ushort'	'usigned short'	Unsigned integer; 16 bits
' ui nt '	'unsigned int'	Unsigned integer; 32 bits
' ul ong'	'unsigned long'	Unsigned integer; 32 or 64 bits
' fl oat'	'float'	Floating-point; 32 bits
' doubl e'	' doubl e'	Floating-point; 64 bits

Two formats map to an input steam of bits rather than bytes:

MATLAB	C or Fortran	Interpretation
' bi tN'		Signed integer; N bits $(1 \le N \le 64)$
' ubi tN'		Unsigned integer; N bits $(1 \le N \le 64)$

## See Also

fclose	Close one or more open files
ferror	Query MATLAB about errors in file input or output
fopen	Open a file or obtain information about open files
fpri ntf	Write formatted data to file
fscanf	Read formatted data from file
fseek	Set file position indicator
ftell	Get file position indicator
fwrite	Write binary data from a MATLAB matrix to a file

Determine frequency spacing for frequency response

### **Syntax**

```
[f1, f2] = freqspace(n)
[f1, f2] = freqspace([m n])
[x1, y1] = freqspace(..., 'meshgrid')
f = freqspace(N)
f = freqspace(N, 'whole')
```

## Description

freqspace returns the implied frequency range for equally spaced frequency responses. freqspace is useful when creating desired frequency responses for various one- and two-dimensional applications.

[f1, f2] = freqspace(n) returns the two-dimensional frequency vectors f1 and f2 for an n-by-n matrix.

For n odd, both f1 and f2 are [-n+1:2:n-1]/n.

For n even, both f1 and f2 are [-n: 2: n-2]/n.

[f1, f2] = freqspace([m n]) returns the two-dimensional frequency vectors f1 and f2 for an m-by-n matrix.

```
[x1, y1] = freqspace(..., 'meshgrid') is equivalent to
[f1, f2] = freqspace(...);
[x1, y1] = meshgrid(f1, f2);
```

f = freqspace(N) returns the one-dimensional frequency vector f assuming N evenly spaced points around the unit circle. For N even or odd, f is (0: 2/N: 1). For N even, freqspace therefore returns (N+2)/2 points. For N odd, it returns (N+1)/2 points.

f = freqspace(N, 'whole') returns N evenly spaced points around the whole unit circle. In this case, f is 0: 2/N: 2\*(N-1)/N.

### See Also

meshgri d

Generate X and Y matrices for three-dimensional plots

# frewind

**Purpose** Rewind an open file

Syntax frewind(fid)

**Description** frewind(fid) sets the file position indicator to the beginning of the file speci-

fied by fid, an integer file identifier obtained from fopen.

**Remarks** Rewinding a fid associated with a tape device may not work even though

frewind does not generate an error message.

**See Also** fclose Close one or more open files

ferror Query MATLAB about errors in file input or output fopen Open a file or obtain information about open files

fprintf Write formatted data to file fread Read binary data from file fscanf Read formatted data from file fseek Set file position indicator ftell Get file position indicator

fwrite Write binary data from a MATLAB matrix to a file

Read formatted data from file

Syntax

A = fscanf(fid, format)

[A, count] = fscanf(fid, format, size)

**Description** 

A = fscanf(fid, format) reads all the data from the file specified by fid, converts it according to the specified format string, and returns it in matrix A. Argument fid is an integer file identifier obtained from fopen. format is a string specifying the format of the data to be read. See "Remarks" for details.

[A, count] = fscanf(fid, format, size) reads the amount of data specified by size, converts it according to the specified format string, and returns it along with a count of elements successfully read. size is an argument that determines how much data is read. Valid options are:

n Read n elements into a column vector.

inf Read to the end of the file, resulting in a column vector containing the same number of elements as are in the file.

[m, n] Read enough elements to fill an m-by-n matrix, filling the matrix in column order, n can be Inf, but not m.

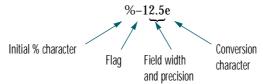
fscanf differs from its C language namesakes scanf() and fscanf() in an important respect — it is *vectorized* in order to return a matrix argument. The *format* string is cycled through the file until an end-of-file is reached or the amount of data specified by size is read in.

Remarks

When MATLAB reads a specified file, it attempts to match the data in the file to the format string. If a match occurs, the data is written into the matrix in column order. If a partial match occurs, only the matching data is written to the matrix, and the read operation stops.

The *format* string consists of ordinary characters and/or conversion specifications. Conversion specifications indicate the type of data to be matched and

involve the character %, optional width fields, and conversion characters, organized as shown below:



Add one or more of these characters between the % and the conversion character:

An asterisk (\*) Skip over the matched value, if the value is matched but

not stored in the output matrix.

A digit string Maximum field width.

A letter The size of the receiving object; for example, h for short as

in %hd for a short integer, or 1 for long as in %l d for a long

integer or %l g for a double floating-point number.

Valid conversion characters are:

%c Sequence of characters; number specified by field width

%d Decimal numbers

%e, %f, %g Floating-point numbers

%i Signed integer

%o Signed octal integer

%s A series of non-white-space characters

%u Signed decimal integer

%x Signed hexadecimal integer

[...] Sequence of characters (scanlist)

If %s is used, an element read may use several MATLAB matrix elements, each holding one character. Use %c to read space characters; the format %s skips all white space.

Mixing character and numeric conversion specifications cause the resulting matrix to be numeric and any characters read to appear as their ASCII values, one character per MATLAB matrix element.

For more information about format strings, refer to the scanf() and fscanf() routines in a C language reference manual.

## **Examples**

The example in fprintf generates an ASCII text file called exp. txt that looks like:

```
0. 00 1. 00000000
0. 10 1. 10517092
...
1. 00 2. 71828183
```

Read this ASCII file back into a two-column MATLAB matrix:

```
fid = fopen('exp.txt');
a = fscanf(fid,'%g %g',[2 inf]) % It has two rows now.
a = a';
fclose(fid)
```

#### See Also

fclose	Close one or more open files
ferror	Query MATLAB about errors in file input or output
fopen	Open a file or obtain information about open files
fprintf	Write formatted data to file
fread	Read binary data from file
fseek	Set file position indicator
ftell	Get file position indicator
fwrite	Write binary data from a MATLAB matrix to a file

## fseek

**Purpose** Set file position indicator

**Syntax** status = fseek(fid, offset, origin)

**Description** status = fseek(fid, offset, origin) repositions the file position indicator

in the file with the given fid to the byte with the specified offset relative to

ori gi n.

**Arguments** fid An integer file identifier obtained from fopen.

offset A value that is interpreted as follows:

offset > 0 Move position indicator offset bytes toward the

end of the file.

offset = 0 Do not change position.

offset < 0 Move position indicator offset bytes toward the

beginning of the file.

*ori gi n* A string whose legal values are:

'bof' −1: Beginning of file.

'cof' 0: Current position in file.

'eof' 1: End of file.

status A returned value that is 0 if the fseek operation is successful and

-1 if it fails. If an error occurs, use the function ferror to get more

information about the nature of the error.

ftell Get file position indicator

**Purpose** Get file position indicator

**Syntax** position = ftell(fid)

**Description** position = ftell (fid) returns the location of the file position indicator for

the file specified by fid, an integer file identifier obtained from fopen. The position is a nonnegative integer specified in bytes from the beginning of the file. A returned value of -1 for position indicates that the query was unsuc-

cessful; use ferror to determine the nature of the error.

**See Also** fclose Close one or more open files

ferror Query MATLAB about errors in file input or output fopen Open a file or obtain information about open files

fprintf Write formatted data to file fread Read binary data from file fscanf Read formatted data from file Set file position indicator

fwrite Write binary data from a MATLAB matrix to a file

Convert sparse matrix to full matrix

Syntax

A = full(S)

Description

A = full(S) converts a sparse matrix S to full storage organization. If S is a full matrix, it is left unchanged. If A is full, i ssparse(A) is 0.

Remarks

Let X be an m-by-n matrix with nz = nnz(X) nonzero entries. Then full(X) requires space to store m\*n real numbers while sparse(X) requires space to store nz real numbers and (nz+n) integers.

On most computers, a real number requires twice as much storage as an integer. On such computers,  $\operatorname{sparse}(X)$  requires less storage than  $\operatorname{full}(X)$  if the density,  $\operatorname{nnz/prod}(\operatorname{size}(X))$ , is less than one third. Operations on sparse matrices, however, require more execution time per element than those on full matrices, so density should be considerably less than two-thirds before sparse storage is used.

## **Examples**

Here is an example of a sparse matrix with a density of about two-thirds. sparse(S) and full(S) require about the same number of bytes of storage.

See Also

sparse

Create sparse matrix

**Purpose** Build full filename from parts

**Syntax** fullfile(dir1, dir2, ..., filename)

**Description** full file (dir1, dir2, ..., filename) builds a full filename from the directo-

ries and filename specified. This is conceptually equivalent to

f = [dir1 dirsep dir2 dirsep ... dirsep filename]

except that care is taken to handle the cases when the directories begin or end with a directory separator. Specify the filename as ' ' to build a pathname from

parts. On VMS, care is taken to handle the cases involving [or].

**Example** fullfile(matlabroot, 'tool box/matlab/general/Contents. m') and

fullfile(matlabroot, 'tool box', 'matlab', 'general', 'Contents.m')

produce the same result on UNIX, but only the second one works on all plat-

forms.

**Function M-files** 

### Description

You add new functions to MATLAB's vocabulary by expressing them in terms of existing functions. The existing commands and functions that compose the new function reside in a text file called an *M-file*.

M-files can be either *scripts* or *functions*. Scripts are simply files containing a sequence of MATLAB statements. Functions make use of their own local variables and accept input arguments.

The name of an M-file begins with an alphabetic character, and has a filename extension of .m. The M-file name, less its extension, is what MATLAB searches for when you try to use the script or function.

A line at the top of a function M-file contains the syntax definition. The name of a function, as defined in the first line of the M-file, should be the same as the name of the file without the . m extension. For example, the existence of a file on disk called stat.m with

```
function [mean, stdev] = stat(x)

n = length(x);

mean = sum(x)/n;

stdev = sqrt(sum((x-mean).^2/n));
```

defines a new function called stat that calculates the mean and standard deviation of a vector. The variables within the body of the function are all local variables.

A *subfunction*, visible only to the other functions in the same file, is created by defining a new function with the function keyword after the body of the preceding function or subfunction. For example, avg is a subfunction within the file stat. m:

```
function [mean, stdev] = stat(x)
n = length(x);
mean = avg(x, n);
stdev = sqrt(sum((x-avg(x, n)).^2)/n);
function mean = avg(x, n)
mean = sum(x)/n;
```

Subfunctions are not visible outside the file where they are defined. Functions normally return when the end of the function is reached. Use a return statement to force an early return.

When MATLAB does not recognize a function by name, it searches for a file of the same name on disk. If the function is found, MATLAB compiles it into memory for subsequent use. In general, if you input the name of something to MATLAB, the MATLAB interpreter:

- 1 Checks to see if the name is a variable.
- **2** Checks to see if the name is an internal function (ei g, si n)that was not overloaded.
- **3** Checks to see if the name is a local function (local in sense of multifunction file).
- **4** Checks to see if the name is a function in a private directory.
- **5** Locates any and all occurrences of function in method directories and on the path. Order is of no importance.

At execution MATLAB:

- **6** Checks to see if the name is wired to a specific function (2, 3, & 4 above)
- 7 Uses precedence rules to determine which instance from 5 above to call (we may default to an internal MATLAB function). Constructors have higher precedence than anything else.

When you call an M-file function from the command line or from within another M-file, MATLAB parses the function and stores it in memory. The parsed function remains in memory until cleared with the clear command or you quit MATLAB. The pcode command performs the parsing step and stores the result on the disk as a P-file to be loaded later.

#### See Also

nargi n	Number of function arguments (input)
nargout	Number of function arguments(output)
pcode	Create preparsed pseudocode file (P-file)

varargi n Pass or return variable numbers of arguments (input)
varargout Pass or return variable numbers of arguments (output)
what Directory listing of M-files, MAT-files, and MEX-files

Evaluate functions of a matrix

### Syntax

```
Y = funm(X, 'function')
[Y, esterr] = funm(X, 'function')
```

### Description

Y = funm(X, 'function') evaluates function using Parlett's method [1]. X must be a square matrix, and function any element-wise function.

The commands funm(X, 'sqrt') and funm(X, 'log') are equivalent to the commands sqrtm(X) and logm(X). The commands funm(X, 'exp') and expm(X) compute the same function, but by different algorithms. expm(X) is preferred.

[Y, esterr] = funm(X, 'function') does not print any message, but returns a very rough estimate of the relative error in the computer result. If X is symmetric or Hermitian, then its Schur form is diagonal, and funm is able to produce an accurate result.

## **Examples**

The statements

```
S = funm(X, 'sin');

C = funm(X, 'cos');
```

produce the same results to within roundoff error as

```
E = expm(i*X);
C = real(E);
S = i mag(E);
```

In either case, the results satisfy S\*S+C\*C = I, where I = eye(size(X)).

## **Algorithm**

The matrix functions are evaluated using Parlett's algorithm, which is described in [1]. The algorithm uses the Schur factorization of the matrix and may give poor results or break down completely when the matrix has repeated eigenvalues. A warning message is printed when the results may be inaccurate.

### See Also

expm	Matrix exponential
logm	Matrix logarithm
sqrtm	Matrix square root

## References

[1] Golub, G. H. and C. F. Van Loan, *Matrix Computation*, Johns Hopkins University Press, 1983, p. 384.

[2] Moler, C. B. and C. F. Van Loan, "Nineteen Dubious Ways to Compute the Exponential of a Matrix," *SIAM Review 20*, 1979, pp. 801-836.

## **fwrite**

Purpose

Write binary data to a file

**Syntax** 

count = fwrite(fid, A, precision)

count = fwrite(fid, A, precision, skip)

Description

count = fwrite(fid, A, precision) writes the elements of matrix A to the specified file, translating MATLAB values to the specified numeric precision. (See "Remarks" for more information.)

The data are written to the file in column order, and a count is kept of the number of elements written successfully. Argument fid is an integer file identifier obtained from fopen.

count = fwrite(fid, A, precision, skip) includes an optional skip argument that specifies the number of bytes to skip before each write. This is useful for inserting data into noncontiguous fields in fixed-length records. If precision is a bit format like 'bitN' or 'ubitN', skip is specified in bits.

Remarks

Numeric precisions can differ depending on how numbers are represented in your computer's architecture, as well as by the type of compiler used to produce executable code for your computer.

The tables below give C-compliant, platform-independent numeric precision string formats that you should use whenever you want your code to be portable.

For convenience, MATLAB accepts some C and Fortran data type equivalents for the MATLAB precisions listed. If you are a C or Fortran programmer, you may find it more convenient to use the names of the data types in the language with which you are most familiar.

MATLAB	C or Fortran	Interpretation
'char'	' char*1'	Character; 8 bits
'schar'	'signed char'	Signed character; 8 bits
'uchar'	'unsigned char'	Unsigned character; 8 bits
' i nt8'	'integer*1'	Integer; 8 bits
' i nt 16'	'integer*2'	Integer; 16 bits
' i nt 32'	'integer*4'	Integer; 32 bits
' i nt 64'	'integer*8'	Integer; 64 bits
' ui nt8'	'integer*1'	Unsigned integer; 8 bits
' ui nt 16'	'integer*2'	Unsigned integer; 16 bits
' ui nt32'	' i nt eger *4'	Unsigned integer; 32 bits
' ui nt64'	'integer*8'	Unsigned integer; 64 bits
' fl oat 32'	' real *4'	Floating-point; 32 bits
' fl oat 64'	' real *8'	Floating-point; 64 bits

If you always work on the same platform and don't care about portability, these platform-dependent numeric precision string formats are also available:

MATLAB	C or Fortran	Interpretation
'short'	'short'	Integer; 16 bits
'int'	'int'	Integer; 32 bits
' l ong'	' l ong'	Integer; 32 or 64 bits
'ushort'	'usigned short'	Unsigned integer; 16 bits
' ui nt '	'unsigned int'	Unsigned integer; 32 bits
' ul ong'	'unsigned long'	Unsigned integer; 32 or 64 bits
' fl oat'	'float'	Floating-point; 32 bits
' doubl e'	' doubl e'	Floating-point; 64 bits

Two formats map to an input steam of bits rather than bytes:

MATLAB	C or Fortran	Interpretation
' bi tN'		Signed integer; N bits $(1 \le N \le 64)$
' ubi t N'		Unsigned integer; N bits $(1 \le N \le 64)$

# **Examples**

```
fid = fopen('magic5.bin','wb');
fwrite(fid, magic(5),'integer*4')
```

creates a 100-byte binary file, containing the 25 elements of the 5-by-5 magic square, stored as 4-byte integers.

## See Also

fclose	Close one or more open files
ferror	Query MATLAB about errors in file input or output
fopen	Open a file or obtain information about open files
fprintf	Write formatted data to file
fread	Read binary data from file
fscanf	Read formatted data from file
fseek	Set file position indicator
ftell	Get file position indicator

#### **Purpose**

Zero of a function of one variable

#### Syntax

```
z = fzero('fun', x)
z = fzero('fun', x, tol)
z = fzero('fun', x, tol, trace)
z = fzero('fun', x, tol, trace, P1, P2, ...)
```

#### **Description**

fzero('fun', x) finds a zero of fun. fun is a string containing the name of a real-valued function of a single real variable. The value returned is near a point where fun changes sign, or NaN if the search fails.

fzero('fun', x) where x is a vector of length 2, assumes x is an interval where the sign of f(x(1)) differs from the sign of f(x(2)). An error occurs if this is not true. Calling fzero with an interval guarantees fzero will return a value near a point where fun changes sign.

fzero('fun', x) where x is a scalar value, uses x as a starting point. fzero looks for an interval containing a sign change for fun and containing x. If no such interval is found, NaN is returned. In this case, the search terminates when the search interval is expanded until an Inf, NaN, or complex value is found.

fzero('fun', x, tol) returns an answer accurate to within a relative error of tol.

z = fzero('fun', x, tol, trace) displays information at each iteration.

z = fzero('fun', x, tol, trace, P1, P2, ...) provides for additional arguments passed to the function fun(x, P1, P2, ...). Pass an empty matrix for tol or trace to use the default value, for example: fzero('fun', x, [], [], P1)

For the purposes of this command, zeros are considered to be points where the function actually crosses, not just touches, the *x*-axis.

## **Arguments**

fun	A string containing the name of a file in which an arbitrary
	function of one variable is defined.

X Your initial estimate of the *x*-coordinate of a zero of the function or an interval in which you think a zero is found.

tol The relative error tolerance. By default, tol is eps.

A nonzero value that causes the fzero command to display information at each iteration of its calculations.

P1, P2 Additional arguments passed to the function

## **Examples**

Calculate  $\pi$  by finding the zero of the sine function near 3.

To find the zero of cosi ne between 1 and 2:

Note that cos(1) and cos(2) differ in sign.

To find a zero of the function:

$$f(x) = x^3 - 2x - 5$$

write an M-file called f.m.

function 
$$y = f(x)$$
  
 $y = x. ^3-2*x-5;$ 

To find the zero near 2

Since this function is a polynomial, the statement  $roots([1\ 0\ -2\ -5])$  finds the same real zero, and a complex conjugate pair of zeros.

fzero('abs(x)+1', 1) returns NaN since this function does not change sign anywhere on the real axis (and does not have a zero as well).

#### **Algorithm**

The fzero command is an M-file. The algorithm, which was originated by T. Dekker, uses a combination of bisection, secant, and inverse quadratic interpolation methods. An Algol 60 version, with some improvements, is given in [1]. A Fortran version, upon which the fzero M-file is based, is in [2].

#### Limitations

The fzero command defines a *zero* as a point where the function crosses the x-axis. Points where the function touches, but does not cross, the x-axis are not valid zeros. For example, y = x.  $^2$  is a parabola that touches the x-axis at (0,0). Since the function never crosses the x-axis, however, no zero is found. For functions with no valid zeros, fzero executes until Inf, NaN, or a complex value is detected.

#### See Also

eps Floating-point relative accuracy
fmin Minimize a function of one variable
roots Polynomial roots

#### References

[1] Brent, R., *Algorithms for Minimization Without Derivatives*, Prentice-Hall, 1973.

[2] Forsythe, G. E., M. A. Malcolm, and C. B. Moler, *Computer Methods for Mathematical Computations*, Prentice-Hall, 1976.

# gallery

**Purpose** Test matrices **Syntax**  $[A, B, C, \dots] = gallery('tmfun', P1, P2, \dots)$ a badly conditioned 3-by-3 matrix gallery(3) an interesting eigenvalue problem gallery(5) **Description** [A, B, C, ...] = gallery('tmfun', P1, P2, ...) returns the test matrices specified by string tmfun. tmfun is the name of a matrix family selected from the table below. P1, P2, . . . are input parameters required by the individual matrix family. The number of optional parameters P1, P2, . . . used in the calling syntax varies from matrix to matrix. The exact calling syntaxes are detailed in the individual matrix descriptions below. The gallery holds over fifty different test matrix functions useful for testing algorithms and other purposes.

Test Matrices				
cauchy	chebspec	chebvand	chow	
ci rcul	clement	compar	condex	
cycol	dorr	dramadah	fi edl er	
forsythe	frank	gearmat	grcar	
hanowa	house	i nvhess	i nvol	
i pj fact	j ordbl oc	kahan	kms	
kryl ov	l auchl i	lehmer	lesp	
lotkin	mi ni j	moler	neumann	
orthog	parter	pei	poi sson	
prol ate	rando	randhess	randsvd	
redheff	ri emann	ri s	rosser	
smoke	toeppd	tri di ag	triw	
vander	wathen	wi l k		

## cauchy—Cauchy matrix

C = gallery('cauchy', x, y) returns an n-by-n matrix, C(i, j) = 1/(x(i)+y(j)). Arguments x and y are vectors of length n. If you pass in scalars for x and y, they are interpreted as vectors 1: x and 1: y.

C = gallery('cauchy', x) returns the same as above with y = x. That is, the command returns C(i,j) = 1/(x(i)+x(j)).

Explicit formulas are known for the inverse and determinant of a Cauchy matrix. The determinant  $\det(C)$  is nonzero if x and y both have distinct elements. C is totally positive if  $0 < x(1) < \ldots < x(n)$  and  $0 < y(1) < \ldots < y(n)$ .

## chebspec—Chebyshev spectral differentiation matrix

C = gallery(' chebspec', n, switch) returns a Chebyshev spectral differentiation matrix of order n. Argument switch is a variable that determines the character of the output matrix. By default, switch = 0.

For  $swi\ tch = 0$  ("no boundary conditions"), C is nilpotent (C<sup>n</sup> = 0) and has the null vector ones (n, 1). The matrix C is similar to a Jordan block of size n with eigenvalue zero.

For switch = 1, C is nonsingular and well-conditioned, and its eigenvalues have negative real parts.

The eigenvector matrix V of the Chebyshev spectral differentiation matrix is ill-conditioned.

#### chebyand—Vandermonde-like matrix for the Chebyshev polynomials

C = gallery('chebvand', p) produces the (primal) Chebyshev Vandermonde matrix based on the vector of points p, which define where the Chebyshev polynomial is calculated.

C = gallery(' chebvand', m, p) where m is scalar, produces a rectangular version of the above, with m rows.

If p is a vector, then:  $C(i,j) = T_{i-1}(p(j))$  where  $T_{i-1}$  is the Chebyshev polynomial of degree i –1. If p is a scalar, then p equally spaced points on the interval [0,1] are used to calculate C.

## chow—Singular Toeplitz lower Hessenberg matrix

A = gallery('chow', n, alpha, delta) returns A such that A = H(alpha) + delta\*eye(n), where  $H_{i,j}(\alpha) = \alpha^{(i-j+1)}$ . Argument n is the order of the Chow matrix, while alpha and delta are scalars with default values 1 and 0, respectively.

H(al pha) has p = floor(n/2) eigenvalues that are equal to zero. The rest of the eigenvalues are equal to  $4*al pha*cos(k*pi/(n+2))^2$ , k=1:n-p.

#### circul—Circulant matrix

C = gallery('circul', v) returns the circulant matrix whose first row is the vector v.

A circulant matrix has the property that each row is obtained from the previous one by cyclically permuting the entries one step forward. It is a special Toeplitz matrix in which the diagonals "wrap around."

```
If v is a scalar, then C = gallery('circul', 1: v).
```

The eigensystem of C (n-by-n) is known explicitly: If t is an nth root of unity, then the inner product of v with  $w = [1 \ t \ t^2 \ ... \ t^n]$  is an eigenvalue of C and w(n: -1:1) is an eigenvector.

## clement—Tridiagonal matrix with zero diagonal entries

A = gallery('clement', n, sym) returns an n by n tridiagonal matrix with zeros on its main diagonal and known eigenvalues. It is singular if order n is odd. About 64 percent of the entries of the inverse are zero. The eigenvalues include plus and minus the numbers n-1, n-3, n-5, ..., as well as (for odd n) a final eigenvalue of 1 or 0.

Argument sym determines whether the Clement matrix is symmetric. For sym = 0 (the default) the matrix is nonsymmetric, while for sym = 1, it is symmetric.

## compar—Comparison matrices

A = gallery('compar', A, 1) returns A with each diagonal element replaced by its absolute value, and each off-diagonal element replaced by minus the absolute value of the largest element in absolute value in its row. However, if A is triangular compar(A, 1) is too.

```
gallery('compar', A) is diag(B) - tril(B, -1) - triu(B, 1), where B = abs(A). compar(A) is often denoted by M(A) in the literature.
```

gallery('compar', A, 0) is the same as compar(A).

#### condex—Counter-examples to matrix condition number estimators

A = gallery('condex', n, k, theta) returns a "counter-example" matrix to a condition estimator. It has order n and scalar parameter theta (default 100).

The matrix, its natural size, and the estimator to which it applies are specified by k as follows:

k = 1	4-by-4	LINPACK (rcond)
k = 2	3-by-3	LINPACK (rcond)
k = 3	arbitrary	LINPACK (roond) (independent of theta)
k = 4	$n \ge 4$	SONEST (Higham 1988) (default)

If n is not equal to the natural size of the matrix, then the matrix is padded out with an identity matrix to order n.

## cycol-Matrix whose columns repeat cyclically

A = gallery('cycol', [m n], k) returns an m-by-n matrix with cyclically repeating columns, where one "cycle" consists of randn(m, k). Thus, the rank of matrix A cannot exceed k. k must be a scalar.

Argument k defaults to round(n/4), and need not evenly divide n.

A = gallery('cycol', n, k), where n is a scalar, is the same as gallery('cycol', [n n], k).

## dorr—Diagonally dominant, ill-conditioned, tridiagonal matrix

[c,d,e]=gallery('dorr',n,theta) returns the vectors defining a row diagonally dominant, tridiagonal order n matrix that is ill-conditioned for small nonnegative values of theta. The default value of theta is 0.01. The Dorr matrix itself is the same as gallery('tridiag',c,d,e).

 $A = \mbox{\rm gallery('dorr', n, theta)}\ \ \mbox{\rm returns the matrix itself, rather than the defining vectors.}$ 

## dramadah—Matrix of zeros and ones whose inverse has large integer entries

A = gallery('dramadah', n, k) returns an n-by-n matrix of 0's and 1's for which  $mu(A) = norm(i\,nv(A), 'fro')$  is relatively large, although not necessarily maximal. An anti-Hadamard matrix A is a matrix with elements 0 or 1 for which mu(A) is maximal.

 $\boldsymbol{n}$  and  $\boldsymbol{k}$  must both be scalars. Argument  $\boldsymbol{k}$  determines the character of the output matrix:

- k=1 Default. A is Toeplitz, with  $abs(\det(A))=1$ , and  $mu(A)>c(1.75)^n$ , where c is a constant. The inverse of A has integer entries.
- k=2 A is upper triangular and Toeplitz. The inverse of A has integer entries.
- k=3 A has maximal determinant among lower Hessenberg (0,1) matrices.  $\det\left(A\right)=$  the nth Fibonacci number. A is Toeplitz. The eigenvalues have an interesting distribution in the complex plane.

#### fiedler—Symmetric matrix

A = gallery('fiedler', c), where c is a length n vector, returns the n-by-n symmetric matrix with elements abs(n(i)-n(j)). For scalar c, A = gallery('fiedler', 1: c).

Matrix A has a dominant positive eigenvalue and all the other eigenvalues are negative.

Explicit formulas for i nv(A) and det(A) are given in [Todd, J., *Basic Numerical Mathematics*, Vol. 2: Numerical Algebra, Birkhauser, Basel, and Academic Press, New York, 1977, p. 159] and attributed to Fiedler. These indicate that i nv(A) is tridiagonal except for nonzero (1, n) and (n, 1) elements.

## forsythe—Perturbed Jordan block

A = gallery('forsythe', n, alpha, lambda) returns the n-by-n matrix equal to the Jordan block with eigenvalue lambda, excepting that A(n, 1) = alpha. The default values of scalars alpha and lambda are sqrt(eps) and 0, respectively.

The characteristic polynomial of A is given by:

```
det(A-t*I) = (lambda-t)^N - alpha*(-1)^n.
```

#### frank—Matrix with ill-conditioned eigenvalues

F = gallery('frank', n, k) returns the Frank matrix of order n. It is upper Hessenberg with determinant 1. If k = 1, the elements are reflected about the anti-diagonal (1, n) - (n, 1). The eigenvalues of F may be obtained in terms of the zeros of the Hermite polynomials. They are positive and occur in reciprocal pairs; thus if n is odd, 1 is an eigenvalue. F has floor(n/2) ill-conditioned eigenvalues—the smaller ones.

## gearmat—Gear matrix

A = gallery('gearmat', n, i, j) returns the n-by-n matrix with ones on the sub- and super-diagonals, sign(i) in the (1, abs(i)) position, sign(j) in the (n, n+1-abs(j)) position, and zeros everywhere else. Arguments i and j default to n and -n, respectively.

Matrix A is singular, can have double and triple eigenvalues, and can be defective.

All eigenvalues are of the form  $2*\cos(a)$  and the eigenvectors are of the form  $[\sin n(w+a), \sin n(w+2a), \ldots, \sin n(w+Na)]$ , where a and w are given in Gear, C. W., "A Simple Set of Test Matrices for Eigenvalue Programs", *Math. Comp.*, Vol. 23 (1969), pp. 119–125.

## grcar—Toeplitz matrix with sensitive eigenvalues

A = gallery('grcar', n, k) returns an n-by-n Toeplitz matrix with -1s on the subdiagonal, 1s on the diagonal, and k superdiagonals of 1s. The default is k = 3. The eigenvalues are sensitive.

## hanowa—Matrix whose eigenvalues lie on a vertical line in the complex plane

A = gallery('hanowa', n, d) returns an n-by-n block 2-by-2 matrix of the form:

Argument n is an even integer n=2\*m. Matrix A has complex eigenvalues of the form  $d \pm k*i$ , for 1 <= k <= m. The default value of d is -1.

#### house—Householder matrix

[v, beta] = gallery('house', x) takes x, a scalar or n-element column vector, and returns v and beta such that eye(n, n) - beta\*v\*v' is a Householder matrix.

A Householder matrix H satisfies the relationship

```
H*x = -sign(x(1))*norm(x)*e1
```

where e1 is the first column of eye(n, n). Note that if x is complex, then sign(x) = exp(i\*arg(x)) (which equals x. /abs(x) when x is nonzero).

```
If x = 0, then y = 0 and beta = 1.
```

## invhess—Inverse of an upper Hessenberg matrix

A = gallery('invhess', x, y), where x is a length n vector and y a length n-1 vector, returns the matrix whose lower triangle agrees with that of ones(n, 1)\*x' and whose strict upper triangle agrees with that of [1 y]\*ones(1, n).

The matrix is nonsingular if  $x(1) \sim 0$  and  $x(i+1) \sim y(i)$  for all i, and its inverse is an upper Hessenberg matrix. Argument y defaults to -x(1:n-1).

If x is a scalar, invhess(x) is the same as invhess(1: x).

## invol—Involutory matrix

A = gallery('invol', n) returns an n-by-n involutory (A\*A = eye(n)) and ill-conditioned matrix. It is a diagonally scaled version of hilb(n).

B = (eye(n) - A)/2 and B = (eye(n) + A)/2 are idempotent (B\*B = B).

#### ipjfact—Hankel matrix with factorial elements

[A, d] = gallery('ipjfact', n, k) returns A, an n-by-n Hankel matrix, and d, the determinant of A, which is known explicitly. If k = 0 (the default), then the elements of A are A(i,j) = (i+j)! If k = 1, then the elements of A are A(i,j) = 1/(i+j).

Note that the inverse of A is also known explicitly.

## jordbloc-Jordan block

A = gallery('jordbloc', n, lambda) returns the n-by-n Jordan block with eigenvalue lambda. The default value for lambda is 1.

## kahan—Upper trapezoidal matrix

A = gallery('kahan', n, theta, pert) returns an upper trapezoidal matrix that has interesting properties regarding estimation of condition and rank.

If n is a two-element vector, then A is n(1)-by-n(2); otherwise, A is n-by-n. The useful range of theta is 0 < theta < pi, with a default value of 1.2.

To ensure that the QR factorization with column pivoting does not interchange columns in the presence of rounding errors, the diagonal is perturbed by pert\*eps\*diag([n: -1:1]). The default pert is 25, which ensures no interchanges for gallery('kahan', n) up to at least n = 90 in IEEE arithmetic.

## kms—Kac-Murdock-Szego Toeplitz matrix

A = gallery('kms', n, rho) returns the n-by-n Kac-Murdock-Szego Toeplitz matrix such that  $A(i,j) = rho^{(abs(i-j))}$ , for real rho.

For complex rho, the same formula holds except that elements below the diagonal are conjugated. rho defaults to 0.5.

The KMS matrix A has these properties:

- An LDL' factorization with L = i nv(tri w(n, -rho, 1)'), and  $D(i, i) = (1-abs(\text{rho})^2) *eye(n)$ , except D(1, 1) = 1.
- Positive definite if and only if 0 < abs(rho) < 1.
- The inverse i nv(A) is tridiagonal.

#### krylov—Krylov matrix

```
B = \text{gallery('krylov', A, x, j)} \text{ returns the Krylov matrix}[x, Ax, A^2x, \dots, A^{(j-1)}x]
```

where A is an n-by-n matrix and x is a length n vector. The defaults are x = ones(n, 1), and j = n.

B = gallery('krylov', n) is the same as gallery('krylov', (randn(n)).

#### lauchli—Rectangular matrix

```
A = gallery('lauchli', n, mu) returns the (n+1)-by-n matrix [ones(1, n); mu*eye(n)]
```

The Lauchli matrix is a well-known example in least squares and other problems that indicates the dangers of forming A'\*A. Argument mu defaults to sqrt(eps).

## lehmer—Symmetric positive definite matrix

A = gallery('lehmer', n) returns the symmetric positive definite n-by-n matrix such that A(i,j) = i/j for j >= i.

The Lehmer matrix A has these properties:

- A is totally nonnegative.
- The inverse i nv(A) is tridiagonal and explicitly known.
- The order  $n \le cond(A) \le 4*n*n$ .

## lesp—Tridiagonal matrix with real, sensitive eigenvalues

A = gallery('lesp', n) returns an n-by-n matrix whose eigenvalues are real and smoothly distributed in the interval approximately [-2\*N-3.5, -4.5].

The sensitivities of the eigenvalues increase exponentially as the eigenvalues grow more negative. The matrix is similar to the symmetric tridiagonal matrix with the same diagonal entries and with off-diagonal entries 1, via a similarity transformation with D = diag(1!, 2!, ..., n!).

#### lotkin—Lotkin matrix

A = gallery('lotkin', n) returns the Hilbert matrix with its first row altered to all ones. The Lotkin matrix A is nonsymmetric, ill-conditioned, and has many negative eigenvalues of small magnitude. Its inverse has integer entries and is known explicitly.

#### minij—Symmetric positive definite matrix

A = gallery('minij', n) returns the n-by-n symmetric positive definite matrix with A(i,j) = min(i,j).

The mi ni j matrix has these properties:

- The inverse i nv(A) is tridiagonal and equal to –1 times the second difference matrix, except its (n, n) element is 1.
- Givens' matrix, 2\*A-ones(si ze(A)), has tridiagonal inverse and eigenvalues
   0.5\*sec((2\*r-1)\*pi/(4\*n))^2, where r=1:n.
- (n+1)\*ones(size(A))-A has elements that are max(i,j) and a tridiagonal inverse.

## moler—Symmetric positive definite matrix

A = gallery('moler', n, alpha) returns the symmetric positive definite n-by-n matrix U'\*U, where U = triw(n, alpha).

For the default al pha = -1, A(i,j) = mi n(i,j) -2, and A(i,i) = i. One of the eigenvalues of A is small.

#### neumann—Singular matrix from the discrete Neumann problem (sparse)

C = gallery(' neumann', n) returns the singular, row-diagonally dominant matrix resulting from discretizing the Neumann problem with the usual five-point operator on a regular mesh. Argument n is a perfect square integer  $n = m^2$  or a two-element vector. C is sparse and has a one-dimensional null space with null vector ones (n, 1).

## orthog—Orthogonal and nearly orthogonal matrices

Q = gallery('orthog', n, k) returns the kth type of matrix of order n, where k>0 selects exactly orthogonal matrices, and k<0 selects diagonal scalings of orthogonal matrices. Available types are:

- $\begin{array}{lll} k = 1 & Q(i\,,j\,) = sqrt(2/(n+1)) * sin(i*j*pi/(n+1)) \\ & Symmetric\ eigenvector\ matrix\ for\ second\ difference\ matrix.\ This is\ the\ default. \end{array}$
- k = 2 Q(i,j) = 2/(sqrt(2\*n+1)) \* sin(2\*i\*j\*pi/(2\*n+1))Symmetric.
- k=3  $Q(r,s)=\exp(2*pi*i*(r-1)*(s-1)/n)$  / sqrt(n) Unitary, the Fourier matrix. Q^4 is the identity. This is essentially the same matrix as fft(eye(n))/sqrt(n)!
- k = 4 Helmert matrix: a permutation of a lower Hessenberg matrix, whose first row is ones(1: n) /sqrt(n).
- $\begin{array}{lll} k=5 & Q(i\,,j\,) = si\,n(2*pi\,*(i\,-1)\,*(j\,-1)\,/n) \ + \\ & \cos(2*pi\,*(i\,-1)\,*(j\,-1)\,/n) \\ & Symmetric\ matrix\ arising\ in\ the\ Hartley\ transform. \end{array}$
- $\begin{array}{ll} k = -1 & Q(i\,,j\,) = cos((i\,-1)\,*(j\,-1)\,*pi\,/(n\!-\!1)) \\ & Chebyshev\ Vandermonde-like\ matrix,\ based\ on\ extrema\ of\ T(n\!-\!1)\,. \end{array}$

## parter—Toeplitz matrix with singular values near pi

C = gallery('parter', n) returns the matrix C such that C(i,j) = 1/(i-j+0.5).

 $\mathtt{C}$  is a Cauchy matrix and a Toeplitz matrix. Most of the singular values of  $\mathtt{C}$  are very close to  $\mathtt{pi}$  .

#### pei—Pei matrix

A = gallery('pei', n, alpha), where alpha is a scalar, returns the symmetric matrix alpha\*eye(n) + ones(n). The default for alpha is 1. The matrix is singular for alpha equal to either 0 or -n.

## poisson—Block tridiagonal matrix from Poisson's equation (sparse)

A = gallery('poisson', n) returns the block tridiagonal (sparse) matrix of order  $n^2$  resulting from discretizing Poisson's equation with the 5-point operator on an n-by-n mesh.

## prolate—Symmetric, ill-conditioned Toeplitz matrix

A = gallery('prolate', n, w) returns the n-by-n prolate matrix with parameter w. It is a symmetric Toeplitz matrix.

If 0 < w < 0.5 then A is positive definite

- The eigenvalues of A are distinct, lie in (0, 1), and tend to cluster around 0 and 1.
- The default value of w is 0.25.

## randhess—Random, orthogonal upper Hessenberg matrix

H = gallery('randhess', n) returns an n-by-n real, random, orthogonal upper Hessenberg matrix.

H = gallery('randhess', x) if x is an arbitrary, real, length n vector with n > 1, constructs H nonrandomly using the elements of x as parameters.

Matrix II is constructed via a product of n-1 Givens rotations.

#### rando—Random matrix composed of elements -1, 0 or 1

A = gallery('rando', n, k) returns a random n-by-n matrix with elements from one of the following discrete distributions:

```
k=1   A(i,j)=0 or 1 with equal probability (default) 
 k=2   A(i,j)=-1 or 1 with equal probability 
 k=3   A(i,j)=-1, 0 or 1 with equal probability
```

Argument n may be a two-element vector, in which case the matrix is n(1)-by-n(2).

## randsvd—Random matrix with preassigned singular values

A = gallery('randsvd', n, kappa, mode, kl, ku) returns a banded (multidiagonal) random matrix of order n with cond(A) = kappa and singular values from the distribution mode. If n is a two-element vector, A is n(1)-by-n(2).

Arguments kl and ku specify the number of lower and upper off-diagonals, respectively, in A. If they are omitted, a full matrix is produced. If only kl is present, ku defaults to kl.

## Distribution mode may be:

- 1 One large singular value
- 2 One small singular value
- 3 Geometrically distributed singular values (default)
- 4 Arithmetically distributed singular values

- 1 One large singular value
- 5 Random singular values with uniformly distributed logarithm
- If mode is -1, -2, -3, -4, or -5, then randsvd treats mode as abs(mode), except that in the original matrix of singular values the order of the diagonal entries is reversed: small to large instead of large to small.

Condition number kappa defaults to sqrt(1/eps). In the special case where kappa < 0, A is a random, full, symmetric, positive definite matrix with cond(A) = -kappa and eigenvalues distributed according to mode. Arguments kl and ku, if present, are ignored.

#### redheff—Redheffer's matrix of 1s and 0s

A = gallery('redheff', n) returns an n-by-n matrix of 0's and 1's defined by A(i,j) = 1, if j = 1 or if i divides j, and A(i,j) = 0 otherwise.

The Redheffer matrix has these properties:

- (n-floor(log2(n)))-1 eigenvalues equal to 1
- A real eigenvalue (the spectral radius) approximately sqrt (n)
- A negative eigenvalue approximately -sqrt(n)
- The remaining eigenvalues are provably "small."
- The Riemann hypothesis is true if and only if  $\det(A) = O(n^{(1/2+epsilon)})$  for every epsilon > 0.

Barrett and Jarvis conjecture that "the small eigenvalues all lie inside the unit circle abs(Z) = 1," and a proof of this conjecture, together with a proof that some eigenvalue tends to zero as n tends to infinity, would yield a new proof of the prime number theorem.

## riemann—Matrix associated with the Riemann hypothesis

A = gallery('riemann', n) returns an n-by-n matrix for which the Riemann hypothesis is true if and only if  $\det(A) = O(n! n^{(-1/2 + epsilon)})$  for every epsilon > 0.

The Riemann matrix is defined by:

```
A = B(2: n+1, 2: n+1)
```

where B(i,j) = i-1 if i divides j, and B(i,j) = -1 otherwise.

The Riemann matrix has these properties:

- Each eigenvalue e(i) satisfies abs(e(i)) <= m-1/m, where m = n+1.
- $i \le e(i) \le i+1$  with at most m-sqrt(m) exceptions.
- All integers in the interval (m/3, m/2] are eigenvalues.

#### ris—Symmetric Hankel matrix

A = gallery('ris', n) returns a symmetric n-by-n Hankel matrix with elements

$$A(i, j) = 0.5/(n-i-j+1.5)$$

The eigenvalues of A cluster around  $\pi/2$  and  $-\pi/2$ . This matrix was invented by F.N. Ris.

## rosser—Classic symmetric eigenvalue test matrix

A = rosser returns the Rosser matrix. This matrix was a challenge for many matrix eigenvalue algorithms. But the Francis QR algorithm, as perfected by Wilkinson and implemented in EISPACK and MATLAB, has no trouble with it. The matrix is 8-by-8 with integer elements. It has:

- A double eigenvalue
- Three nearly equal eigenvalues
- Dominant eigenvalues of opposite sign
- · A zero eigenvalue
- A small, nonzero eigenvalue

## smoke—Complex matrix with a 'smoke ring' pseudospectrum

A = gallery('smoke', n) returns an n-by-n matrix with 1's on the superdiagonal, 1 in the (n, 1) position, and powers of roots of unity along the diagonal.

A = gallery('smoke', n, 1) returns the same except that element A(n, 1) is zero.

The eigenvalues of smoke(n, 1) are the nth roots of unity; those of smoke(n) are the nth roots of unity times  $2^{(1/n)}$ .

#### toeppd—Symmetric positive definite Toeplitz matrix

A = gallery('toeppd', n, m, w, theta) returns an n-by-n symmetric, positive semi-definite (SPD) Toeplitz matrix composed of the sum of m rank 2 (or, for certain theta, rank 1) SPD Toeplitz matrices. Specifically,

```
T = w(1)*T(theta(1)) + ... + w(m)*T(theta(m)) where T(theta(k)) has (i,j) element cos(2*pi*theta(k)*(i-j)).
By default: m = n, w = rand(m, 1), and theta = rand(m, 1).
```

## toeppen—Pentadiagonal Toeplitz matrix (sparse)

P = gallery('toeppen', n, a, b, c, d, e) returns the n-by-n sparse, pentadiagonal Toeplitz matrix with the diagonals: P(3, 1) = a, P(2, 1) = b, P(1, 1) = c, P(1, 2) = d, and P(1, 3) = e, where a, b, c, d, and e are scalars.

By default, (a, b, c, d, e) = (1, -10, 0, 10, 1), yielding a matrix of Rutishauser. This matrix has eigenvalues lying approximately on the line segment 2\*cos(2\*t) + 20\*i\*sin(t).

## tridiag—Tridiagonal matrix (sparse)

A = gallery('tri di ag', c, d, e) returns the tridiagonal matrix with subdiagonal c, diagonal d, and superdiagonal e. Vectors c and e must have l ength(d) - 1.

A = gallery('tridiag', n, c, d, e), where c, d, and e are all scalars, yields the Toeplitz tridiagonal matrix of order n with subdiagonal elements c, diagonal elements d, and superdiagonal elements e. This matrix has eigenvalues

```
d + 2*sqrt(c*e)*cos(k*pi/(n+1))
where k = 1: n. (see [1].)
```

A = gallery('tridiag', n) is the same as

A = gallery('tridiag', n, -1, 2, -1), which is a symmetric positive definite M-matrix (the negative of the second difference matrix).

#### triw—Upper triangular matrix discussed by Wilkinson and others

A = gallery('triw', n, alpha, k) returns the upper triangular matrix with ones on the diagonal and alphas on the first k >= 0 superdiagonals.

Order n may be a 2-vector, in which case the matrix is n(1)-by-n(2) and upper trapezoidal.

Ostrowski ["On the Spectrum of a One-parametric Family of Matrices, *J. Reine Angew. Math.*, 1954] shows that

```
cond(gallery('triw', n, 2)) = cot(pi/(4*n))^2,
```

and, for large abs(al pha), cond(gallery('triw', n, al pha)) is approximately abs(al pha)  $^n*\sin(pi/(4*n-2))$ .

Adding  $-2^{(2-n)}$  to the (n, 1) element makes triw(n) singular, as does adding  $-2^{(1-n)}$  to all the elements in the first column.

#### vander—Vandermonde matrix

A = gallery('vander', c) returns the Vandermonde matrix whose second to last column is c. The j th column of a Vandermonde matrix is given by  $A(:,j) = C^{\wedge}(n-j)$ .

## wathen—Finite element matrix (sparse, random entries)

A = gallery('wathen', nx, ny) returns a sparse, random, n-by-n finite element matrix where

```
n = 3*nx*ny + 2*nx + 2*ny + 1.
```

Matrix A is precisely the "consistent mass matrix" for a regular nx-by-ny grid of 8-node (serendipity) elements in two dimensions. A is symmetric, positive definite for any (positive) values of the "density,"  ${\rm rho}({\rm nx,\,ny})$ , which is chosen randomly in this routine.

A = gallery('wathen', nx, ny, 1) returns a diagonally scaled matrix such that

$$0.25 \le eig(inv(D)*A) \le 4.5$$

where  $D = di \, ag(di \, ag(A))$  for any positive integers nx and ny and any densities rho(nx, ny).

## wilk—Various matrices devised or discussed by Wilkinson

[A, b] = gallery('wilk', n) returns a different matrix or linear system depending on the value of n:

n	MATLAB Code	Result
n = 3	[A, b] = gallery('wilk', 3)	Upper triangular system Ux=b illustrating inaccurate solution.
n = 4	[A, b] = gallery('wilk', 4)	Lower triangular system Lx=b, ill-conditioned.
n = 5	A = gallery('wilk',5)	hilb(6) (1: 5, 2: 6) *1.8144. A symmetric positive definite matrix.
n = 21	A = gallery('wilk', 21)	W21+, tridiagonal matrix. Eigenvalue problem.

See Also hadamard Hadamard matrix

hilb Hilbert matrix

i nvhi l b Inverse of the Hilbert matrix

magi c Magic square

wilkinson's eigenvalue test matrix

#### References

The MATLAB gallery of test matrices is based upon the work of Nicholas J. Higham at the Department of Mathematics, University of Manchester, Manchester, England. Additional detail on these matrices is documented in *The Test Matrix Toolbox for MATLAB (Version 3.0)* by N. J. Higham, September, 1995. To obtain this report in pdf format, enter the doc command at the MATLAB prompt and select the item Rel ated Papers > Test Matrix Tool box under the Full Documentation Set entry on the Help Desk main screen. This report is also available via anonymous ftp from The MathWorks at /pub/contrib/linalg/testmatrix/testmatrix.ps or World Wide Web (ftp://ftp.ma.man.ac.uk/pub/narep or http://www.ma.man.ac.uk/MCCM/MCCM html). Further background may be found in the book *Accuracy and Stability of Numerical Algorithms*, Nicholas J. Higham, SIAM, 1996.

# gamma, gammainc, gammain

**Purpose** 

Gamma functions

**Syntax** 

Y = gamma (A) Gamma function

Y = gammai nc(X, A) Incomplete gamma function Y = gammal n(A) Logarithm of gamma function

**Definition** 

The gamma function is defined by the integral:

$$\Gamma(a) = \int_{0}^{\infty} e^{-t} t^{a-1} dt$$

The gamma function interpolates the factorial function. For integer n:

$$gamma(n+1) = n! = prod(1:n)$$

The incomplete gamma function is:

$$P(x, a) = \frac{1}{\Gamma(a)} \int_0^x e^{-t} t^{a-1} dt$$

Description

Y = gamma(A) returns the gamma function at the elements of A. A must be real.

 $Y = \text{gammai} \, \text{nc}(X, A)$  returns the incomplete gamma function of corresponding elements of X and A. Arguments X and A must be real and the same size (or either can be scalar).

 $Y = gammal\,n(A)$  returns the logarithm of the gamma function,  $gammal\,n(A) = l\,og(gamma(A))$ . The gammal n command avoids the underflow and overflow that may occur if it is computed directly using  $l\,og(gamma(A))$ .

**Algorithm** 

The computations of gamma and gammal n are based on algorithms outlined in [1]. Several different minimax rational approximations are used depending

# gamma, gammainc, gammain

upon the value of A. Computation of the incomplete gamma function is based on the algorithm in [2].

# gamma, gammainc, gammain

#### References

[1] Cody, J., *An Overview of Software Development for Special Functions*, Lecture Notes in Mathematics, 506, Numerical Analysis Dundee, G. A. Watson (ed.), Springer Verlag, Berlin, 1976.

[2] Abramowitz, M. and I.A. Stegun, *Handbook of Mathematical Functions*, National Bureau of Standards, Applied Math. Series #55, Dover Publications, 1965, sec. 6.5.

**Purpose** 

Greatest common divisor

Syntax

$$G = \gcd(A, B)$$
  
 $[G, C, D] = \gcd(A, B)$ 

**Description** 

 $G = \gcd(A,B)$  returns an array containing the greatest common divisors of the corresponding elements of integer arrays A and B. By convention,  $\gcd(0,0)$  returns a value of 0; all other inputs return positive integers for G.

[G, C, D] = gcd(A, B) returns both the greatest common divisor array G, and the arrays C and D, which satisfy the equation:  $A(i) \cdot *C(i) + B(i) \cdot *D(i) = G(i)$ . These are useful for solving Diophantine equations and computing elementary Hermite transformations.

**Examples** 

The first example involves elementary Hermite transformations.

For any two integers a and b there is a 2-by-2 matrix E with integer entries and determinant = 1 (a *unimodular* matrix) such that:

$$E * [a; b] = [g, 0],$$

where g is the greatest common divisor of a and b as returned by the command [g, c, d] = gcd(a, b).

The matrix E equals:

$$\begin{array}{cc} c & d \\ -b/g & a/g \end{array}$$

In the case where a = 2 and b = 4:

So that:

$$\begin{array}{ccc} E & = & & & \\ & 1 & & 0 \\ & -2 & & 1 \end{array}$$

In the next example, we solve for x and y in the Diophantine equation 30x + 56y = 8.

By the definition, for scalars  $\boldsymbol{c}$  and  $\boldsymbol{d}$ :

$$30(-13) + 56(7) = 2,$$

Multiplying through by 8/2:

$$30(-13*4) + 56(7*4) = 8$$

Comparing this to the original equation, a solution can be read by inspection:

$$x = (-13*4) = -52; y = (7*4) = 28$$

See Also

 $l\,cm$ 

Least common multiple

References

[1] Knuth, Donald, *The Art of Computer Programming*, Vol. 2, Addison-Wesley: Reading MA, 1973. Section 4.5.2, Algorithm X.

**Purpose** Macintosh gestalt function

**Syntax** gestalthits = gestalt('selector')

**Description** gestal tbits = gestal t('selector') passes the four-character string

sel ector to the Macintosh Operating System function gestalt. For details about gestalt, refer to Chapter 1 of *Inside Macintosh: Operating System Util*-

ities.

The result, a 32-bit integer, is stored bitwise in gestal tbits. Thus, the least significant bit of the result is gestal tbits(32), while the most significant bit

is gestal tbi ts(1).

**Example** After executing:

gestaltbits = gestalt('sysa')

gestal tbi ts(32) will be 1 if run from a 680x0-based Macintosh, while gestal tbi ts(31) will be 1 if run from a PowerPC-based Macintosh.

Purpose Get field of structure array

Syntax f = getfield(s, 'field') $f = getfield(s, \{i, j\}, 'field', \{k\})$ 

**Description** f = getfield(s, 'field'), where s is a 1-by-1 structure, returns the contents of the specified field. This is equivalent to the syntax f = s. field.

 $f = getfield(s, \{i, j\}, 'field', \{k\})$  returns the contents of the specified field. This is equivalent to the syntax f = s(i, j). field(k). All subscripts must be passed as cell arrays—that is, they must be enclosed in curly braces (similar to $\{i, j\}$  and  $\{k\}$  above). Pass field references as strings.

## **Examples** Given the structure:

```
mystr(1, 1). name = 'alice';
mystr(1, 1).ID = 0;
mystr(2, 1). name = 'gertrude';
mystr(2, 1).ID = 1
```

Then the command  $f = getfield(mystr, \{2, 1\}, 'name')$  yields

f = gertrude

To list the contents of all name (or other) fields, embed getfield in a loop:

```
for i = 1:2
    name{i} = getfield(mystr, {i, 1}, 'name');
end
name

name =
    'alice' 'gertrude'
```

#### See Also

fields Field names of a structure setfield Set field of structure array

**Purpose** Define global variables

**Syntax** global X Y Z

**Description** 

global X Y Z defines X, Y, and Z as global in scope.

Ordinarily, each MATLAB function, defined by an M-file, has its own local variables, which are separate from those of other functions, and from those of the base workspace and nonfunction scripts. However, if several functions, and possibly the base workspace, *all* declare a particular name as global, they all share a single copy of that variable. Any assignment to that variable, in any function, is available to all the functions declaring it global. If the global variable does not exist the first time you issue the global statement, it is initializied to the empty matrix. By convention, global variable names are often long with all capital letters (not required).

It is an error to declare a variable global if:

- in the current workspace, a variable with the same name exists.
- in an M-file, it has been referenced previously.

#### Remarks

Use clear global *variable* to clear a global variable from the global workspace. Use clear *variable* to clear the global link from the current workspace without affecting the value of the global.

To use a global within a callback, declare the global, use it, then clear the global link from the workspace. This avoids declaring the global after it has been referenced. For example:

```
ui control ('style', 'pushbutton', 'CallBack',... 'global MY_GLOBAL, disp(MY_GLOBAL), MY_GLOBAL = MY_GLOBAL+1, clear MY_GLOBAL',... 'string', 'count')
```

## **Examples**

Here is the code for the functions  $ti\ c$  and toc (some comments abridged), which manipulate a stopwatch-like timer. The global variable TI CTOC is shared

by the two functions, but it is invisible in the base workspace or in any other functions that do not declare it.

```
function tic
     TIC Start a stopwatch timer.
         TIC; any stuff; TOC
     prints the time required.
     See also: TOC, CLOCK.
global TICTOC
TICTOC = clock;
function t = toc
     TOC Read the stopwatch timer.
     TOC prints the elapsed time since TIC was used.
     t = TOC; saves elapsed time in t, does not print.
     See also: TIC, ETIME.
global TICTOC
if nargout < 1
    elapsed_time = etime(clock, TICTOC)
else
    t = etime(clock, TICTOC);
end
```

## See Also

clear, isglobal, who

#### **Purpose**

Generalized Minimum Residual method (with restarts)

#### **Syntax**

```
x = gmres(A, b, restart)
gmres(A, b, restart, tol)
gmres(A, b, restart, tol, maxit)
gmres(A, b, restart, tol, maxit, M)
gmres(A, b, restart, tol, maxit, M1, M2)
gmres(A, b, restart, tol, maxit, M1, M2, x0)
x = gmres(A, b, restart, tol, maxit, M1, M2, x0)
[x, flag] = gmres(A, b, restart, tol, maxit, M1, M2, x0)
[x, flag, relres] = gmres(A, b, restart, tol, maxit, M1, M2, x0)
[x, flag, relres, iter] = gmres(A, b, restart, tol, maxit, M1, M2, x0)
[x, flag, relres, iter, resvec] = gmres(A, b, restart, tol, maxit, M1, M2, x0)
```

#### Description

x = gmres(A, b, restart) attempts to solve the system of linear equations A\*x = b for x. The coefficient matrix A must be square and the right hand side (column) vector b must have length n, where A is n-by-n. gmres will start iterating from an initial estimate that by default is an all zero vector of length n. gmres will restart itself every restart iterations using the last iterate from the previous outer iteration as the initial guess for the next outer iteration. Iterates are produced until the method either converges, fails, or has computed the maximum number of iterations. Convergence is achieved when an iterate x has relative residual norm(b-A\*x)/norm(b) less than or equal to the tolerance of the method. The default tolerance is 1e-6. The default maximum number of iterations is the minimum of n/restart and 10. No preconditioning is used.

gmres(A, b, restart, tol) specifies the tolerance of the method, tol.

gmres(A, b, restart, tol, maxit) additionally specifies the maximum number of iterations, maxit.

gmres(A, b, restart, tol, maxit, M) and gmres(A, b, restart, tol, maxit, M1, M2) use left preconditioner Mor M = M1\*M2 and effectively solve the system i nv(M)\*A\*x = i nv(M)\*b for x. If M1 or M2 is given as the empty matrix ([]), it is considered to be the identity matrix, equivalent to no preconditioning at all. Since systems of equations of the form M\*y = r are solved using backslash within gmres, it is wise to factor precondi-

tioners into their LU factors first. For example, replace gmres(A, b, restart, tol, maxit, M) with:

```
[M1, M2] = lu(M);
gmres(A, b, restart, tol, maxit, M1, M2).
```

gmres(A, b, restart, tol, maxit, M1, M2, x0) specifies the first initial estimate x0. If x0 is given as the empty matrix ([]), the default all zero vector is used.

x = gmres(A, b, restart, tol, maxit, M1, M2, x0) returns a solution x. If gmres converged, a message to that effect is displayed. If gmres failed to converge after the maximum number of iterations or halted for any reason, a warning message is printed displaying the relative residual  $\text{norm}(b-A^*x) / \text{norm}(b)$  and the iteration number at which the method stopped or failed.

[x, flag] = gmres(A, b, restart, tol, maxit, M1, M2, x0) returns a solution x and a flag which describes the convergence of gmres:

Flag	Convergence
0	gmres converged to the desired tolerance tol within maxit iterations without failing for any reason.
1	gmres iterated maxit times but did not converge.
2	One of the systems of equations of the form $M^*y = r$ involving the preconditioner was ill-conditioned and did not return a useable result when solved by $\setminus$ (backslash).
3	The method stagnated. (Two consecutive iterates were the same.)

Whenever fl ag is not 0, the solution x returned is that with minimal norm residual computed over all the iterations. No messages are displayed if the fl ag output is specified.

[x, flag, rel res] = gmres(A, b, restart, tol, maxit, M1, M2, x0) also returns the relative residual norm(b-A\*x)/norm(b). If flag is 0, then rel res  $\leq$  tol.

[x, flag, rel res, i ter] = gmres(A, b, restart, tol, maxit, M1, M2, x0) also returns both the outer and inner iteration numbers at which x was computed. The outer iteration number i ter(1) is an integer between 0 and maxit. The inner iteration number i ter(2) is an integer between 0 and restart.

```
[x, flag, rel res, i ter, resvec] = gmres(A, b, restart, tol, maxit, M1, M2, x0) also returns a vector of the residual norms at each inner iteration, starting from resvec(1) = norm(b-A*x0). If flag is 0 and i ter = [i j], resvec is of length (i-1)*restart+j+1 and resvec(end) \leq tol*norm(b).
```

## **Examples**

```
load west0479
A = west0479
b = sum(A, 2)
[x, flag] = gmres(A, b, 5)
```

flag is 1 since gmres(5) will not converge to the default tolerance 1e-6 within the default 10 outer iterations.

```
[L1, U1] = luinc(A, 1e-5);

[x1, flag1] = gmres(A, b, 5, 1e-6, 5, L1, U1);
```

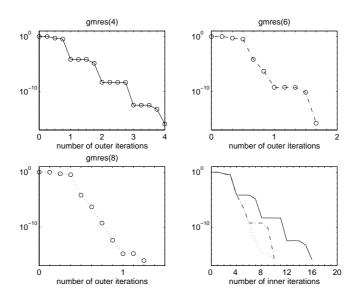
flag1 is 2 since the upper triangular U1 has a zero on its diagonal so gmres (5) fails in the first iteration when it tries to solve a system such as U1\*y = r for y with backslash.

```
[L2, U2] = luinc(A, 1e-6);
tol = 1e-15;
[x4, flag4, relres4, iter4, resvec4] = gmres(A, b, 4, tol, 5, L2, U2);
[x6, flag6, relres6, iter6, resvec6] = gmres(A, b, 6, tol, 3, L2, U2);
[x8, flag8, relres8, iter8, resvec8] = gmres(A, b, 8, tol, 3, L2, U2);
```

fl ag4, fl ag6, and fl ag8 are all 0 since gmres converged when restarted at iterations 4, 6, and 8 while preconditioned by the incomplete LU factorization with a drop tolerance of 1e-6. This is verified by the plots of outer iteration number against relative residual. A combined plot of all three clearly shows the restarting at iterations 4 and 6. The total number of iterations computed may

## gmres

be more for lower values of restart, but the number of length n vectors stored is fewer, and the amount of work done in the method decreases proportionally.



#### See Also

bi cg
bi cgstab
bi cgstab
BiConjugate Gradients Method
cgs
Conjugate Gradients Stabilized method
lui nc
Incomplete LU matrix factorizations
pcg
Preconditioned Conjugate Gradients method
qmr
Quasi-Minimal Residual method
Matrix left division

#### References

Saad, Youcef and Martin H. Schultz, *GMRES: A generalized minimal residual algorithm for solving nonsymmetric linear systems*, SIAM J. Sci. Stat. Comput., July 1986, Vol. 7, No. 3, pp. 856-869

Templates for the Solution of Linear Systems: Building Blocks for Iterative Methods, SIAM, Philadelphia, 1994.

Numerical gradient

**Syntax** 

FX = gradi ent (F)
[FX, FY] = gradi ent (F)
[Fx, Fy, Fz, ...] = gradi ent (F)
[...] = gradi ent (F, h)
[...] = gradi ent (F, h1, h2, ...)

**Definition** 

The *gradient* of a function of two variables, F(x,y), is defined as:

$$\nabla F = \frac{\partial F}{\partial x}\hat{i} + \frac{\partial F}{\partial y}\hat{j}$$

and can be thought of as a collection of vectors pointing in the direction of increasing values of F. In MATLAB, numerical gradients (differences) can be computed for functions with any number of variables. For a function of N variables, F(x,y,z,...),

$$\nabla F = \frac{\partial F}{\partial x} \tilde{\mathbf{i}} + \frac{\partial F}{\partial y} \tilde{\mathbf{j}} + \frac{\partial F}{\partial z} \hat{\mathbf{k}} + \dots$$

Description

FX = gradient (F) where F is a vector returns the one-dimensional numerical gradient of F. FX corresponds to  $\partial F/\partial x$ , the differences in the x direction.

[FX, FY] = gradient (F) where F is a matrix returns the x and y components of the two-dimensional numerical gradient. FX corresponds to  $\partial F/\partial x$ , the differences in the x (column) direction. FY corresponds to  $\partial F/\partial y$ , the differences in the y (row) direction. The spacing between points in each direction is assumed to be one.

[FX, FY, FZ,  $\dots$ ] = gradient(F) where F has N dimensions returns the N components of the gradient of F.

There are two ways to control the spacing between values in F:

A single spacing value, h, specifies the spacing between points in every direction.

N spacing values (h1, h2,  $\dots$ ) specify the spacing for each dimension of F. Scalar spacing parameters specify a constant spacing for each dimension. Vector

parameters specify the coordinates of the values along corresponding dimensions of F. In this case, the length of the vector must match the size of the corresponding dimension.

 $[\dots]=$  gradi ent (F,h) where h is a scalar uses h as the spacing between points in each direction.

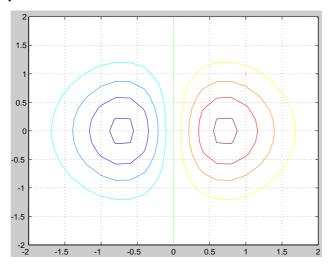
[...] = gradi ent (F, h1, h2, ...) with N spacing parameters specifies the spacing for each dimension of F.

# **Examples**

### The statements

```
v = -2: 0.2: 2;
[x, y] = meshgrid(v);
z = x \cdot * exp(-x \cdot ^2 - y \cdot ^2);
[px, py] = gradient(z, .2, .2);
contour(v, v, z), hold on, quiver(px, py), hold off
```

#### produce



Given,

```
F(:,:,1) = magic(3); \ F(:,:,2) = pascal(3); \\ gradient(F) \ takes \ dx = dy = dz = 1. \\ [PX, PY, PZ] = gradient(F, 0. 2, 0. 1, 0. 2) \ takes \ dx = 0. 2, \ dy = 0. 1, \ and \ dz = 0. 2.
```

See Also

del 2 Discrete Laplacian

diff Differences and approximate derivatives

Data gridding

**Syntax** 

```
ZI = gri ddata(x, y, z, XI, YI)
[XI, YI, ZI] = gri ddata(x, y, z, xi, yi)
[...] = gri ddata(..., method)
```

### Description

ZI = griddata(x, y, z, XI, YI) fits a surface of the form z = f(x, y) to the data in the (usually) nonuniformly spaced vectors (x, y, z). griddata interpolates this surface at the points specified by (XI, YI) to produce ZI. The surface always passes through the data points. XI and YI usually form a uniform grid (as produced by meshgrid).

XI can be a row vector, in which case it specifies a matrix with constant columns. Similarly, YI can be a column vector, and it specifies a matrix with constant rows.

[XI, YI, ZI] = gri ddata(x, y, z, xi, yi) returns the interpolated matrix ZI as above, and also returns the matrices XI and YI formed from row vector xi and column vector yi. These latter are the same as the matrices returned by meshgri d.

 $[\dots] = griddata(\dots, method)$  uses the specified interpolation method:

'linear' Triangle-based linear interpolation

(default)

' cubi c' Triangle-based cubic interpolation

'nearest'
Nearest neighbor interpolation
'v4'
MATLAB 4 gri ddata method

The state of the s

The method defines the type of surface fit to the data. The 'cubi c' and 'v4' methods produce smooth surfaces while 'linear' and 'nearest' have discontinuities in the first and zero'th derivatives, respectively. All the methods except 'v4' are based on a Delaunay triangulation of the data.

#### Remarks

XI and YI can be matrices, in which case <code>griddata</code> returns the values for the corresponding points (XI (i,j), YI (i,j)). Alternatively, you can pass in the row and column vectors xi and yi, respectively. In this case, <code>griddata</code> inter-

prets these vectors as if they were matrices produced by the command meshgri d(xi, yi).

## **Algorithm**

The griddata(..., 'v4') command uses the method documented in [1]. The other methods are based on Delaunay triangulation (see del aunay).

## **Examples**

Sample a function at 100 random points between  $\pm 2$ . 0:

```
rand('seed', 0)

x = rand(100, 1)*4-2; y = rand(100, 1)*4-2;

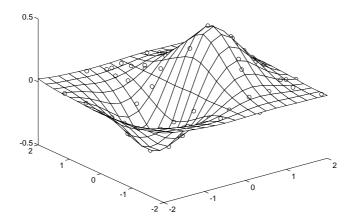
z = x. *exp(-x. ^2-y. ^2);
```

 $\mathbf{x},\,\mathbf{y},\,\mathbf{and}\,\,\mathbf{z}$  are now vectors containing nonuniformly sampled data. Define a regular grid, and grid the data to it:

```
ti = -2:.25:2;
[XI, YI] = meshgrid(ti, ti);
ZI = griddata(x, y, z, XI, YI);
```

Plot the gridded data along with the nonuniform data points used to generate it:

```
mesh(XI,YI,ZI), hold plot3(x,y,z,'o'), hold off
```



# griddata

See Also del aunay, i nterp2, meshgri d

**References** [1] Sandwell, David T., "Biharmonic Spline Interpolation of GEOS-3 and

SEASAT Altimeter Data", Geophysical Research Letters, 2, 139-142,1987.

[2] Watson, David E., *Contouring: A Guide to the Analysis and Display of Spatial Data*, Tarrytown, NY: Pergamon (Elsevier Science, Inc.): 1992.

Purpose Hadamard matrix

**Syntax** H = hadamard(n)

**Description** H = hadamard(n) returns the Hadamard matrix of order n.

**Definition** Hadamard matrices are matrices of 1's and -1's whose columns are orthogonal,

$$H' *H = n*I$$

where  $[n \ n] = size(H)$  and I = eye(n,n).

They have applications in several different areas, including combinatorics, signal processing, and numerical analysis, [1], [2].

An n-by-n Hadamard matrix with n>2 exists only if rem(n,4)=0. This function handles only the cases where n, n/12, or n/20 is a power of 2.

**Examples** The command hadamard(4) produces the 4-by-4 matrix:

1 1 1 1 1 -1 1 -11 1 -1 -11 -1 -1 1

See Also compan Companion matrix

hankel Hankel matrix toeplitz Toeplitz matrix

**References** [1] Ryser, H. J., *Combinatorial Mathematics*, John Wiley and Sons, 1963.

[2] Pratt, W. K., Digital Signal Processing, John Wiley and Sons, 1978.

# hankel

**Purpose** 

Hankel matrix

**Syntax** 

H = hankel(c)
H = hankel(c, r)

**Description** 

H = hankel (c) returns the square Hankel matrix whose first column is c and whose elements are zero below the first anti-diagonal.

H = hankel (c, r) returns a Hankel matrix whose first column is c and whose last row is r. If the last element of c differs from the first element of r, the last element of c prevails.

**Definition** 

A Hankel matrix is a matrix that is symmetric and constant across the anti-diagonals, and has elements h(i,j) = p(i+j-1), where vector  $p = [c \ r(2:end)]$  completely determines the Hankel matrix.

**Examples** 

A Hankel matrix with anti-diagonal disagreement is

 $p = [1 \ 2 \ 3 \ 8 \ 9 \ 10]$ 

See Also

hadamard Hadamard matrix toeplitz Toeplitz matrix

**Purpose** Online help for MATLAB functions and M-files

Syntax hel p

help topic

Description

hel p, by itself, lists all primary help topics. Each main help topic corresponds to a directory name on MATLAB's search path.

hel p  $topi\ c$  gives help on the specified topic. The topic can be a function name, a directory name, or a MATLABPATH relative partial pathname If it is a function name, hel p displays information on that function. If it is a directory name, hel p displays the contents file for the specified directory. It is not necessary to give the full pathname of the directory; the last component, or the last several components, is sufficient.

It's possible to write help text for your own M-files and toolboxes; see Remarks.

**Remarks** 

MATLAB's Help system, like MATLAB itself, is highly extensible. This allows you to write help descriptions for your own M-files and toolboxes – using the same self-documenting method that MATLAB's M-files and toolboxes use.

The command  $hel\ p$ , by itself, lists all help topics by displaying the first line (the H1 line) of the contents files in each directory on MATLAB's search path. The contents files are the M-files named Contents. m within each directory.

The command help topic, where topic is a directory name, displays the comment lines in the Contents. m file located in that directory. If a contents file does not exist, help displays the H1 lines of all the files in the directory.

The command help topic, where topic is a function name, displays help on the function by listing the first contiguous comment lines in the M-file topic. m

#### **Creating Online Help for Your Own M-Files**

Create self-documenting online help for your own M-files by entering text on one or more contiguous comment lines, beginning with the second line of the file (first line if it is a script). (See *Applying MATLAB* for information about creating

M-files.) For example, an abridged version of the M-file angle. m provided with MATLAB could contain:

```
function p = angle(h)
% ANGLE Polar angle.
% ANGLE(H) returns the phase angles, in radians, of a matrix
% with complex elements. Use ABS for the magnitudes.
p = atan2(i mag(h), real(h));
```

When you execute help angle, lines 2, 3, and 4 display. These lines are the first block of contiguous comment lines. The help system ignores comment lines that appear later in an M-file, after any executable statements, or after a blank line.

The first comment line in any M-file (the H1 line) is special. It should contain the function name and a brief description of the function. The lookfor command searches and displays this line, and help displays these lines in directories that do not contain a Contents. m file.

#### Creating Contents Files for Your Own M-File Directories

A Contents. m file is provided for each M-file directory included with the MATLAB software. If you create directories in which to store your own M-files, you should create Contents. m files for them too. To do so, simply follow the format used in an existing Contents. m file.

## **Examples**

#### The command

help datafun

gives help on the datafun directory.

To prevent long descriptions from scrolling off the screen before you have time to read them, enter more on; then enter the help command.

#### See Also

di r	Directory listing	
lookfor	Keyword search through all help entries	
more	Control paged output for the command window	
path	Control MATLAB's directory search path	
what	Directory listing of M-files, MAT-files, and MEX-files	
whi ch	Locate functions and files	
Can also noutialmath		

See also partialpath.

Hessenberg form of a matrix

Syntax

$$[P, H] = hess(A)$$
  
 $H = hess(A)$ 

Description

H = hess(A) finds H, the Hessenberg form of matrix A.

[P, H] = hess(A) produces a Hessenberg matrix H and a unitary matrix P so that A = P\*H\*P' and P'\*P = eye(size(A)).

**Definition** 

A Hessenberg matrix is zero below the first subdiagonal. If the matrix is symmetric or Hermitian, the form is tridiagonal. This matrix has the same eigenvalues as the original, but less computation is needed to reveal them.

**Examples** 

H is a 3-by-3 eigenvalue test matrix:

$$\begin{array}{ccccc} H & = & & & \\ -149 & & -50 & & -154 \\ 537 & & 180 & & 546 \\ -27 & & -9 & & -25 \end{array}$$

Its Hessenberg form introduces a single zero in the (3,1) position:

**Algorithm** 

For real matrices, hess uses the EISPACK routines ORTRAN and ORTHES. ORTHES converts a real general matrix to Hessenberg form using orthogonal similarity transformations. ORTRAN accumulates the transformations used by ORTHES.

When hess is used with a complex argument, the solution is computed using the QZ algorithm by the EISPACK routines QZHES. It has been modified for complex problems and to handle the special case B = I.

For detailed write-ups on these algorithms, see the EISPACK Guide.

See Also

ei g Eigenvalues and eigenvectors qz QZ factorization for generalized eigenvalues

schur Schur decomposition

# hess

#### References

- [1] Smith, B. T., J. M. Boyle, J. J. Dongarra, B. S. Garbow, Y. Ikebe, V. C. Klema, and C. B. Moler, *Matrix Eigensystem Routines EISPACK Guide*, Lecture Notes in Computer Science, Vol. 6, second edition, Springer-Verlag, 1976.
- [2] Garbow, B. S., J. M. Boyle, J. J. Dongarra, and C. B. Moler, *Matrix Eigensystem Routines EISPACK Guide Extension*, Lecture Notes in Computer Science, Vol. 51, Springer-Verlag, 1977.
- [3] Moler, C.B. and G. W. Stewart, "An Algorithm for Generalized Matrix Eigenvalue Problems," *SIAM J. Numer. Anal.*, Vol. 10, No. 2, April 1973.

**Purpose** IEEE hexadecimal to decimal number conversion

**Syntax** d = hex2dec(' hex\_val ue')

**Description** d = hex2dec('hex\_value') converts hex\_value to its floating-point integer

representation. The argument *hex\_value* is a hexadecimal integer stored in a MATLAB string. If *hex\_value* is a character array, each row is interpreted as a

hexadecimal string.

**Examples** hex2dec('3ff') is 1023.

For a character array S

S = 0FF 2DE 123

hex2dec(S)

ans = 255 734 291

See Also dec2hex Decimal to hexadecimal number conversion

format Control the output display format

hex2num Hexadecimal to double number conversion

sprintf Write formatted data to a string

## hex2num

**Purpose** Hexadecimal to double number conversion

**Syntax** f = hex2num(' hex\_val ue')

**Description**  $f = hex2num('hex_value')$  converts  $hex_value$  to the IEEE double preci-

sion floating-point number it represents. NaN, I  $_{\rm nf}$ , and denormalized numbers are all handled correctly. Fewer than 16 characters are padded on the right

with zeros.

**Examples** f = hex2num('400921fb54442d18')

f =

3. 14159265358979

 $\textbf{Limitations} \hspace{15mm} \text{hex2num only works for IEEE numbers; it does not work for the floating-point} \\$ 

representation of the VAX or other non-IEEE computers.

**See Also** format Control the output display format

hex2dec IEEE hexadecimal to decimal number conversion

sprintf Write formatted data to a string

Purpose Hilbert matrix

Syntax H = hilb(n)

**Description** H = hilb(n) returns the Hilbert matrix of order n.

**Definition** The Hilbert matrix is a notable example of a poorly conditioned matrix [1]. The

elements of the Hilbert matrices are H(i, j) = 1/(i+j-1).

**Examples** Even the fourth-order Hilbert matrix shows signs of poor conditioning.

cond(hilb(4)) = 1.5514e+04

**Algorithm** See the M-file for a good example of efficient MATLAB programming where

conventional for loops are replaced by vectorized statements.

**See Also** i nyhi l b Inverse of the Hilbert matrix

**References** [1] Forsythe, G. E. and C. B. Moler, *Computer Solution of Linear Algebraic* 

Systems, Prentice-Hall, 1967, Chapter 19.

Purpose Imaginary unit

Syntax i

a+bi x+i \*y

**Description** 

As the basic imaginary unit sqrt(-1), i is used to enter complex numbers. Since i is a function, it can be overridden and used as a variable. This permits you to use i as an index in for loops, etc.

If desired, use the character i without a multiplication sign as a suffix in forming a complex numerical constant.

You can also use the character j as the imaginary unit.

Examples Z = 2+3i

Z = x+i \*y

Z = r\*exp(i\*theta)

See Also conj Complex conjugate

i mag Imaginary part of a complex number

j Imaginary unit

real Real part of complex number

#### **Purpose** Conditionally execute statements

#### Syntax

if expression statements

end

if expression1 statements elseif expression2 statements

else

statements

end

#### Description

if conditionally executes statements.

The simple form is:

if expression statements

More complicated forms use el se or el sei f. Each i f must be paired with a matching end.

## **Arguments**

expressi on

A MATLAB expression, usually consisting of smaller expressions or variables joined by relational operators (==, <, >, <=, >=, or ~=). Two examples are: count < limit and (height - offset) >= 0.

Expressions may also include logical functions, as in:

isreal(A).

Simple expressions can be combined by logical operators  $(\&,|,\sim)$  into compound expressions such as: (count < limit) & ((height - offset) >= 0).

statements

One or more MATLAB statements to be executed only if the *expressi on* is *true* (or nonzero). See Examples for information about how nonscalar variables are evaluated.

## **Examples**

Here is an example showing if, else, and elseif:

```
for i = 1:n

for j = 1:n

if i == j

a(i,j) = 2;

elseif abs([i \ j]) == 1

a(i,j) = 1;

else

a(i,j) = 0;

end

end
```

Such expressions are evaluated as *false* unless every element-wise comparison evaluates as *true*. Thus, given matrices A and B:

The expression:

A < B	Evaluates as false	Since $A(1, 1)$ is not less than $B(1, 1)$ .
A < (B+1)	Evaluates as true	Since no element of A is greater than the corresponding element of B.
A & B	Evaluates as false	Since $A(1, 2) \mid B(1, 2)$ is false.
5 > B	Evaluates as true	Since every element of B is less than 5.

## See Also

break	Break out of flow control structures
el se	Conditionally execute statements
end	Terminate for, while, switch, and if statements or
	indicate last index
for	Repeat statements a specific number of times
return	Return to the invoking function
switch	Switch among several cases based on expression
whi l e	Repeat statements an indefinite number of times
	<del>-</del>

**Purpose** Inverse one-dimensional fast Fourier transform

**Syntax** y = ifft(X)

y = ifft(X, n)

y = i fft(X, [], dim)y = i fft(X, n, dim)

**Description** y = i fft(X) returns the inverse fast Fourier transform of vector X.

If X is a matrix, ifft returns the inverse Fourier transform of each column of the matrix.

If X is a multidimensional array, ifft operates on the first non-singleton dimension.

y = i fft(X, n) returns the n-point inverse fast Fourier transform of vector X.

y = ifft(X, [], dim) and y = ifft(X, n, dim) return the inverse discrete Fourier transform of X across the dimension dim.

**Examples** For any x, ifft(fft(x)) equals x to within roundoff error. If x is real,

ifft(fft(x)) may have small imaginary parts.

**Algorithm** The algorithm for ifft(x) is the same as the algorithm for fft(x), except for

a sign change and a scale factor of  $n = l \, \text{ength}(x)$ . So the execution time is

fastest when n is a power of 2 and slowest when n is a large prime.

**See Also** dftmtx, freqz, specpl ot, and spectrum in the Signal Processing Toolbox, and:

fft One-dimensional fast Fourier transform fft2 Two-dimensional fast Fourier transform

fftshift Shift DC component of fast Fourier transform to center

of spectrum

**Purpose** Inverse two-dimensional fast Fourier transform

**Syntax** Y = ifft2(X)

Y = ifft2(X, m, n)

**Description** Y = i fft2(X) returns the two-dimensional inverse fast Fourier transform of

matrix X.

Y = i fft2(X, m, n) returns the m-by-n inverse fast Fourier transform of

matrix X.

**Examples** For any X, ifft2(fft2(X)) equals X to within roundoff error. If X is real,

ifft2(fft2(X)) may have small imaginary parts.

**Algorithm** The algorithm for ifft2(X) is the same as the algorithm for fft2(X), except

for a sign change and scale factors of [m, n] = size(X). The execution time is fastest when m and n are powers of 2 and slowest when they are large primes.

**See Also** dftmtx, freqz, specpl ot, and spectrum in the Signal Processing Toolbox, and:

fft2 Two-dimensional fast Fourier transform

fft shift Shift DC component of fast Fourier transform to center

of spectrum

ifft Inverse one-dimensional fast Fourier transform

Inverse multidimensional fast Fourier transform

**Syntax** 

```
Y = ifftn(X)

Y = ifftn(X, siz)
```

**Description** 

Y = i fftn(X) performs the N-dimensional inverse fast Fourier transform. The result Y is the same size as X.

Y = i fftn(X, si z) pads X with zeros, or truncates X, to create a multidimensional array of size si z before performing the inverse transform. The size of the result Y is si z.

Remarks

For any X, ifftn(fftn(X)) equals X within roundoff error. If X is real, ifftn(X) may have small imaginary parts.

**Algorithm** 

ifftn(X) is equivalent to

```
Y = X;
for p = 1:length(size(X))
        Y = ifft(Y,[],p);
end
```

This computes in-place the one-dimensional inverse fast Fourier transform along each dimension of X. The time required to compute ifftn(X) depends strongly on the number of prime factors of the dimensions of X. It is fastest when all of the dimensions are powers of 2.

See Also

fft	One-dimensional fast Fourier transform
fft2	Two-dimensional fast Fourier transform
fftn	Multidimensional fast Fourier transform

# imag

**Purpose** Imaginary part of a complex number

**Syntax** Y = i mag(Z)

**Description** Y = i mag(Z) returns the imaginary part of the elements of array Z.

Examples i mag(2+3i) ans =

ns = 3

See Also conj Complex conjugate

i, j Imaginary unit  $(\sqrt{-1})$ 

real Real part of complex number

Return information about a graphics file

**Synopsis** 

info = imfinfo(filename, fmt)
info = imfinfo(filename)

**Description** 

info = i mfinfo(filename, fmt) returns a structure whose fields contain information about an image in a graphics file. filename is a string that specifies the name of the graphics file, and fmt is a string that specifies the format of the file. The file must be in the current directory or in a directory on the MATLAB path. If i mfinfo cannot find a filenamed filename, it looks for a filenamed filename. fmt.

This table lists the possible values for fmt:

Format	File type
'bmp'	Windows Bitmap (BMP)
' hdf'	Hierarchical Data Format (HDF)
'jpg' or'jpeg'	Joint Photographic Experts Group (JPEG)
' pcx'	Windows Paintbrush (PCX)
'tif' or'tiff'	Tagged Image File Format (TIFF)
' xwd'	X Windows Dump (XWD)

If filename is a TIFF or HDF file containing more than one image, info is a structure array with one element (i.e., an individual structure) for each image in the file. For example, info(3) would contain information about the third image in the file.

# imfinfo

The set of fields in i nf o depends on the individual file and its format. However, the first nine fields are always the same. This table lists these fields and describes their values:

Field	Value	
Filename	A string containing the name of the file; if the file is not in the current directory, the string contains the full pathname of the file	
FileModDate	A string containing the date when the file was last modified	
Fi l eSi ze	An integer indicating the size of the file in bytes	
Format	A string containing the file format, as specified by fmt; for JPEG and TIFF files, the three-letter variant is returned	
FormatVersi on	A string or number describing the version of the format	
Wi dth	An integer indicating the width of the image in pixels	
Hei ght	An integer indicating the height of the image in pixels	
BitDepth	An integer indicating the number of bits per pixel	
ColorType	A string indicating the type of image; either 'truecol or' for a truecolor RGB image, 'grayscal e' for a grayscale intensity image, or 'indexed' for an indexed image	

info = imfinfo(filename) attempts to infer the format of the file from its content.

```
Example
                     info = imfinfo('flowers.bmp')
                     info =
                                    Filename: 'flowers.bmp'
                                 FileModDate: '16-0ct-1996 11:41:38'
                                    FileSize: 182078
                                      Format: 'bmp'
                               FormatVersion: 'Version 3 (Microsoft Windows 3.x)'
                                       Wi dth: 500
                                      Height: 362
                                    BitDepth: 8
                                   Col orType: 'i ndexed'
                             FormatSi gnature: 'BM'
                         NumColormapEntries: 256
                                    Colormap: [256x3
                                                      double]
                                     RedMask: []
                                   GreenMask: []
                                    BlueMask: []
                             ImageDataOffset: 1078
                            BitmapHeaderSize: 40
                                   NumPl anes: 1
                             Compressi onType: 'none'
                                  BitmapSize: 181000
                              HorzResolution: 0
                              VertResolution: 0
                               NumColorsUsed: 256
                         NumImportantColors: 0
```

See Also

i mread Read image from graphics file i mwri te Write an image to a graphics file

Read image from graphics file

## **Synopsis**

```
A = i mread(filename, fmt)
[X, map] = i mread(filename, fmt)
[...] = i mread(filename)
[...] = i mread(..., i dx) (TIFF only)
[...] = i mread(..., ref) (HDF only)
```

## Description

A = i mread(filename, fmt) reads the image in filename into A, whose class is uint 8. If the file contains a grayscale intensity image, A is a two-dimensional array. If the file contains a truecolor (RGB) image, A is a three-dimensional (m-by-n-by-3) array. filename is a string that specifies the name of the graphics file, and fmt is a string that specifies the format of the file. The file must be in the current directory or in a directory in the MATLAB path. If i mread cannot find a file named filename, it looks for a file named filename. fmt.

This table lists the possible values for fmt:

Format	File type
'bmp'	Windows Bitmap (BMP)
'hdf'	Hierarchical Data Format (HDF)
'jpg' or'jpeg'	Joint Photographic Experts Group (JPEG)
'pcx'	Windows Paintbrush (PCX)
'tif' or'tiff'	Tagged Image File Format (TIFF)
' xwd'	X Windows Dump (XWD)

[X, map] = i mread(filename, fmt) reads the indexed image in filename into X and its associated colormap into map. X is of class ui nt 8, and map is of class double. The colormap values are rescaled to the range [0, 1].

 $[\dots] = i \text{ mread}(filename)$  attempts to infer the format of the file from its content.

 $[\dots]$  = i mread $(\dots,i$  dx) reads in one image from a multi-image TIFF file. i dx is an integer value that specifies the order in which the image appears in the file. For example, if i dx is 3, i mread reads the third image in the file. If you omit this argument, i mread reads the first image in the file.

[...] = i mread(..., ref) reads in one image from a multi-image HDF file. ref is an integer value that specifies the reference number used to identify the image. For example, if ref is 12, i mread reads the image whose reference number is 12. (Note that in an HDF file the reference numbers do not necessarily correspond to the order of the images in the file.) If you omit this argument, i mread reads the first image in the file.

This table summarizes the types of images that i mread can read:

Format	Variants
BMP	1-bit, 4-bit, 8-bit, and 24-bit uncompressed images; 4-bit and 8-bit run-length encoded (RLE) images
HDF	8-bit raster image datasets, with or without associated colormap; 24-bit raster image datasets
JPEG	Any baseline JPEG image; JPEG images with some commonly used extensions
PCX	1-bit, 8-bit, and 24-bit images
TIFF	Any baseline TIFF image, including 1-bit, 8-bit, and 24-bit uncompressed images; 1-bit, 8-bit, and 24-bit images with packbit compression; 1-bit images with CCITT compression
XWD	1-bit and 8-bit ZPixmaps; XYBitmaps; 1-bit XYPixmaps

# imread

## **Examples**

This example reads the sixth image in a TIFF file:

```
[X, map] = i mread('flowers.tif', 6);
```

This example reads the fourth image in an HDF file:

```
info = imfinfo('skull.hdf');
[X, map] = imread('skull.hdf', info(4).Reference);
```

## See Also

i mf i nf oi mf i nf oi mwr i teReturn information about a graphics filei write an image to a graphics file

\_\_\_\_

Write an image to a graphics file

#### **Synopsis**

```
i mwrite(A, filename, fmt)
i mwrite(X, map, filename, fmt)
i mwrite(..., filename)
i mwrite(..., Parameter, Value,...)
```

#### Description

i mwrite(A, filename, fmt) writes the image in A to filename. filename is a string that specifies the name of the output file, and fmt is a string that specifies the format of the file. If A is a grayscale intensity image or a truecolor (RGB) image of class uint8, i mwrite writes the actual values in the array to the file. If A is of class double, i mwrite rescales the values in the array before writing, using uint8(round(255\*A)). This operation converts the floating-point numbers in the range [0, 1] to 8-bit integers in the range [0, 255].

This table lists the possible values for fmt:

Format	File type
' bmp'	Windows Bitmap (BMP)
'hdf'	Hierarchical Data Format (HDF)
'jpg' or 'jpeg'	Joint Photographers Expert Group (JPEG)
'pcx'	Windows Paintbrush (PCX)
'tif' or 'tiff'	Tagged Image File Format (TIFF)
' xwd'	X Windows Dump (XWD)

i mwrite(X, map, filename, fmt) writes the indexed image in X, and its associated colormap map, to filename. If X is of class uint8, i mwrite writes the actual values in the array to the file. If X is of class double, i mwrite offsets the values in the array before writing, using uint8(X-1). map must be of class double; i mwrite rescales the values in map using uint8(round(255\*map)).

i mwrite(..., filename) writes the image to filename, inferring the format to use from the filename's extension. The extension must be one of the legal values for fmt.

i mwri te( $\dots$ , Parameter, Value, $\dots$ ) specifies parameters that control various characteristics of the output file. Parameters are currently supported for HDF, JPEG, and TIFF files.

This table describes the available parameters for HDF files:

Parameter	Values	Default
'Compression'	One of these strings: 'none', 'rle', 'j peg'	'rle'
' Qual i ty'	A number between 0 and 100; parameter applies only if 'Compressi on' is 'j peg'; higher numbers mean quality is better (less image degradation due to compression), but the resulting file size is larger	75
'WriteMode'	One of these strings: 'overwrite', 'append'	'overwrite'

This table describes the available parameters for JPEG files:

Parameter	Values	Default
' Qual i ty'	A number between 0 and 100; higher numbers mean quality is better (less image degradation due to compression), but the resulting file size is larger	75

This table describes the available parameters for TIFF files:

Parameter	Values	Default
'Compression'	One of these strings: 'none', 'packbits','ccitt';'ccitt' is valid for binary images only	'ccitt' for binary images; 'packbits' for all other images
' Descri pti on'	Any string; fills in the I mageDescription field returned by i mfinfo	empty

This table summarizes the types of images that i  ${\tt mwrite}$  can write:

Format	Variants
BMP	8-bit uncompressed images with associated colormap; 24-bit uncompressed images
HDF	8-bit raster image datasets, with or without associated colormap; 24-bit raster image datasets
JPEG	Baseline JPEG images
PCX	8-bit images
TIFF	Baseline TIFF images, including 1-bit, 8-bit, and 24-bit uncompressed images; 1-bit, 8-bit, and 24-bit images with packbit compression; 1-bit images with CCITT compression
XWD	8-bit ZPixmaps

# **Example**

```
i mwrite(X, map, 'flowers. hdf', 'Compression', 'none', ... 'WriteMode', 'append')
```

## **See Also**

i mfi nfo	Return information about a graphics file
i mread	Read image from graphics file

Subscripts from linear index

**Syntax** 

$$[I, J] = i \operatorname{nd2sub}(si z, IND)$$
  
 $[I1, I2, I3, ..., In] = i \operatorname{nd2sub}(si z, IND)$ 

Description

The  $i\,nd2sub$  command determines the equivalent subscript values corresponding to a single index into an array.

 $[I, J] = i \, nd2sub(si\, z, IND)$  returns the arrays I and J containing the equivalent row and column subscripts corresponding to the index matrix IND for a matrix of size  $si\, z$ .

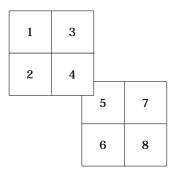
For matrices,  $[I, J] = i \, nd2sub(si \, ze(A), fi \, nd(A>5))$  returns the same values as

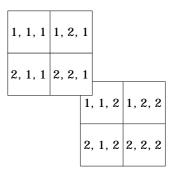
[I, J] = find(A>5).

 $[I1,I2,I3,\ldots,In]=i$  nd2sub(siz,IND) returns n subscript arrays I1,I2,...,In containing the equivalent multidimensional array subscripts equivalent to IND for an array of size siz.

**Examples** 

The mapping from linear indexes to subscript equivalents for a 2-by-2-by-2 array is:





See Also

sub2i nd fi nd Single index from subscripts
Find indices and values of nonzero elements

Purpose Infinity

Syntax Inf

**Description** Inf returns the IEEE arithmetic representation for positive infinity. Infinity

results from operations like division by zero and overflow, which lead to results

too large to represent as conventional floating-point values.

**Examples** 1/0, 1. e1000, 2^1000, and exp(1000) all produce Inf.

log(0) produces –Inf.

Inf-Inf and Inf/Inf both produce NaN, Not-a-Number.

**See Also** is\* Detect state

NaN Not-a-Number

# inferiorto

Purpose Inferior class relationship

**Syntax** inferiorto('class1', 'class2',...)

**Description** The inferior to function establishes a hierarchy which determines the order

in which MATLAB calls object methods.

inferiorto('class1', 'class2',...) invoked within a class constructor method (say mycl ass. m) indicates that mycl ass's method should not be invoked if a function is called with an object of class mycl ass and one or more objects of

class class1, class2, and so on.

**Remarks** Suppose A is of class 'class a', B is of class 'class b' and C is of class

'class\_c'. Also suppose the constructor class\_c. m contains the statement: inferiorto('class\_a'). Then e = fun(a, c) or e = fun(c, a) invokes

class\_a/fun.

If a function is called with two objects having an unspecified relationship, the two objects are considered to have equal precedence, and the leftmost object's

method is called. So, fun(b, c) calls class\_b/fun, while fun(c, b) calls

class\_c/fun.

See Also Superior to Superior class relationship

Construct an inline object

#### **Syntax**

```
g = i nl i ne(expr)
```

g = inline(expr, arg1, arg2, ...)

g = i nl i ne(expr, n)

## Description

inline(expr) constructs an inline function object from the MATLAB expression contained in the string expr. The input argument to the inline function is automatically determined by searching expr for an isolated lower case alphabetic character, other than i or j, that is not part of a word formed from several alphabetic characters. If no such character exists, x is used. If the character is not unique, the one closest to x is used. If there is a tie, the one later in the alphabet is chosen.

inline(expr, arg1, arg2, ...) constructs an inline function whose input arguments are specified by the strings arg1, arg2,... Multicharacter symbol names may be used.

i nl i ne ( expr, n) , where n is a scalar, constructs an inline function whose input arguments are x, P1, P2, ...

#### Remarks

Three commands related to i nl i ne allow you to examine an inline function object and determine how it was created.

 ${\rm char}(\mathit{fun})\ \ {\rm converts}\ {\rm the}\ {\rm inline}\ {\rm function}\ {\rm into}\ {\rm a}\ {\rm character}\ {\rm array}.$  This is identical to formul a(  $\mathit{fun}$ ) .

argnames(fun) returns the names of the input arguments of the inline object fun as a cell array of strings.

formula (fun) returns the formula for the inline object fun.

A fourth command vectorize(fun) inserts a . before any ^, \* or /' in the formula for fun. The result is a vectorized version of the inline function.

# **Examples**

Create a simple inline function to square a number:

```
g = inline('t^2')
g =
    Inline function:
    g(t) = t^2
char(g)
ans =
    t^2
reate an inline function
```

Create an inline function to compute the formula  $f = 3\sin(2x^2)$ :

```
g(pi)

ans =

2.3306

g(2*pi)

ans =

-1.2151

fmin(g, pi, 2*pi)

ans =

3.8630
```

# inmem

**Purpose** Functions in memory

Syntax M = i nmem

[M, mex] = i nmem

**Description** M = i nmem returns a cell array of strings containing the names of the M-files

that are in the P-code buffer.

[M, mex] = i nmem returns a cell array containing the names of the MEX-files

that have been loaded.

**Examples** clear all % start with a clean slate

erf(.5) M = inmem

lists the M-files that were required to run erf.

Detect points inside a polygonal region

**Syntax** 

IN = inpolygon(X, Y, xv, yv)

**Description** 

IN = inpolygon(X, Y, xv, yv) returns a matrix IN the same size as X and Y. Each element of IN is assigned one of the values 1, 0.5 or 0, depending on whether the point (X(p,q),Y(p,q)) is inside the polygonal region whose vertices are specified by the vectors xv and yv. In particular:

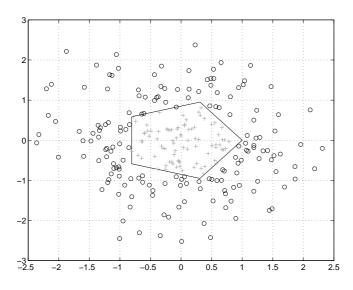
IN(p, q) = 1 If (X(p, q), Y(p, q)) is inside the polygonal region

IN(p, q) = 0.5 If (X(p, q), Y(p, q)) is on the polygon boundary

IN(p, q) = 0 If (X(p, q), Y(p, q)) is outside the polygonal region

**Examples** 

```
 \begin{array}{l} L = l \, i \, nspace(0, 2. \, ^*pi, 6); \quad xv = cos(L) \, '; \, yv = si \, n(L) \, '; \\ xv = [xv \; ; \; xv(1)]; \quad yv = [yv \; ; \; yv(1)]; \\ x = randn(250, 1); \quad y = randn(250, 1); \\ i \, n = i \, npol \, ygon(x, y, xv, yv); \\ pl \, ot(xv, yv, x(i \, n), y(i \, n), ' \, r+', x(\sim i \, n), y(\sim i \, n), ' \, bo') \end{array}
```



Request user input

#### **Syntax**

```
user_entry = input('prompt')
user_entry = input('prompt', 's')
```

# Description

The response to the input prompt can be any MATLAB expression, which is evaluated using the variables in the current workspace.

user\_entry = input('prompt') displays prompt as a prompt on the screen,
waits for input from the keyboard, and returns the value entered in
user\_entry.

user\_entry = input('prompt', 's') returns the entered string as a text variable rather than as a variable name or numerical value.

#### Remarks

If you press the **Return** key without entering anything, i nput returns an empty matrix.

The text string for the prompt may contain one or more ' $\n'$  characters. The ' $\n'$  means to skip to the next line. This allows the prompt string to span several lines. To display just a backslash, use ' $\n'$ '.

### **Examples**

Press Return to select a default value by detecting an empty matrix:

```
i = input('Do you want more? Y/N [Y]: ','s');
if isempty(i)
        i = 'Y';
end
```

#### See Also

The gi nput and ui control commands in the MATLAB Graphics Guide, and:

keyboard Invoke the keyboard in an M-file menu Generate a menu of choices for user input **Purpose** Input argument name

**Syntax** i nput name ( argnum)

**Description** This command can be used only inside the body of a function.

i nput name ( argnum) returns the workspace variable name corresponding to the argument number argnum. If the input argument has no name (for example, if it is an expression instead of a variable), the input name command returns the empty string ('').

Examples

Suppose the function myfun. m is defined as:

```
 \begin{array}{lll} function \ c &= myfun(a,b) \\ disp(sprintf('First \ calling \ variable \ is \ "%s".', inputname(1)) \end{array}
```

Then

```
x = 5; y = 3; myfun(x, y)
```

produces

First calling variable is "x".

But

```
myfun(pi+1, pi-1)
```

produces

First calling variable is "".

See Also

nargi n, nargout Number of function arguments
nargchk Check number of input arguments

# int2str

**Purpose** Integer to string conversion

**Syntax** str = int2str(N)

**Description** str = int2str(N) converts an integer to a string with integer format. The

input N can be a single integer or a vector or matrix of integers. Noninteger

inputs are rounded before conversion.

**Examples** int2str(2+3) is the string '5'.

One way to label a plot is

```
title(['case number ' int2str(n)])
```

For matrix or vector inputs, int2str returns a string matrix:

int2str(eye(3))

ans =

1 0 0 0 1 0 0 0 1

See Also

fprintf Write formatted data to file
num2str Number to string conversion
sprintf Write formatted data to a string

One-dimensional data interpolation (table lookup)

**Syntax** 

$$yi = interp1(x, Y, xi)$$

$$yi = interp1(x, Y, xi, method)$$

Description

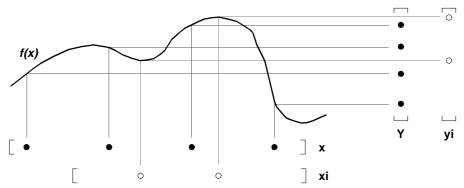
yi = interp1(x, Y, xi) returns vector yi containing elements corresponding to the elements of xi and determined by interpolation within vectors x and Y. The vector x specifies the points at which the data Y is given. If Y is a matrix, then the interpolation is performed for each column of Y and Y will be  $1 \operatorname{ength}(xi)$ -by-si Z be Y. Out of range values are returned as NaNs.

yi = interp1(x, Y, xi, method) interpolates using alternative methods:

- 'nearest' for nearest neighbor interpolation
- 'linear' for linear interpolation
- 'spline' for cubic spline interpolation
- 'cubi c' for cubic interpolation

All the interpolation methods require that x be monotonic. For faster interpolation when x is equally spaced, use the methods '\*linear', '\*cubic', '\*nearest', or '\*spline'.

The interp1 command interpolates between data points. It finds values of a one-dimensional function f(x) underlying the data at intermediate points. This is shown below, along with the relationship between vectors  $\mathbf{x}$ ,  $\mathbf{y}$ ,  $\mathbf{x}$ , and  $\mathbf{y}$ .



Interpolation is the same operation as *table lookup*. Described in table lookup terms, the *table* is tab = [x, y] and interp1 *looks up* the elements of xi in x,

and, based upon their locations, returns values  $\mathbf{y}\mathbf{i}$  interpolated within the elements of  $\mathbf{y}$ .

# **Examples**

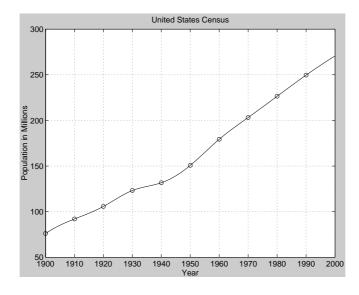
Here are two vectors representing the census years from 1900 to 1990 and the corresponding United States population in millions of people.

The expression interp1(t, p, 1975) interpolates within the census data to estimate the population in 1975. The result is

```
ans = 214. 8585
```

Now interpolate within the data at every year from 1900 to 2000, and plot the result.

```
x = 1900: 1: 2000;
y = interp1(t, p, x, 'spline');
plot(t, p, 'o', x, y)
```



Sometimes it is more convenient to think of interpolation in table lookup terms where the data are stored in a single table. If a portion of the census data is stored in a single 5-by-2 table,

```
tab =
    1950    150. 697
    1960    179. 323
    1970    203. 212
    1980    226. 505
    1990    249. 633
```

then the population in 1975, obtained by table lookup within the matrix tab, is

```
p = interp1(tab(:,1),tab(:,2),1975)
p =
    214.8585
```

# **Algorithm**

The interp1 command is a MATLAB M-file. The 'nearest' , 'li near' and 'cubi c' methods have fairly straightforward implementations. For the 'spline' method, interp1 calls a function spline that uses the M-files ppval, mkpp, and unmkpp. These routines form a small suite of functions for working with piecewise polynomials. spline uses them in a fairly simple fashion to perform cubic spline interpolation. For access to the more advanced features, see these M-files and the Spline Toolbox.

#### See Also

interpft	One-dimensional interpolation using the FFT method.
interp2	Two-dimensional data interpolation (table lookup)
interp3	Three-dimensional data interpolation (table lookup)
interpn	Multidimensional data interpolation (table lookup)
spl i ne	Cubic spline interpolation

#### References

[1] de Boor, C. A Practical Guide to Splines, Springer-Verlag, 1978.

Two-dimensional data interpolation (table lookup)

### **Syntax**

ZI = interp2(X, Y, Z, XI, YI)

ZI = interp2(Z, XI, YI)

ZI = interp2(Z, ntimes)

ZI = interp2(X, Y, Z, XI, YI, method)

# Description

ZI = interp2(X, Y, Z, XI, YI) returns matrix ZI containing elements corresponding to the elements of XI and YI and determined by interpolation within the two-dimensional function specified by matrices X, Y, and Y and Y must be monotonic, and have the same format ("plaid") as if they were produced by meshgri Y d. Matrices Y and Y specify the points at which the data Y is given. Out of range values are returned as Y NaNs.

XI and YI can be matrices, in which case interp2 returns the values of Z corresponding to the points (XI (i,j), YI (i,j)). Alternatively, you can pass in the row and column vectors xi and yi, respectively. In this case, interp2 interprets these vectors as if you issued the command meshgrid(xi, yi).

ZI = interp2(Z, XI, YI) assumes that X = 1: n and Y = 1: m, where [m, n] = size(Z).

ZI = interp2(Z, ntimes) expands Z by interleaving interpolates between every element, working recursively for ntimes. interp2(Z) is the same as interp2(Z, 1).

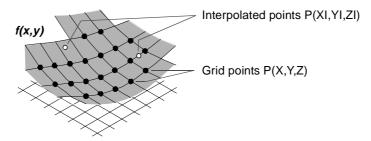
ZI = interp2(X, Y, Z, XI, YI, method) specifies an alternative interpolation method:

- 'linear' for bilinear interpolation (default)
- $\bullet$  ' nearest ' for nearest neighbor interpolation
- $\bullet$   $\,^{\prime}$  cubi  $c^{\prime}\,$  for bicubic interpolation

All interpolation methods require that X and Y be monotonic, and have the same format ("plaid") as if they were produced by meshgrid. Variable spacing is handled by mapping the given values in X, Y, XI, and YI to an equally spaced domain before interpolating. For faster interpolation when X and Y are equally spaced and monotonic, use the methods '\*linear', '\*cubic', or '\*nearest'.

# **Remarks**

The interp2 command interpolates between data points. It finds values of a two-dimensional function f(x,y) underlying the data at intermediate points.

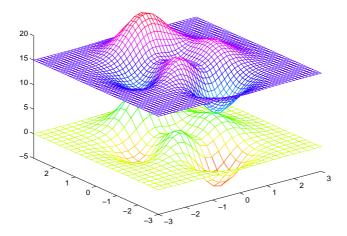


Interpolation is the same operation as table lookup. Described in table lookup terms, the table is tab = [NaN, Y; X, Z] and interp2 looks up the elements of XI in X, YI in Y, and, based upon their location, returns values ZI interpolated within the elements of Z.

# **Examples**

Interpolate the peaks function over a finer grid:

```
 \begin{split} & [\,X,\,Y] = meshgri\,d(-3:\,.\,25:\,3)\,; \\ & Z = peaks(X,\,Y)\,; \\ & [\,XI\,,\,YI\,] = meshgri\,d(-3:\,.\,125:\,3)\,; \\ & ZI = i\,nterp2(X,\,Y,\,Z,\,XI\,,\,YI\,)\,; \\ & mesh(X,\,Y,\,Z)\,, \ hol\,d, \ mesh(XI\,,\,YI\,,\,ZI\,+15) \\ & hol\,d\,off \\ & axi\,s([\,-3\,\,3\,\,-3\,\,3\,\,-5\,\,20]\,) \end{split}
```



Given this set of employee data,

```
years = 1950: 10: 1990;

servi ce = 10: 10: 30;

wage = [150. 697 199. 592 187. 625

179. 323 195. 072 250. 287

203. 212 179. 092 322. 767

226. 505 153. 706 426. 730

249. 633 120. 281 598. 243];
```

it is possible to interpolate to find the wage earned in 1975 by an employee with 15 years' service:

```
w = interp2(service, years, wage, 15, 1975)
w =
   190, 6287
```

See Also	gri ddata	Data gridding

interp1 One-dimensional data interpolation (table lookup)
interp3 Three-dimensional data interpolation (table lookup)
interpn Multidimensional data interpolation (table lookup)
meshgrid Generation of X and Y arrays for three-dimensional

plots.

Three-dimensional data interpolation (table lookup)

### **Syntax**

VI = interp3(X, Y, Z, V, XI, YI, ZI)

VI = interp3(V, XI, YI, ZI) VI = interp3(V, ntimes) VI = interp3(..., method)

### Description

VI = interp3(X, Y, Z, V, XI, YI, ZI) interpolates to find VI, the values of the underlying three-dimensional function V at the points in matrices XI, YI and ZI. Matrices X,Y and Z specify the points at which the data V is given. Out of range values are returned as NaN.

XI, YI, and ZI can be matrices, in which case interp3 returns the values of Z corresponding to the points (XI(i,j), YI(i,j), ZI(i,j)). Alternatively, you can pass in the vectors xi, yi, and zi. Vector arguments that are not the same size are interpreted as if you called meshgrid.

```
VI = interp3(V, XI, YI, ZI) assumes X=1: N, Y=1: M, Z=1: P where [M, N, P]=size(V).
```

VI = interp3(V, ntimes) expands V by interleaving interpolates between every element, working recursively for ntimes iterations. The command interp3(V, 1) is the same as interp3(V).

VI = interp3(..., method) specifies alternative methods:

- $\bullet$  'linear' for linear interpolation (default)
- 'cubi c' for cubic interpolation
- $\bullet$   $\,\,$  ' nearest '  $\,$  for nearest neighbor interpolation

# **Discussion**

All the interpolation methods require that X,Y and Z be monotonic and have the same format ("plaid") as if they were produced by meshgrid. Variable spacing is handled by mapping the given values in X,Y,Z,XI,YI and ZI to an equally spaced domain before interpolating. For faster interpolation when X,Y, and Z are equally spaced and monotonic, use the methods '\*linear', '\*cubic', or '\*nearest'.

# **Examples**

To generate a course approximation of flow and interpolate over a finer mesh:

# See Also

i nterp1	One-dimensional data interpolation (table lookup)
interp2	Two-dimensional data interpolation (table lookup)
interpn	Multidimensional data interpolation (table lookup).
meshgri d	Generate X and Y matrices for three-dimensional plots

# interpft

**Purpose** One-dimensional interpolation using the FFT method

**Syntax** y = interpft(x, n)

y = interpft(x, n, dim)

**Description** y = i nterpft(x, n) returns the vector y that contains the value of the periodic

function x resampled to n equally spaced points.

If l ength(x) = m, and x has sample interval dx, then the new sample interval

for y is

dy = dx\*m/n. Note that n cannot be smaller than m.

If X is a matrix, interpft operates on the columns of X, returning a matrix Y

with the same number of columns as X, but with n rows.

y = i nterpft(x, n, dim) operates along the specified dimension.

**Algorithm** The interpft command uses the FFT method. The original vector x is trans-

formed to the Fourier domain using fft and then transformed back with more

points.

See Also interp1 One-dimensional data interpolation (table lookup)

Multidimensional data interpolation (table lookup)

#### **Syntax**

```
VI = interpn(X1, X2, X3, ..., V, Y1, Y2, Y3, ...)

VI = interpn(V, V1, V2, V3, ...)
```

VI = interpn(V, Y1, Y2, Y3, ...)

VI = interpn(V, ntimes)
VI = interpn(..., method)

# Description

Y1, Y2, Y3,... can be matrices, in which case interpn returns the values of VI corresponding to the points (Y1(i,j),Y2(i,j),Y3(i,j),...). Alternatively, you can pass in the vectors y1, y2, y3,... In this case, interpn interprets these vectors as if you issued the command ndgrid(y1,y2,y3,...).

```
VI = interpn(V, Y1, Y2, Y3, ...) interpolates as above, assuming X1 = 1: size(V, 1), X2 = 1: size(V, 2), X3 = 1: size(V, 3), and so on.
```

VI = interpn(V, ntimes) expands V by interleaving interpolates between each element, working recursively for ntimes iterations. interpn(V, 1) is the same as interpn(V).

VI = interpn(..., method) specifies alternative methods:

- 'linear' for linear interpolation (default)
- 'cubi c' for cubic interpolation
- $\bullet$   $\,$  'nearest' for nearest neighbor interpolation

#### Discussion

All the interpolation methods require that X,Y and Z be monotonic and have the same format ("plaid") as if they were produced by ndgrid. Variable spacing is handled by mapping the given values in X1,X2,X3,... and Y1,Y2,Y3,... to an equally spaced domain before interpolating. For faster interpolation when X1,X2,Y3, and so on are equally spaced and monotonic, use the methods '\*linear', '\*cubic', or '\*nearest'.

# interpn

# See Also

interp1 interp2 ndgrid One-dimensional data interpolation (table lookup) Two-dimensional data interpolation (table lookup) Generate arrays for multidimensional functions and

interpolation

**Purpose** Set intersection of two vectors

# **Syntax**

```
c = intersect(a, b)
c = intersect(A, B, 'rows')
[c,ia,ib] = intersect(...)
```

# **Description**

c=i ntersect (a,b) returns the values common to both a and b. The resulting vector is sorted in ascending order. In set theoretic terms, this is  $a\cap b$ .

c = intersect(A, B, 'rows') when A and B are matrices with the same number of columns returns the rows common to both A and B.

[c, ia, ib] = intersect(a, b) also returns column index vectors ia and ib such that c = a(ia) and c = b(ib) (or c = a(ia, :) and c = b(ib, :)).

# **Examples**

```
A = [1 2 3 6]; B = [1 2 3 4 6 10 20];

[c, ia, ib] = intersect(A, B);

disp([c; ia; ib])

1 2 3 6

1 2 3 4

1 2 3 5
```

#### See Also

ismember	True for a set member
setdiff	Return the set difference of two vectors
setxor	Set exclusive-or of two vectors
uni on	Set union of two vectors
uni que	Unique elements of a vector

Matrix inverse

**Syntax** 

Y = i nv(X)

Description

 $Y = i \, nv(X)$  returns the inverse of the square matrix X. A warning message is printed if X is badly scaled or nearly singular.

In practice, it is seldom necessary to form the explicit inverse of a matrix. A frequent misuse of i nv arises when solving the system of linear equations Ax = b. One way to solve this is with x = i nv(A)\*b. A better way, from both an execution time and numerical accuracy standpoint, is to use the matrix division operator  $x = A \ b$ . This produces the solution using Gaussian elimination, without forming the inverse. See  $\ and \ for$  further information.

# **Examples**

Here is an example demonstrating the difference between solving a linear system by inverting the matrix with i nv(A)\*b and solving it directly with  $A \setminus b$ . A matrix A of order 100 has been constructed so that its condition number, cond(A), is 1. e10, and its norm, norm(A), is 1. The exact solution x is a random vector of length 100 and the right-hand side is b = A\*x. Thus the system of linear equations is badly conditioned, but consistent.

On a 20 MHz 386SX notebook computer, the statements

err = norm(z-x)res = norm(A\*z-b)

#### produce

```
elapsed_time = 3.9500
err = 6.6161e-08
res = 9.1103e-16
```

It takes almost two and one half times as long to compute the solution with  $y = i \, nv(A) *b$  as with  $z = A \b$ . Both produce computed solutions with about the same error, 1. e–7, reflecting the condition number of the matrix. But the size of the residuals, obtained by plugging the computed solution back into the original equations, differs by several orders of magnitude. The direct solution produces residuals on the order of the machine accuracy, even though the system is badly conditioned.

The behavior of this example is typical. Using  $A \setminus b$  instead of  $i \operatorname{nv}(A) * b$  is two to three times as fast and produces residuals on the order of machine accuracy, relative to the magnitude of the data.

# **Algorithm**

The i nv command uses the subroutines ZGEDI and ZGEFA from LINPACK. For more information, see the *LINPACK Users' Guide*.

# **Diagnostics**

From inv, if the matrix is singular,

```
Matrix is singular to working precision.
```

On machines with IEEE arithmetic, this is only a warning message. inv then returns a matrix with each element set to Inf. On machines without IEEE arithmetic, like the VAX, this is treated as an error.

If the inverse was found, but is not reliable, this message is displayed.

```
Warning: Matrix is close to singular or badly scaled. Results may be inaccurate. RCOND = xxx
```

# inv

See Also

Matrix left division (backslash)

Matrix right division (slash)

 $\begin{array}{lll} \text{det} & & \text{Matrix determinant} \\ \text{lu} & & \text{LU matrix factorization} \\ \text{rref} & & \text{Reduced row echelon form} \end{array}$ 

**References** [1] Dongarra, J.J., J.R. Bunch, C.B. Moler, and G.W. Stewart, *LINPACK Users*'

Guide, SIAM, Philadelphia, 1979.

**Purpose** Inverse of the Hilbert matrix

**Syntax** H = i nvhi l b(n)

**Description** H = i nvhi l b(n) generates the exact inverse of the exact Hilbert matrix for n

less than about 15. For larger n, i  $nvhi\ l\ b(n)$  generates an approximation to the

inverse Hilbert matrix.

**Limitations** The exact inverse of the exact Hilbert matrix is a matrix whose elements are large integers. These integers may be represented as floating-point numbers

without roundoff error as long as the order of the matrix, n, is less than 15.

Comparing i nvhilb(n) with inv(hilb(n)) involves the effects of two or three sets of roundoff errors:

• The errors caused by representing hilb(n)

• The errors in the matrix inversion process

• The errors, if any, in representing i nvhilb(n)

It turns out that the first of these, which involves representing fractions like 1/3 and 1/5 in floating-point, is the most significant.

**Examples** invhilb(4) is

$$\begin{array}{ccccc} 16 & -120 & 240 & -140 \\ -120 & 1200 & -2700 & 1680 \\ 240 & -2700 & 6480 & -4200 \\ -140 & 1680 & -4200 & 2800 \end{array}$$

See Also hilb Hilbert matrix

**References** [1] Forsythe, G. E. and C. B. Moler, *Computer Solution of Linear Algebraic Systems*, Prentice-Hall, 1967, Chapter 19.

# ipermute

**Purpose** 

Inverse permute the dimensions of a multidimensional array

**Syntax** 

A = ipermute(B, order)

Description

 $A = i \ permute(B, order)$  is the inverse of permute.  $i \ permute$  rearranges the dimensions of B so that permute(A, order) will produce B. B has the same values as A but the order of the subscripts needed to access any particular element are rearranged as specified by order. All the elements of order must be unique.

Remarks

permute and i permute are a generalization of transpose (. ') for multidimensional arrays.

**Examples** 

Consider the 2-by-2-by-3 array a:

```
a = cat(3, eye(2), 2*eye(2), 3*eye(2))
a(:,:,1) =
                       a(:,:,2) =
     1
           0
                           2
                                  0
     0
                           0
                                  2
           1
a(:,:,3) =
     3
           0
     0
           3
```

Permuting and inverse permuting a in the same fashion restores the array to its original form:

```
B = permute(a, [3 2 1]);
C = i permute(B, [3 2 1]);
i sequal(a, C)
ans=
```

1

See Also

permute

Rearrange the dimensions of a multidimensional array

#### **Detect state**

### **Syntax**

k = i slogical(A)
TF = i snan(A)
k = i snumeric(A)
k = i sobj ect(A)
k = i sppc
TF = i sprime(A)
k = i sreal(A)
TF = isspace('str')
k = issparse(S)
k = i sstruct(S)
k = i sstudent
k = i suni x
k = i svms

# **Description**

 $k = i \, scell(C)$  returns logical true (1) if C is a cell array and logical false (0) otherwise.

 $k = i \, scel \, l \, str(S)$  returns logical true (1) if S is a cell array of strings and logical false (0) otherwise. A cell array of strings is a cell array where every element is a character array.

 $k = i \operatorname{schar}(S)$  returns logical true (1) if S is a character array and logical false (0) otherwise.

 $k=i\ sempty(A)$  returns logical true (1) if A is an empty array and logical false (0) otherwise. An empty array has at least one dimension of size zero, for example, 0-by-0 or 0-by-5.

k = i sequal (A, B, ...) returns logical true (1) if the input arrays are the same type and size and hold the same contents, and logical false (0) otherwise.

k = i sfield(S, 'field') returns logical true (1) if field is the name of a field in the structure array S.

TF = i sfi ni te(A) returns an array the same size as A containing logical true (1) where the elements of the array A are finite and logical false (0) where they are infinite or NaN.

For any A, exactly one of the three quantities i s f i n i t e(A), i s i n f(A), and i s n a n(A) is equal to one.

k = i sgl obal (NAME) returns logical true (1) if NAME has been declared to be a global variable, and logical false (0) if it has not been so declared.

 $TF = i \, shandl \, e(H)$  returns an array the same size as H that contains logical true (1) where the elements of H are valid graphics handles and logical false (0)where they are not.

k=i shold returns logical true (1) if hold is on, and logical false (0) if it is of f. When hold is on, the current plot and all axis properties are held so that subsequent graphing commands add to the existing graph. hold on means the Next-Plot property of both figure and axes is set to add.

k = i si eee returns logical true (1) on machines with IEEE arithmetic (e.g., IBM PC, most UNIX workstations, Macintosh) and logical false (0) on machines without IEEE arithmetic (e.g., VAX, Cray).

 $TF = i \sin nf(A)$  returns an array the same size as A containing logical true (1) where the elements of A are +I nf or -I nf and logical false (0) where they are not.

TF = i sl etter('str') returns an array the same size as 'str' containing logical true (1) where the elements of str are letters of the alphabet and logical false (0) where they are not.

k = i sl ogi cal (A) returns logical true (1) if A is a logical array and logical false (0) otherwise.

TF = i snan(A) returns an array the same size as A containing logical true (1) where the elements of A are NaNs and logical false (0) where they are not.

k = i snumeri c(A) returns logical true (1) if A is a numeric array and logical false (0) otherwise. For example, sparse arrays, and double precision arrays are numeric while strings, cell arrays, and structure arrays are not.

k = i sobject (A) returns logical true (1) if A is an object and logical false (0) otherwise.

 $k = i \, sppc \, returns \, logical \, true \, (1) \, if \, the \, computer \, running \, MATLAB \, is \, a \, Macintosh \, Power \, PC \, and \, logical \, false \, (0) \, otherwise.$ 

 $TF = i \operatorname{sprime}(A)$  returns an array the same size as A containing logical true (1) for the elements of A which are prime, and logical false (0) otherwise.

k = i sreal (A) returns logical true (1) if all elements of A are real numbers, and logical false (0) if either A is not a numeric array, or if any element of A has a nonzero imaginary component. Since strings are a subclass of numeric arrays, i sreal always returns 1 for a string input.

Because MATLAB supports complex arithmetic, certain of its functions can introduce significant imaginary components during the course of calculations that appear to be limited to real numbers. Thus, you should use i sreal with discretion.

TF = i sspace('str') returns an array the same size as 'str' containing logical true (1) where the elements of str are ASCII white spaces and logical false (0) where they are not. White spaces in ASCII are space, newline, carriage return, tab, vertical tab, or formfeed characters.

 $k = i \, ssparse(S)$  returns logical true (1) if the storage class of S is sparse and logical false (0) otherwise.

k = i sstruct(S) returns logical true (1) if S is a structure and logical false (0) otherwise.

k=i sstudent returns logical true (1) for student editions of MATLAB and logical false (0) for commercial editions.

k = i suni x returns logical true (1) for UNIX versions of MATLAB and logical false (0) otherwise.

k=i svms returns logical true (1) for VMS versions of MATLAB and logical false (0) otherwise.

# **Examples**

```
s = 'A1, B2, C3';
isletter(s)
ans =
    1   0   0   1   0   0   1   0
B = rand(2, 2, 2);
B(:,:,:) = [];
i sempty(B)
ans =
    1
```

#### Given,

i sequal (A, B, C) returns 0, and i sequal (A, B) returns 1.

#### Let

$$a = [-2 \quad -1 \quad 0 \quad 1 \quad 2]$$

#### Then

```
i s f i n i t e (1./a) = [1 \ 1 \ 0 \ 1 \ 1]

i s i n f (1./a) = [0 \ 0 \ 1 \ 0 \ 0]

i s n a n (1./a) = [0 \ 0 \ 0 \ 0]
```

#### and

```
i s f i n i t e (0./a) = [1 \ 1 \ 0 \ 1 \ 1]

i s i n f (0./a) = [0 \ 0 \ 0 \ 0]

i s n a n (0./a) = [0 \ 0 \ 1 \ 0 \ 0]
```

**Purpose** Detect an object of a given class

**Syntax** K = i sa(obj, 'class\_name')

**Description** K = i sa(obj, 'cl ass\_name') returns logical true (1) if obj is of class (or a

subclass of) class\_name, and logical false (0) otherwise.

The argument  $class_name$  is the name of a user-defined or pre-defined class of

objects. Predefined MATLAB classes include:

cell Multidimensional cell array

doubl e Multidimensional double precision array

sparse Two-dimensional real (or complex) sparse array

char Array of alphanumeric characters

struct Structure

' class\_name' User-defined object class

**Examples** i sa(rand(3, 4), 'double') returns 1.

See Also class Create object or return class of object

# ismember

**Purpose** 

Detect members of a set

**Syntax** 

k = i smember(a, S)

k = ismember(A, S, 'rows')

**Description** 

k=i smember (a, S) returns an vector the same length as a containing logical true (1) where the elements of a are in the set S, and logical false (0) elsewhere. In set theoretic terms, k is 1 where  $a \in S$ .

 $k=i\ smember(A,S,'rows')$  when A and S are matrices with the same number of columns returns a vector containing 1 where the rows of A are also rows of S and 0 otherwise.

# **Examples**

```
set = [0 2 4 6 8 10 12 14 16 18 20];
a = reshape(1:5, [5 1])
```

a =

1

2

3

4 5

ismember(a, set)

ans =

0

1

0

1

0

#### See Also

 $i\,ntersect \hspace{1.5cm} Set\,\,intersection\,\,of\,\,two\,\,vectors$ 

set difference of two vectors

set xor Set exclusive-or of two vectors

uni on Set union of two vectors

uni que Unique elements of a vector

# isstr

Purpose Detect strings

**Description** This MATLAB 4 function has been renamed i schar in MATLAB 5.

See Also is\* Detect state

Purpose Imaginary unit

Syntax j

x+yj x+j \*y

**Description** 

Use the character j in place of the character i, if desired, as the imaginary unit.

As the basic imaginary unit sqrt(-1), j is used to enter complex numbers. Since j is a function, it can be overridden and used as a variable. This permits you to use j as an index in for loops, etc.

It is possible to use the character j without a multiplication sign as a suffix in forming a numerical constant.

**Examples** 

Z = 2+3j Z = x+j\*y Z = r\*exp(j\*theta)

See Also

conj Complex conjugate i Imaginary unit

i mag Imaginary part of a complex number

real Real part of complex number

# keyboard

**Purpose** Invoke the keyboard in an M-file

Syntax keyboard

**Description** keyboard , when placed in an M-file, stops execution of the file and gives

control to the keyboard. The special status is indicated by a K appearing before the prompt. You can examine or change variables; all MATLAB commands are

valid. This keyboard mode is useful for debugging your M-files.

To terminate the keyboard mode, type the command:

return

then press the Return key.

**See Also** dbstop Set breakpoints in an M-file function

 $\begin{array}{ll} i \; nput & Request \; user \; input \\ qui \; t & Terminate \; MATLAB \end{array}$ 

return Terminate keyboard mode

Kronecker tensor product

**Syntax** 

$$K = kron(X, Y)$$

**Description** 

K = kron(X, Y) returns the Kronecker tensor product of X and Y. The result is a large array formed by taking all possible products between the elements of X and those of Y. If X is m-by-n and Y is p-by-q, then kron(X, Y) is m\*p-by-n\*q.

**Examples** 

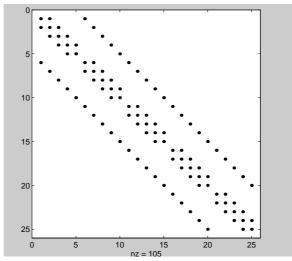
If X is 2-by-3, then kron(X, Y) is

```
 \begin{bmatrix} X(1,1) * Y & X(1,2) * Y & X(1,3) * Y \\ X(2,1) * Y & X(2,2) * Y & X(2,3) * Y \end{bmatrix}
```

The matrix representation of the discrete Laplacian operator on a two-dimensional, n-by-n grid is a  $n^2$ -by- $n^2$  sparse matrix. There are at most five nonzero elements in each row or column. The matrix can be generated as the Kronecker product of one-dimensional difference operators with these statements:

```
I = speye(n, n);
E = sparse(2: n, 1: n-1, 1, n, n);
D = E+E' -2*I;
A = kron(D, I) + kron(I, D);
```

Plotting this with the spy function for n = 5 yields:



Last error message

#### **Syntax**

```
str = lasterr
lasterr('')
```

#### Description

str = lasterr returns the last error message generated by MATLAB.

lasterr('') resets lasterr so it returns an empty matrix until the next error occurs.

# **Examples**

Here is a function that examines the lasterr string and displays its own message based on the error that last occurred. This example deals with two cases, each of which is an error that can result from a matrix multiply.

```
function catch
l = lasterr;
j = findstr(l, 'Inner matrix dimensions');
if j ~=[]
    disp('Wrong dimensions for matrix multiply')
else
    k = findstr(l, 'Undefined function or variable')
    if (k~=[])
        disp('At least one operand does not exist')
    end
end
```

The lasterr function is useful in conjunction with the two-argument form of the eval function:

```
eval ('str', 'catchstr')
```

where *catchstr* examines the lasterr string to determine the cause of the error and take appropriate action. The eval function evaluates the string str and returns if no error occurs. If an error occurs, eval executes *catchstr*. Using eval with the catch function above:

```
clear A = [1 \ 2 \ 3; \ 6 \ 7 \ 2; \ 0 \ -1 \ 5]; \\ B = [9 \ 5 \ 6; \ 0 \ 4 \ 9]; \\ eval('A*B', 'catch')
```

 $MATLAB \ responds \ with \ Wrong \ dimensions \ for \ matrix \ multiply.$ 

See Also error Display error messages

eval Interpret strings containing MATLAB expressions

# **Icm**

**Purpose** Least common multiple

**Syntax** L = l cm(A, B)

**Description** L = 1 cm(A, B) returns the least common multiple of corresponding elements of

arrays A and B. Inputs A and B must contain positive integer elements and must

be the same size (or either can be scalar).

Examples l cm(8, 40)

ans = 40

lcm(pascal(3), magic(3))

ans =

8 1 6 3 10 21 4 9 6

See Also gcd Greatest common divisor

**Associated Legendre functions** 

Syntax

**Definition** 

The Legendre functions are defined by:

$$P_n^m(x) = (-1)^m (1-x^2)^{m/2} \frac{d^m}{dx^m} P_n(x)$$

where  $P_n(x)$  is the Legendre polynomial of degree n:

$$P_n(x) = \frac{1}{2^n n!} \left[ \frac{d^n}{dx} (x^2 - 1)^n \right]$$

The Schmidt seminormalized associated Legendre functions are related to the nonnormalized associated Legendre functions  $P_n^m(x)$  by:

$$S_n^m(x) = \sqrt{\frac{2(n-m)!}{(n+m)!}} P_n^m(x)$$

**Description** 

 $P = l \, egendre(n, X)$  computes the associated Legendre functions of degree n and order  $m = 0, 1, \ldots, n$ , evaluated at X. Argument n must be a scalar integer less than 256, and X must contain real values in the domain  $-1 \le X \le 1$ .

The returned array P has one more dimension than X, and each element P(m+1,d1,d2...) contains the associated Legendre function of degree n and order m evaluated at X(d1,d2...).

If X is a vector, then P is a matrix of the form:

$$P_2^0(x(1))$$
  $P_2^0(x(2))$   $P_2^0(x(3))$  ...  $P_2^1(x(1))$   $P_2^1(x(2))$   $P_2^1(x(3))$  ...

$$P_2^2(x(1))$$
  $P_2^2(x(2))$   $P_2^2(x(3))$  ...

# legendre

S = legendre(..., 'sch') computes the Schmidt seminormalized associated Legendre functions  $S_n^m(x)$ .

# **Examples**

The statement legendre (2, 0: 0. 1: 0. 2) returns the matrix:

	x = 0	x = 0.1	x = 0.2
m = 0	0. 5000	0. 4850	0. 4400
m = 1	0	0. 2985	0. 5879
m = 2	3. 0000	2. 9700	2. 8800

Note that this matrix is of the form shown at the bottom of the previous page. Given,

Then size(P) is 3-by-2-by-4-by-5, and P(:, 1, 2, 3) is the same as l egendre(n, X(1, 2, 3)).

Purpose Length of vector

**Syntax**  $n = l \operatorname{ength}(X)$ 

 $\textbf{Description} \qquad \qquad \text{The statement 1 ength}(X) \ \ \text{is equivalent to } \max(\operatorname{size}(X)) \ \ \text{for nonempty arrays}$ 

and 0 for empty arrays.

 $n = l \, \text{ength}(X)$  returns the size of the longest dimension of X. If X is a vector, this is the same as its length.

**Examples** x = ones(1, 8);

n = length(x)
n =
 8

x = rand(2, 10, 3);n = length(x)

n = 10

See Also

ndi ms Number of array dimensions

si ze Array dimensions

# lin2mu

**Purpose** Linear to mu-law conversion

Syntax mu = li n2mu(y)

**Description** mu = li n2mu(y) converts linear audio signal amplitudes in the range

 $-1 \le Y \le 1$  to mu-law encoded "flints" in the range  $0 \le mu \le 255$ .

See Also Write NeXT/SUN (. au) sound file

mu2l i n Mu-law to linear conversion

**Purpose** Generate linearly spaced vectors

**Syntax** y = linspace(a, b)

y = linspace(a, b, n)

**Description** The linspace function generates linearly spaced vectors. It is similar to the

colon operator ":", but gives direct control over the number of points.

y = linspace(a, b) generates a row vector y of 100 points linearly spaced

between a and b.

y = linspace(a, b, n) generates n points.

See Also : (Colon) Create vectors, matrix subscripting, and for iterations

logspace Generate logarithmically spaced vectors

Retrieve variables from disk

## **Syntax**

l oad

load filename load (filename) load filename.ext load filename -ascii load filename -mat

### Description

The load and save commands retrieve and store MATLAB variables on disk.

load by itself, loads all the variables saved in the file 'matlab. mat'.

load filename retrieves the variables from 'filename. mat' given a full pathname or a MATLABPATH relative partial pathname.

load (filename) loads a file whose name is stored in filename. The statements:

```
str = 'filename.mat'; load (str)
```

retrieve the variables from the binary file 'filename. mat'.

load filename. ext reads ASCII files that contain rows of space separated values. The resulting data is placed into an variable with the same name as the file (without the extension). ASCII files may contain MATLAB comments (lines that begin with %).

load filename -ascii or load filename -mat can be used to force load to treat the file as either an ASCII file or a MAT file.

#### Remarks

MAT-files are double-precision binary MATLAB format files created by the save command and readable by the 1 oad command. They can be created on one machine and later read by MATLAB on another machine with a different floating-point format, retaining as much accuracy and range as the disparate formats allow. They can also be manipulated by other programs, external to MATLAB.

The Application Program Interface Libraries contain C and Fortran callable routines to read and write MAT-files from external programs.

fscanf Read formatted data from file save Save workspace variables on disk

spconvert Import matrix from sparse matrix external format

See also partialpath.

# log

**Purpose** 

Natural logarithm

**Syntax** 

$$Y = log(X)$$

**Description** 

The  $\log$  function operates element-wise on arrays. Its domain includes complex and negative numbers, which may lead to unexpected results if used unintentionally.

 $Y = l \circ g(X)$  returns the natural logarithm of the elements of X. For complex or negative z, where z = x + y\*i, the complex logarithm is returned:

$$log(z) = log(abs(z)) + i*atan2(y, x)$$

**Examples** 

The statement abs(log(-1)) is a clever way to generate  $\pi$ :

See Also

exp Exponential

l og 10 Common (base 10) logarithm

l og2 Base 2 logarithm and dissect floating-point numbers

into exponent and mantissa

l ogm Matrix logarithm

Base 2 logarithm and dissect floating-point numbers into exponent and mantissa  $\,$ 

**Syntax** 

$$Y = \log 2(X)$$
$$[F, E] = \log 2(X)$$

**Description** 

Y = log2(X) computes the base 2 logarithm of the elements of X.

 $[F, E] = \log 2(X)$  returns arrays F and E. Argument F is an array of real values, usually in the range  $0.5 \le abs(F) < 1$ . For real X, F satisfies the equation: X = F. \*2. ^E. Argument E is an array of integers that, for real X, satisfy the equation: X = F. \*2. ^E.

Remarks

This function corresponds to the ANSI C function frexp() and the IEEE floating-point standard function logb(). Any zeros in X produce F=0 and E=0.

**Examples** 

For IEEE arithmetic, the statement [F, E] = log2(X) yields the values:

X	F	E
1	1/2	1
pi	pi /4	2
-3	-3/4	2
eps	1/2	-51
real max	1-eps/2	1024
real mi n	1/2	-1021

See Also

l og Natural logarithm
pow2 Base 2 power and scale floating-point numbers

# log10

Purpose Common (base 10) logarithm

**Syntax** Y = l og 10(X)

**Description** The log10 function operates element-by-element on arrays. Its domain

includes complex numbers, which may lead to unexpected results if used unin-

tentionally.

Y = log10(X) returns the base 10 logarithm of the elements of X.

**Examples** On a computer with IEEE arithmetic

log10(real max) is 308.2547

and

log10(eps) is -15.6536

See Also exp Exponential

l og Natural logarithm

l og2 Base 2 logarithm and dissect floating-point numbers

into exponent and mantissa

l ogm Matrix logarithm

Convert numeric values to logical

**Syntax** 

K = logical(A)

Description

 $K = 1 \, \mathrm{ogi} \, \mathrm{cal} \, (A)$  returns an array that can be used for logical indexing or logical tests. The array K is the same size as A and is displayed using A where corresponding elements of A are nonzero, and A0 where corresponding elements of A0 are zero.

Remarks

Logical arrays are also created by the relational operators ( $==,<,>,\sim$ , etc.) and functions like any, all, i snan, i sinf, and i sfinite.

**Examples** 

Given  $A = [1\ 2\ 3;\ 4\ 5\ 6;\ 7\ 8\ 9]$ , the statement  $B = l\,ogi\,cal\,(eye(3))$  returns a logical array

which can be used in logical indexing that returns A's diagonal elements:

A(B)

ans =
1
5
9

However, attempting to index into A using the *numeric* array eye(3) results in:

A(eye(3))

??? Index into matrix is negative or zero.

Matrix logarithm

**Syntax** 

$$Y = logm(X)$$

[Y, esterr] = logm(X)

Description

 $Y = l \circ gm(X)$  returns the matrix logarithm: the inverse function of expm(X). Complex results are produced if X has negative eigenvalues. A warning message is printed if the computed expm(Y) is not close to X.

[Y, esterr] =  $l \circ gm(X)$  does not print any warning message, but returns an estimate of the relative residual, norm(expm(Y) - X) / norm(X).

Remarks

If X is real symmetric or complex Hermitian, then so is  $l \circ gm(X)$ .

Some matrices, like  $X = [0 \ 1; \ 0 \ 0]$ , do not have any logarithms, real or complex, and  $l \circ gm$  cannot be expected to produce one.

Limitations

For most matrices:

$$logm(expm(X)) = X = expm(logm(X))$$

These identities may fail for some X. For example, if the computed eigenvalues of X include an exact zero, then  $l \circ gm(X)$  generates infinity. Or, if the elements of X are too large, expm(X) may overflow.

**Examples** 

Suppose A is the 3-by-3 matrix

and  $X = \exp(A)$  is

Then A = logm(X) produces the original matrix A.

A =

1.0000	1. 0000	0.0000
0	0	2.0000
0	0	-1.0000

But  $l \circ g(X)$  involves taking the logarithm of zero, and so produces

ans =

# **Algorithm**

The matrix functions are evaluated using an algorithm due to Parlett, which is described in [1]. The algorithm uses the Schur factorization of the matrix and may give poor results or break down completely when the matrix has repeated eigenvalues. A warning message is printed when the results may be inaccurate.

#### See Also

expm Matrix exponential
funm Evaluate functions of a matrix
sqrtm Matrix square root

### References

[1] Golub, G. H. and C. F. Van Loan, *Matrix Computation*, Johns Hopkins University Press, 1983, p. 384.

[2] Moler, C. B. and C. F. Van Loan, "Nineteen Dubious Ways to Compute the Exponential of a Matrix," *SIAM Review* 20, 1979,pp. 801-836.

# logspace

**Purpose** Generate logarithmically spaced vectors

**Syntax** y = logspace(a, b)

y = logspace(a, b, n) y = logspace(a, pi)

**Description** The logspace function generates logarithmically spaced vectors. Especially

useful for creating frequency vectors, it is a logarithmic equivalent of l i nspace

and the ":" or colon operator.

y = logspace(a, b) generates a row vector y of 50 logarithmically spaced

points between decades 10<sup>a</sup> and 10<sup>b</sup>.

y = 1 ogspace(a, b, n) generates n points between decades  $10^a$  and  $10^b$ .

y = logspace(a, pi) generates the points between  $10^a$  and pi, which is useful for digital signal processing where frequencies over this interval go

around the unit circle.

**Remarks** All the arguments to logspace must be scalars.

**See Also** : (Colon) Create vectors, matrix subscripting, and for iterations

linspace Generate linearly spaced vectors

**Purpose** Keyword search through all help entries

**Syntax** lookfor topic

lookfor topic -all

**Description** lookfor topic searches for the string topic in the first comment line (the H1

line) of the help text in all M-files found on MATLAB's search path. For all files

in which a match occurs, lookfor displays the H1 line.

lookfor topic -all searches the entire first comment block of an M-file

looking for topi c.

**Examples** For example

lookfor inverse

finds at least a dozen matches, including H1 lines containing "inverse hyperbolic cosine," "two-dimensional inverse FFT," and "pseudoinverse." Contrast this with

which inverse

or

what inverse

These commands run more quickly, but probably fail to find anything because MATLAB does not ordinarily have a function i nverse.

In summary, what lists the functions in a given directory, whi ch finds the directory containing a given function or file, and lookfor finds all functions in all directories that might have something to do with a given keyword.

See Also di r Directory listing

hel p Online help for MATLAB functions and M-files what Directory listing of M-files, MAT-files, and MEX-files

whi ch Locate functions and files

who List directory of variables in memory

# **lower**

**Purpose** Convert string to lower case

Syntax t = lower('str')

**Description** t = lower('str') returns the string formed by converting any upper-case

characters in str to the corresponding lower-case characters and leaving all

other characters unchanged.

**Examples** lower('MathWorks') is mathworks.

**Remarks** Character sets supported:

Mac: Standard RomanPC: Windows Latin-1

• Other: ISO Latin-1 (ISO 8859-1)

See Also upper Convert string to upper case

Least squares solution in the presence of known covariance

**Syntax** 

$$x = 1 \operatorname{scov}(A, b, V)$$
  
 $[x, dx] = 1 \operatorname{scov}(A, b, V)$ 

Description

 $x = 1 \operatorname{scov}(A, b, V)$  returns the vector x that solves A\*x = b + e where e is normally distributed with zero mean and covariance V. Matrix A must be m-by-n where m > n. This is the over-determined least squares problem with covariance V. The solution is found without inverting V.

 $[x, dx] = 1 \operatorname{scov}(A, b, V)$  returns the standard errors of x in dx. The standard statistical formula for the standard error of the coefficients is:

$$mse = B'*(i nv(V) - i nv(V) *A*i nv(A'*i nv(V) *A) *A'*i nv(V)) *B. /(m-n)$$
  
 $dx = sqrt(di ag(i nv(A'*i nv(V) *A) *mse))$ 

Algorithm

The vector x minimizes the quantity (A\*x-b)'\*inv(V)\*(A\*x-b). The classical linear algebra solution to this problem is

$$x = i nv(A' *i nv(V) *A) *A' *i nv(V) *b$$

but the 1 scov function instead computes the QR decomposition of A and then modifies Q by V.

See Also

\ Matrix left division (backslash) nnlsNonnegative least squares

Orthogonal-triangular decomposition qr

Reference

Strang, G., Introduction to Applied Mathematics, Wellesley-Cambridge, 1986, p. 398.

LU matrix factorization

## **Syntax**

$$[L, U] = l u(X)$$

$$[L, U, P] = l u(X)$$

$$l u(X)$$

## **Description**

The  $1\,\mathrm{u}$  function expresses any square matrix X as the product of two essentially triangular matrices, one of them a permutation of a lower triangular matrix and the other an upper triangular matrix. The factorization is often called the LU, or sometimes the LR, factorization.

[L, U] = lu(X) returns an upper triangular matrix in U and a psychologically lower triangular matrix (i.e., a product of lower triangular and permutation matrices) in L, so that X = L\*U.

[L, U, P] = lu(X) returns an upper triangular matrix in U, a lower triangular matrix in L, and a permutation matrix in P, so that L\*U = P\*X.

lu(X) returns the output from the LINPACK routine ZGEFA.

## Remarks

Most of the algorithms for computing LU factorization are variants of Gaussian elimination. The factorization is a key step in obtaining the inverse with i nv and the determinant with  $\det$ . It is also the basis for the linear equation solution or matrix division obtained with  $\setminus$  and /.

# **Arguments**

- L A factor of X. Depending on the form of the function, L is either lower triangular, or else the product of a lower triangular matrix with a permutation matrix P.
- U An upper triangular matrix that is a factor of X.
- P The permutation matrix satisfying the equation  $L^*U = P^*X$ .

# **Examples**

Start with

To see the LU factorization, call l u with two output arguments:

Notice that L is a permutation of a lower triangular matrix that has 1's on the permuted diagonal, and that U is upper triangular. To check that the factorization does its job, compute the product:

L\*U

which returns the original A. Using three arguments on the left-hand side to get the permutation matrix as well

$$[L, U, P] = lu(A)$$

returns the same value of U, but L is reordered:

L =					
	1.00	00		0	0
	0. 1429		1. 0	0000	0
0. 5714		14	0. 5	5000	1. 0000
U =					
	7. 00	00	8. 0	0000	0
		0	0. 8	3571	3. 0000
		0		0	4. 5000
P =					
	0	0	1		
	1	0	0		
	0	1	0		

To verify that L\*U is a permuted version of A, compute L\*U and subtract it from P\*A:

$$P*A - L*U$$

The inverse of the example matrix, X = i nv(A), is actually computed from the inverses of the triangular factors:

$$X = i nv(U) *i nv(L)$$

The determinant of the example matrix is

$$d = det(A)$$

which gives

It is computed from the determinants of the triangular factors:

$$d = det(L) * det(U)$$

The solution to Ax = b is obtained with matrix division:

$$\mathbf{x} = \mathbf{A} \setminus \mathbf{b}$$

The solution is actually computed by solving two triangular systems:

$$y = L \setminus b, x = U \setminus y$$

## **Algorithm**

l u uses the subroutines ZGEDI and ZGEFA from LINPACK. For more information, see the *LINPACK Users' Guide*.

#### See Also

\ Matrix left division (backslash)
/ Matrix right division (slash)

cond Condition number with respect to inversion

det Matrix determinant i nv Matrix inverse

qr Orthogonal-triangular decomposition

rref Reduced row echelon form

#### References

[1] Dongarra, J.J., J.R. Bunch, C.B. Moler, and G.W. Stewart, *LINPACK Users' Guide*, SIAM, Philadelphia, 1979.

Incomplete LU matrix factorizations

## **Syntax**

```
lui nc(X, '0')
[L, U] = lui nc(X, '0')
[L, U, P] = lui nc(X, '0')
lui nc(X, droptol)
lui nc(X, opti ons)
[L, U] = lui nc(X, opti ons)
[L, U] = lui nc(X, droptol)
[L, U, P] = lui nc(X, opti ons)
[L, U, P] = lui nc(X, opti ons)
```

## Description

 $l\,ui\,nc$  produces a unit lower triangular matrix, an upper triangular matrix, and a permutation matrix.

lui nc(X, '0') computes the incomplete LU factorization of level 0 of a square sparse matrix. The triangular factors have the same sparsity pattern as the permutation of the original sparse matrix X, and their product agrees with the permutated X over its sparsity pattern. lui nc(X, '0') returns the strict lower triangular part of the factor and the upper triangular factor embedded within the same matrix. The permutation information is lost, but nnz(luinc(X, '0')) = nnz(X), with the possible exception of some zeros due to cancellation.

 $[L,U]=1\,\mathrm{ui}\,\mathrm{nc}(X,\,{}^{'}\,0^{'})$  returns the product of permutation matrices and a unit lower triangular matrix in L and an upper triangular matrix in U. The exact sparsity patterns of L, U, and X are not comparable but the number of nonzeros is maintained with the possible exception of some zeros in L and U due to cancellation:

```
nnz(L) + nnz(U) = nnz(X) + n, where X is n-by-n.
```

The product L\*U agrees with X over its sparsity pattern. (L\*U) . \*spones(X) –X has entries of the order of eps.

 $[L, U, P] = 1 \, ui \, nc(X, '0')$  returns a unit lower triangular matrix in L, an upper triangular matrix in U and a permutation matrix in P. L has the same sparsity pattern as the lower triangle of the permuted X

```
spones(L) = spones(tril(P*X))
```

with the possible exceptions of 1's on the diagonal of L where P\*X may be zero, and zeros in L due to cancellation where P\*X may be nonzero. U has the same sparsity pattern as the upper triangle of P\*X

```
spones(U) = spones(triu(P*X))
```

with the possible exceptions of zeros in U due to cancellation where P\*X may be nonzero. The product L\*U agrees within rounding error with the permuted matrix P\*X over its sparsity pattern. (L\*U). \*spones(P\*X)-P\*X has entries of the order of eps.

lui nc(X, droptol) computes the incomplete LU factorization of any sparse matrix using a drop tolerance. droptol must be a non-negative scalar. lui nc(X, droptol) produces an approximation to the complete LU factors returned by lu(X). For increasingly smaller values of the drop tolerance, this approximation improves, until the drop tolerance is 0, at which time the complete LU factorization is produced, as in lu(X).

As each column j of the triangular incomplete factors is being computed, the entries smaller in magnitude than the local drop tolerance (the product of the drop tolerance and the norm of the corresponding column of X)

```
droptol *norm(X(:, j))
```

are dropped from the appropriate factor.

The only exceptions to this dropping rule are the diagonal entries of the upper triangular factor, which are preserved to avoid a singular factor.

lui nc(X, options) specifies a structure with up to four fields that may be used in any combination: droptol, milu, udi ag, thresh. Additional fields of options are ignored.

dropt of is the drop tolerance of the incomplete factorization.

If milu is 1, luinc produces the modified incomplete LU factorization that subtracts the dropped elements in any column from the diagonal element of the upper triangular factor. The default value is 0.

If udi ag is 1, any zeros on the diagonal of the upper triangular factor are replaced by the local drop tolerance. The default is 0.

thresh is the pivot threshold between 0 (forces diagonal pivoting) and 1, the default, which always chooses the maximum magnitude entry in the column to be the pivot. thresh is desribed in greater detail in 1 u.

luinc(X, options) is the same as luinc(X, droptol) if options has droptol as its only field.

 $[L,U]=1\,\mathrm{ui}\,\mathrm{nc}(X,\mathrm{opti}\,\mathrm{ons})$  returns a permutation of a unit lower triangular matrix in L and an upper trianglar matrix in U. The product L\*U is an approximation to X.  $1\,\mathrm{ui}\,\mathrm{nc}(X,\mathrm{opti}\,\mathrm{ons})$  returns the strict lower triangular part of the factor and the upper triangular factor embedded within the same matrix. The permutation information is lost.

[L, U] = luinc(X, options) is the same as luinc(X, droptol) if options has droptol as its only field.

[L, U, P] = 1 ui nc(X, opti ons) returns a unit lower triangular matrix in L, an upper triangular matrix in U, and a permutation matrix in P. The nonzero entries of U satisfy

```
abs(U(i,j)) >= droptol*norm((X:,j)),
```

with the possible exception of the diagonal entries which were retained despite not satisfying the criterion. The entries of L were tested against the local drop tolerance before being scaled by the pivot, so for nonzeros in L

```
abs(L(i,j)) >= droptol*norm(X(:,j))/U(j,j).
```

The product L\*U is an approximation to the permuted P\*X.

[L, U, P] = luinc(X, options) is the same as [L, U, P] = luinc(X, droptol) if options has droptol as its only field.

#### Remarks

These incomplete factorizations may be useful as preconditioners for solving large sparse systems of linear equations. The lower triangular factors all have 1's along the main diagonal but a single 0 on the diagonal of the upper triangular factor makes it singular. The incomplete factorization with a drop tolerance prints a warning message if the upper triangular factor has zeros on the diagonal. Similarly, using the udi ag option to replace a zero diagonal only gets rid of the symptoms of the problem but does not solve it. The preconditioner may not be singular, but it probably is not useful and a warning message is printed.

# luinc

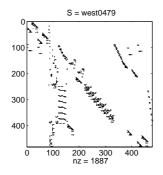
# Limitations

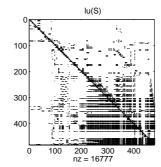
lui nc(X, '0') works on square matrices only.

# **Examples**

Start with a sparse matrix and compute its LU factorization.

load west0479;
S = west0479;
LU = lu(S);



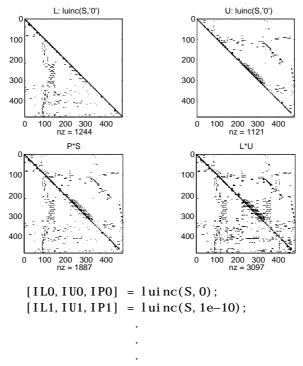


Compute the incomplete LU factorization of level  $\boldsymbol{0}.$ 

[L, U, P] = luinc(S, '0');D = (L\*U).\*spones(P\*S)-P\*S;

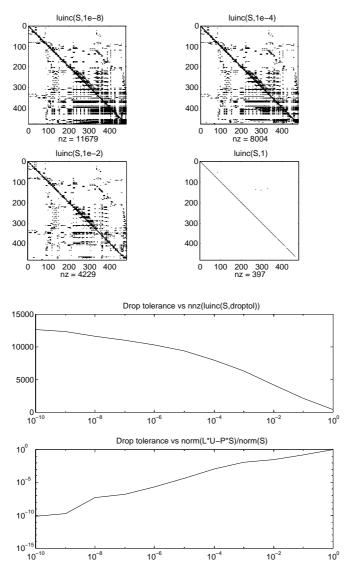
 $spones(\texttt{U}) \ and \ spones(\texttt{tri} \, u(\texttt{P*S})) \ are \ identical.$ 

 $spones(L) \ and \ spones(tril(P*S)) \ disagree \ at \ 73 \ places \ on \ the \ diagonal, \\ where \ L \ is \ 1 \ and \ P*S \ is \ 0, \ and \ also \ at \ position \ (206,113), \ where \ L \ is \ 0 \ due \ to \\ cancellation, \ and \ P*S \ is \ -1. \ D \ has \ entries \ of \ the \ order \ of \ eps.$ 



A drop tolerance of 0 produces the complete LU factorization. Increasing the drop tolerance increases the sparsity of the factors (decreases the number of

nonzeros) but also increases the error in the factors, as seen in the plot of drop tolerance versus norm(L\*U-P\*S, 1)/norm(S, 1) in second figure below.



**Algorithm** lui nc(X, '0') is based on the "KJI" variant of the LU factorization with partial

pivoting. Updates are made only to positions which are nonzero in X.

luinc(X, droptol) and luinc(X, options) are based on the column-oriented lu

for sparse matrices.

See Also lu LU matrix factorization

chol i nc Incomplete Cholesky factorizations bi cg BiConjugate Gradients method

**References** Saad, Yousef, *Iterative Methods for Sparse Linear Systems*, PWS Publishing

Company, 1996, Chapter 10 - Preconditioning Techniques.

# magic

**Purpose** 

Magic square

**Syntax** 

M = magic(n)

**Description** 

 $M=magi\ c(n)$  returns an n-by-n matrix constructed from the integers 1 through  $n^2$  with equal row and column sums. The order n must be a scalar greater than or equal to 3.

**Remarks** 

A magic square, scaled by its magic sum, is doubly stochastic.

**Examples** 

The magic square of order 3 is

This is called a magic square because the sum of the elements in each column is the same.

$$sum(M) = 15 15 15$$

And the sum of the elements in each row, obtained by transposing twice, is the same.

This is also a special magic square because the diagonal elements have the same sum.

```
sum(diag(M)) = 15
```

The value of the characteristic sum for a magic square of order  $\boldsymbol{n}$  is

```
sum(1:n^2)/n
```

which, when n = 3, is 15.

# **Algorithm**

There are three different algorithms: one for odd n, one for even n not divisible by four, and one for even n divisible by four.

To make this apparent, type:

```
for n = 3:20
    A = magic(n);
    plot(A,'-')
    r(n) = rank(A);
end
r
```

#### Limitations

If you supply n less than 3, magi c returns either a nonmagic square, or else the degenerate magic squares 1 and  $[\ ]$ .

#### See Also

ones Create an array of all ones
rand Uniformly distributed random numbers and arrays

# mat2str

Purpose

Convert a matrix into a string

**Syntax** 

```
str = mat2str(A)
str = mat2str(A, n)
```

**Description** 

str = mat2str(A) converts matrix A into a string, suitable for input to the eval function, using full precision.

str = mat2str(A, n) converts matrix A using n digits of precision.

Limitations

The mat2str function is intended to operate on scalar, vector, or rectangular array inputs only. An error will result if A is a multidimensional array.

**Examples** 

Consider the matrix:

The statement

$$b = mat2str(A)$$

produces:

$$b = [1 \ 2 \ ; 3 \ 4]$$

where b is a string of 11 characters, including the square brackets, spaces, and a semicolon.

eval (mat2str(A)) reproduces A.

See Also

int2str Integer to string conversion
sprintf Write formatted data to a string
str2num String to number conversion

Purpose MATLAB startup M-file

Syntax

matlabrc startup

### Description

At startup time, MATLAB automatically executes the master M-file matlabrc. m and, if it exists, startup. m. On multiuser or networked systems, matlabrc. m is reserved for use by the system manager. The file matlabrc. m invokes the file startup. m if it exists on MATLAB's search path.

As an individual user, you can create a startup file in your own MATLAB directory. Use these files to define physical constants, engineering conversion factors, graphics defaults, or anything else you want predefined in your workspace.

## **Algorithm**

Only matlabrc is actually invoked by MATLAB at startup. However, matlabrc m contains the statements:

```
if exist('startup') == 2
    startup
end
```

that invoke startup.  ${\tt m.}$  Extend this process to create additional startup M-files, if required.

#### See Also

! Operating system command exist Check if a variable or file exists

path Control MATLAB's directory search path

qui t Terminate MATLAB

# matlabroot

**Purpose** Root directory of MATLAB installation

**Syntax** rd = matlabroot

**Description** rd = matl abroot returns the name of the directory in which the MATLAB soft-

ware is installed.

**Example** fullfile(matlabroot, 'toolbox', 'matlab', 'general', '')

produces a full path to the tool box/matl ab/general directory that is correct

for the platform it is executed on.

Maximum elements of an array

## Syntax

```
C = \max(A)
C = \max(A, B)
C = \max(A, [], dim)
[C, I] = \max(...)
```

## Description

C = max(A) returns the largest elements along different dimensions of an array.

If A is a vector, max(A) returns the largest element in A.

If A is a matrix,  $\max(A)$  treats the columns of A as vectors, returning a row vector containing the maximum element from each column.

If A is a multidimensional array,  $\max(A)$  treats the values along the first non-singleton dimension as vectors, returning the maximum value of each vector.

C = max(A, B) returns an array the same size as A and B with the largest elements taken from A or B.

C = max(A, [], dim) returns the largest elements along the dimension of A specified by scalar dim. For example, max(A, [], 1) produces the maximum values along the first dimension (the rows) of A.

[C, I] = max(...) finds the indices of the maximum values of A, and returns them in output vector I. If there are several identical maximum values, the index of the first one found is returned.

#### Remarks

For complex input A,  $\max$  returns the complex number with the largest modulus, computed with  $\max(abs(A))$ . The  $\max$  function ignores NaNs.

Detect Not-A-Number (NaN)

#### See Also

isnan

1011011	
mean	Average or mean values of array
medi an	Median values of array
mi n	Minimum elements of an array
sort	Sort elements in ascending order

Average or mean value of arrays

Syntax

M = mean(A)
M = mean(A, dim)

Description

M = mean(A) returns the mean values of the elements along different dimensions of an array.

If A is a vector, mean(A) returns the mean value of A.

If A is a matrix, mean(A) treats the columns of A as vectors, returning a row vector of mean values.

If A is a multidimensional array, mean(A) treats the values along the first non-singleton dimension as vectors, returning an array of mean values.

M = mean(A, dim) returns the mean values for elements along the dimension of A specified by scalar dim

## **Examples**

```
A = [1 2 4 4; 3 4 6 6; 5 6 8 8; 5 6 8 8];

mean(A)

ans =

3.5000 4.5000 6.5000 6.5000
```

ans = 2. 7500 4. 7500

> 6. 7500 6. 7500

See Also

corrcoef Correlation coefficients Covariance matrix

max Maximum elements of an array

medi an Median value of arrays

mi n Minimum elements of an array

std Standard deviation

**Purpose** Median value of arrays

Syntax M = median(A)

M = median(A, dim)

**Description** 

M = median(A) returns the median values of the elements along different dimensions of an array.

If A is a vector, median (A) returns the median value of A.

If A is a matrix, medi an(A) treats the columns of A as vectors, returning a row vector of median values.

If A is a multidimensional array, medi an(A) treats the values along the first nonsingleton dimension as vectors, returning an array of median values.

M = median(A, dim) returns the median values for elements along the dimension of A specified by scalar dim

## **Examples**

```
 A = [1\ 2\ 4\ 4;\ 3\ 4\ 6\ 6;\ 5\ 6\ 8\ 8;\ 5\ 6\ 8\ 8];  medi an(A) ans =  4 \qquad 5 \qquad 7 \qquad 7
```

median(A, 2)

See Also

corrcoef Correlation coefficients
cov Covariance matrix
max Maximum elements of an array

mean Average or mean value of arrays
min Minimum elements of an array

std Standard deviation

# menu

**Purpose** Generate a menu of choices for user input

**Syntax** k = menu('mtitle', 'opt1', 'opt2', ..., 'optn')

**Description** k = menu('mtitle', 'opt1', 'opt2', ..., 'optn') displays the menu whose

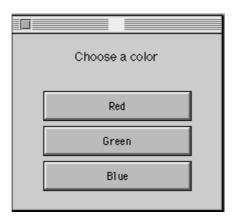
title is in the string variable 'mtitle' and whose choices are string variables

'opt1', 'opt2', and so on. menu returns the value you entered.

**Remarks** To call menu from another ui-object, set that object's Interruptible property to

'yes'. For more information, see the MATLAB Graphics Guide.

**Examples** k = menu('Choose a color', 'Red', 'Green', 'Blue') displays



After input is accepted, use k to control the color of a graph.

**See Also** The ui control command in the *MATLAB Graphics Guide*, and:

i nput Request user input

#### **Purpose**

Generate X and Y matrices for three-dimensional plots

### Syntax

$$[X, Y] = meshgrid(x, y)$$
  
 $[X, Y] = meshgrid(x)$   
 $[X, Y, Z] = meshgrid(x, y, z)$ 

### Description

[X,Y] = meshgrid(x,y) transforms the domain specified by vectors x and y into arrays X and Y, which can be used to evaluate functions of two variables and three-dimensional mesh/surface plots. The rows of the output array X are copies of the vector x; columns of the output array Y are copies of the vector Y.

$$[X, Y] = \text{meshgrid}(x)$$
 is the same as  $[X, Y] = \text{meshgrid}(x, x)$ .

[X,Y,Z] = meshgrid(x,y,z) produces three-dimensional arrays used to evaluate functions of three variables and three-dimensional volumetric plots.

#### Remarks

The meshgrid function is similar to ndgrid except that the order of the first two input and output arguments is switched. That is, the statement

$$[X, Y, Z] = meshgrid(x, y, z)$$

produces the same result as

$$[Y, X, Z] = ndgrid(y, x, z)$$

Because of this, meshgrid is better suited to problems in two- or three-dimensional Cartesian space, while ndgrid is better suited to multidimensional problems that aren't spatially based.

meshgri d is limited to two- or three-dimensional Cartesian space.

# **Examples**

The function

$$[X, Y] = meshgrid(1: 3, 10: 14)$$

produces two output arrays, X and Y:

# meshgrid

See Also

mesh, slice, and surf in the  ${\it MATLAB~Graphics~Guide}$ , griddata, ndgrid

**Purpose** Display method names

Syntax methods class\_name

n = methods('class\_name')

**Description** methods *class\_name* displays the names of the methods for the class with the

name class\_name.

 $n = methods('class\_name')$  returns the method names in a cell array of

strings.

**See Also** hel p Online help for MATLAB functions and M-files

what List M-, MAT- and MEX-files which Locate functions and files

# mexext

**Purpose** Return the MEX-filename extension

**Syntax** ext = mexext

**Description** ext = mexext returns the filename extension for the current platform.

**Purpose** The name of the currently running M-file

Syntax mfilename

**Description** mfilename returns a string containing the name of the most recently invoked

M-file. When called from within an M-file, it returns the name of that M-file, allowing an M-file to determine its name, even if the filename has been

changed.

When called from the command line, mfilename returns an empty matrix.

# min

### **Purpose**

Minimum elements of an array

### **Syntax**

 $C = \min (A)$   $C = \min (A, B)$   $C = \min (A, [], dim)$  $[C, I] = \min (...)$ 

### **Description**

 $C = mi \, n(A)$  returns the smallest elements along different dimensions of an array.

If A is a vector, min(A) returns the smallest element in A.

If A is a matrix,  $\min_{n(A)}$  treats the columns of A as vectors, returning a row vector containing the minimum element from each column.

If A is a multidimensional array,  $\min$  n operates along the first nonsingleton dimension.

C = min(A, B) returns an array the same size as A and B with the smallest elements taken from A or B.

 $C = \min n(A, [], \text{ dim})$  returns the smallest elements along the dimension of A specified by scalar dim. For example,  $\min n(A, [], 1)$  produces the minimum values along the first dimension (the rows) of A.

 $[C, I] = mi \, n(\ldots)$  finds the indices of the minimum values of A, and returns them in output vector I. If there are several identical minimum values, the index of the first one found is returned.

#### **Remarks**

For complex input A, min returns the complex number with the smallest modulus, computed with min(abs(A)). The min function ignores NaNs.

#### See Also

maxMaximum elements of an arraymeanAverage or mean values of arraymedianMedian values of arraysortSort elements in ascending order

**Purpose** 

Modulus (signed remainder after division)

**Syntax** 

$$M = mod(X, Y)$$

**Definition** 

$$mod(x, y)$$
 is  $x \mod y$ .

Description

M = mod(X, Y) returns the remainder X - Y. \*floor(X. /Y) for nonzero Y, and returns X otherwise. mod(X, Y) always differs from X by a multiple of Y.

Remarks

So long as operands X and Y are of the same sign, the function mod(X, Y) returns the same result as does rem(X, Y). However, for positive X and Y,

$$mod(-x, y) = rem(-x, y) + y$$

The mod function is useful for congruence relationships: x and y are congruent (mod m) if and only if mod(x, m) == mod(y, m).

**Examples** 

1

1

Limitations

Arguments X and Y should be integers. Due to the inexact representation of floating-point numbers on a computer, real (or complex) inputs may lead to unexpected results.

See Also

rem

Remainder after division

## more

**Purpose** Control paged output for the command window

Syntax more off

more on more(n)

**Description** more off disables paging of the output in the MATLAB command window.

more on enables paging of the output in the MATLAB command window.

more(n) displays n lines per page.

When you've enabled more and are examining output:

Press the	То
Return key	Advance to the next line of output.
Space bar	Advance to the next page of output.
q (for quit) key	Terminate display of the text.

By default, more is disabled. When enabled, more defaults to displaying 23 lines per page.

See Also di ary Save session in a disk file

**Purpose** Mu-law to linear conversion

Syntax y = mu2lin(mu)

**Description** y = mu21 i n(mu) converts mu-law encoded 8-bit audio signals, stored as

"flints" in the range  $0 \le mu \le 255$ , to linear signal amplitude in the range -s < Y < s where  $s = 32124/32768 \sim 9803$ . The input mu is often obtained using fread(..., 'uchar') to read byte-encoded audio files. "Flints" are MATLAB's

integers – floating-point numbers whose values are integers.

See Also auread Read NeXT/SUN (. au) sound file

lin2mu Linear to mu-law conversion

# NaN

Purpose Not-a-Number

Syntax NaN

**Description** NaN returns the IEEE arithmetic representation for Not-a-Number (NaN).

These result from operations which have undefined numerical results.

**Examples** These operations produce NaN:

• Any arithmetic operation on a NaN, such as sqrt (NaN)

• Addition or subtraction, such as magnitude subtraction of infinities as

(+I nf) + (-I nf)

• Multiplication, such as 0\*Inf

• Division, such as 0/0 and I nf/I nf

• Remainder, such as rem(x, y) where y is zero or x is infinity

**Remarks** Logical operations involving NaNs always return false, except ~= (not equal).

Consequently, the statement NaN ~= NaN is true while the statement NaN == NaN

is false.

See Also Infinity

**Purpose** Check number of input arguments

**Syntax** msg = nargchk(*low*, *high*, number)

**Description** The nargchk function often is used inside an M-file to check that the correct

number of arguments have been passed.

msg = nargchk(low, high, number) returns an error message if number is less than low or greater than high. If number is between low and high (inclusive),

nargchk returns an empty matrix.

**Arguments** *low, high* The minimum and maximum number of input arguments that

should be passed.

number The number of arguments actually passed, as determined by the

nargi n function.

**Examples** Given the function foo:

function f = foo(x, y, z)
error(nargchk(2, 3, nargin))

Then typing foo(1) produces:

Not enough input arguments.

See Also nargin, nargout Number of function arguments

### **Purpose**

Number of function arguments

### **Syntax**

```
n = nargi n
n = nargi n('fun')
n = nargout
n = nargout('fun')
```

### Description

In the body of a function M-file, nargi n and nargout indicate how many input or output arguments, respectively, a user has supplied. Outside the body of a function M-file, nargi n and nargout indicate the number of input or output arguments, respectively, for a given function. The number of arguments is negative if the function has a variable number of arguments.

nargi n returns the number of input arguments specified for a function.

nargi n('fun') returns the number of declared inputs for the M-file function fun or -1 if the function has a variable of input arguments.

nargout returns the number of output arguments specified for a function.

nargout('fun') returns the number of declared outputs for the M-file function fun.

# **Examples**

This example shows portions of the code for a function called mypl ot, which accepts an optional number of input and output arguments:

```
function [x0, y0] = myplot(fname, lims, npts, angl, subdiv) % MYPLOT Plot a function. % MYPLOT(fname, lims, npts, angl, subdiv) % The first two input arguments are % required; the other three have default values. ... if nargin < 5, subdiv = 20; end if nargin < 4, angl = 10; end if nargin < 3, npts = 25; end ... if nargout == 0 plot(x, y) else x0 = x;
```

# nargin, nargout

y0 = y; end

See Also

inputname nargchk Input argument name Check number of input arguments

# nchoosek

**Purpose** All combinations of the n elements in v taken k at a time

**Syntax** C = nchoosek(v, k)

**Description** C = nchoosek(v, k), where v is a row vector of length n, creates a matrix

whose rows consist of all possible combinations of the n elements of v taken k

at a time. Matrix C contains  $n!/((n-k)! \ k!)$  rows and k columns.

**Examples** The command nchoosek(2: 2: 10, 4) returns the even numbers from two to ten,

taken four at a time:

**Limitations** This function is only practical for situations where n is less than about 15.

**See Also** perms All possible permutations

#### **Purpose**

Generate arrays for multidimensional functions and interpolation

Syntax

$$[X1, X2, X3, ...] = ndgrid(x1, x2, x3, ...)$$
  
 $[X1, X2, ...] = ndgrid(x)$ 

Description

[X1, X2, X3, ...] = ndgri d(x1, x2, x3, ...) transforms the domain specified by vectors x1,x2,x3... into arrays X1,X2,X3... that can be used for the evaluation of functions of multiple variables and multidimensional interpolation. The ith dimension of the output array Xi are copies of elements of the vector xi.

 $[X1, X2, \dots] = ndgrid(x)$  is the same as  $[X1, X2, \dots] = ndgrid(x, x, \dots)$ .

**Examples** 

To evaluate the function  $x_1 e^{-x_1^2 - x_2^2}$  over the range  $-2 < x_1 < 2$ ;  $-2 < x_2 < 2$ :

$$\begin{array}{lll} [\ X1,\ X2] &=& ndgri\ d(-2:\ .\ 2:\ 2,\ -2:\ .\ 2:\ 2)\ ; \\ Z &=& X1\ .\ ^*\ exp(-X1.\ ^2\ -\ X2.\ ^2)\ ; \\ mesh(Z) \end{array}$$

Remarks

The ndgrid function is like meshgrid except that the order of the first two input arguments are switched. That is, the statement

$$[X1, X2, X3] = ndgrid(x1, x2, x3)$$

produces the same result as

$$[X2, X1, X3] = meshgrid(x2, x1, x3).$$

Because of this, ndgrid is better suited to multidimensional problems that aren't spatially based, while meshgrid is better suited to problems in two- or three-dimensional Cartesian space.

See Also

meshgri d interpn Generate X and Y matrices for three-dimensional plots Multidimensional data interpolation (table lookup).

# ndims

**Purpose** Number of array dimensions

**Syntax** n = ndims(A)

**Description** n = ndims(A) returns the number of dimensions in the array A. The number

of dimensions in an array is always greater than or equal to 2. Trailing

singleton dimensions are ignored. A singleton dimension is any dimension for

which size(A, dim) = 1.

**Algorithm** ndims(x) is length(size(x)).

See Also si ze Array dimensions

Purpose Next power of two

**Syntax** p = nextpow2(A)

**Description** p = nextpow2(A) returns the smallest power of two that is greater than or

equal to the absolute value of A. (That is, p that satisfies  $2^p \ge abs(A)$ ).

This function is useful for optimizing FFT operations, which are most efficient

when sequence length is an exact power of two.

If A is non-scalar, next pow2 returns the smallest power of two greater than or

equal to length(A).

**Examples** For any integer n in the range from 513 to 1024, nextpow2(n) is 10.

For a 1-by-30 vector A, length(A) is 30 and nextpow2(A) is 5.

**See Also** fft One-dimensional fast Fourier transform

log2 Base 2 logarithm and dissect floating-point numbers

into exponent and mantissa

pow2 Base 2 power and scale floating-point numbers

#### **Purpose**

Nonnegative least squares

### **Syntax**

```
x = nnl s(A, b)

x = nnl s(A, b, tol)

[x, w] = nnl s(A, b)

[x, w] = nnl s(A, b, tol)
```

# **Description**

 $\mathbf{x} = \mathrm{nnl}\,\mathbf{s}(\mathbf{A},\mathbf{b})$  solves the system of equations Ax = b in a least squares sense, subject to the constraint that the solution vector  $\mathbf{x}$  has nonnegative elements:  $x_j \geq 0, \quad j = 1, 2, \dots n$ . The solution  $\mathbf{x}$  minimizes  $\|(Ax = b)\|$  subject to  $x \geq 0$ .

 $x = nnl \, s(A, b, tol)$  solves the system of equations, and specifies a tolerance tol. By default, tol is: max(size(A))\*norm(A, 1)\*eps.

[x, w] = nnl s(A, b) also returns the dual vector w, where  $w_i \le 0$  when  $x_i = 0$  and  $w_i \ge 0$  when  $x_i > 0$ .

[x, w] = nnl s(A, b, tol) solves the system of equations, returns the dual vector w, and specifies a tolerance tol.

# **Examples**

Compare the unconstrained least squares solution to the  ${\tt nnl\ s}$  solution for a 4-by-2 problem:

```
A =
     0.0372
                 0.2869
     0.6861
                 0.7071
     0.6233
                 0.6245
     0.6344
                 0.6170
b =
     0.8587
     0.1781
     0.0747
     0.8405
[A \setminus b \text{ nnls}(A, b)] =
     -2.5627
      3. 1108
                0.6929
```

$$[norm(A*(a\b)-b) norm(A*nnls(a,b)-b)] = 0.6674 0.9118$$

The solution from nnl s does not fit as well, but has no negative components.

**Algorithm** 

The nnl s function uses the algorithm described in [1], Chapter 23. The algorithm starts with a set of possible basis vectors, computes the associated dual vector w, and selects the basis vector corresponding to the maximum value in w to swap out of the basis in exchange for another possible candidate, until  $w \le 0$ .

See Also

Matrix left division (backslash)

References

[1] Lawson, C. L. and R. J. Hanson, *Solving Least Squares Problems*, Prentice-Hall, 1974, Chapter 23.

# nnz

**Purpose** Number of nonzero matrix elements

**Syntax** n = nnz(X)

**Description** n = nnz(X) returns the number of nonzero elements in matrix X.

The density of a sparse matrix is nnz(X)/prod(size(X)).

**Examples** The matrix

w = sparse(wilkinson(21));

is a tridiagonal matrix with 20 nonzeros on each of three diagonals, so

nnz(w) = 60.

**See Also** find Find indices and values of nonzero elements

nonzeros Nonzero matrix elements

nzmax Amount of storage allocated for nonzero matrix

elements

si ze Array dimensions

whos List directory of variables in memory isa Detect an object of a given class

**Purpose** Nonzero matrix elements

**Syntax** s = nonzeros(A)

**Description** s = nonzeros(A) returns a full column vector of the nonzero elements in A,

ordered by columns.

This gives the s, but not the i and j, from [i, j, s] = find(A). Generally,

 $l \, ength(s) = nnz(A) \le nzmax(A) \le prod(size(A))$ 

**See Also** find Find indices and values of nonzero elements

nnz Number of nonzero matrix elements

nzmax Amount of storage allocated for nonzero matrix

elements

si ze Array dimensions

whos List directory of variables in memory

i sa Detect an object of a given class

**Purpose** 

Vector and matrix norms

**Syntax** 

n = norm(A)n = norm(A, p)

**Description** 

The *norm* of a matrix is a scalar that gives some measure of the magnitude of the elements of the matrix. The norm function calculates several different types of matrix norms:

n = norm(A) returns the largest singular value of A, max(svd(A)).

n = norm(A, p) returns a different kind of norm, depending on the value of p:

If <i>p</i> is	Then norm returns
1	The 1-norm, or largest column sum of A, max(sum(abs((A))).
2	The largest singular value (same as norm(A)).
inf	The infinity norm, or largest row sum of A, max(sum(abs(A'))).
'fro'	The Frobenius-norm of matrix A, sqrt(sum(di ag(A'*A))).

When A is a vector, slightly different rules apply:

norm(A, p)	Returns sum(abs(A). $p$ ) $(1/p)$ , for any $1 \le p \le \infty$ .
norm(A)	Returns norm(A, 2).
norm(A, inf)	Returns max(abs(A)).
norm(A, -i nf)	Returns $\min n(abs(A))$ .

Remarks

To obtain the root-mean-square (RMS) value, use norm(A) / sqrt(n). Note that norm(A), where A is an n-element vector, is the length of A.

See Also

condCondition number with respect to inversionnormest2-norm estimatesvdSingular value decomposition

**Purpose** 2-norm estimate

**Syntax** nrm = normest(S)

nrm = normest(S, tol)

[nrm, count] = normest(...)

**Description** This function is intended primarily for sparse matrices, although it works

correctly and may be useful for large, full matrices as well.

nrm = normest(S) returns an estimate of the 2-norm of the matrix S.

nrm = normest(S, tol) uses relative error tol instead of the default tolerance 1. e-6. The value of tol determines when the estimate is considered accept-

able.

[nrm, count] = normest(...) returns an estimate of the 2-norm and also

gives the number of power iterations used.

**Examples** The matrix W = gallery('wilkinson', 101) is a tridiagonal matrix. Its order,

101, is small enough that norm(full(W)), which involves svd(full(W)), is feasible. The computation takes 4.13 seconds (on one computer) and produces the exact norm, 50.7462. On the other hand, normest(sparse(W)) requires

only 1.56 seconds and produces the estimated norm, 50.7458.

**Algorithm** The power iteration involves repeated multiplication by the matrix S and its

transpose, S'. The iteration is carried out until two successive estimates agree

to within the specified relative tolerance.

**See Also** cond Condition number with respect to inversion

condest 1-norm matrix condition number estimate

norm Vector and matrix norms svd Singular value decomposition

# now

**Purpose** Current date and time

**Syntax** t = now

**Description** t = now returns the current date and time as a serial date number. To return

the time only, use rem(now, 1). To return the date only, use floor(now).

**Examples** t1 = now, t2 = rem(now, 1)

t1 =

7.2908e+05

t2 =

0.4013

**See Also** clock Current time as a date vector

date Current date string datenum Serial date number

**Purpose** Null space of a matrix

Syntax B = null(A)

**Description** B = null(A) returns an orthonormal basis for the null space of A.

**Remarks** B' \* B = I, A\*B has negligible elements, and (if B is not equal to the empty

matrix) the number of columns of B is the nullity of A.

See Also orth Range space of a matrix

qr Orthogonal-triangular decomposition

svd Singular value decomposition

# num2cell

**Purpose** Convert a numeric array into a cell array

**Syntax** c = num2cell(A)

c = num2cell(A, dims)

**Description** c = num2cell(A) converts the matrix A into a cell array by placing each

element of A into a separate cell. Cell array c will be the same size as matrix A.

c = num2cell(A, dims) converts the matrix A into a cell array by placing the dimensions specified by dims into separate cells. C will be the same size as A

except that the dimensions matching dims will be 1.

**Examples** The statement

num2cell(A, 2)

places the rows of A into separate cells. Similarly

num2cell(A, [1 3])

places the column-depth pages of A into separate cells.

See Also cat Concatenate arrays

**Purpose** Number to string conversion

**Syntax** str = num2str(A)

str = num2str(A, precision)
str = num2str(A, format)

Description

The num2str function converts numbers to their string representations. This function is useful for labeling and titling plots with numeric values.

str = num2str(a) converts array A into a string representation str with roughly four digits of precision and an exponent if required.

str = num2str(a, precision) converts the array A into a string representation str with maximum precision specified by precision. Argument precision specifies the number of digits the output string is to contain. The default is four.

str = num2str(A, format) converts array A using the supplied format. By default, this is '%11.4g', which signifies four significant digits in exponential or fixed-point notation, whichever is shorter. (See fprintf for format string details).

**Examples** 

num2str(pi) is 3. 142.

num2str(eps) is 2. 22e-16.

num2str(magic(2)) produces the string matrix

 $\begin{matrix} 1 & 3 \\ 4 & 2 \end{matrix}$ 

See Also

fprintf Write formatted data to file
int2str Integer to string conversion
sprintf Write formatted data to a string

### nzmax

**Purpose** Amount of storage allocated for nonzero matrix elements

**Syntax** n = nzmax(S)

**Description** n = nzmax(S) returns the amount of storage allocated for nonzero elements.

If S is a sparse matrix... nzmax(S) is the number of storage locations

allocated for the nonzero elements in S.

If S is a full matrix... nzmax(S) = prod(size(S)).

Often, nnz(S) and nzmax(S) are the same. But if S is created by an operation which produces fill-in matrix elements, such as sparse matrix multiplication or sparse LU factorization, more storage may be allocated than is actually required, and nzmax(S) reflects this. Alternatively, sparse(i,j,s,m,n,nzmax) or its simpler form, spalloc(m,n,nzmax), can set nzmax in anticipation of later fill-in.

See Also find Find indices and values of nonzero elements

nnz Number of nonzero matrix elements

nonzeros Nonzero matrix elements

si ze Array dimensions

whos List directory of variables in memory isa Detect an object of a given class

### **Purpose**

Solve differential equations

### **Syntax**

```
[T, Y] = sol ver('F', tspan, y0)
[T, Y] = sol ver('F', tspan, y0, options)
[T, Y] = sol ver('F', tspan, y0, options, p1, p2...)
[T, Y, TE, YE, IE] = sol ver('F', tspan, y0, options)
[T, X, Y] = sol ver('model', tspan, y0, options, ut, p1, p2, ...)
```

### **Arguments**

F

Name of the ODE file, a MATLAB function of t and y returning a column vector. All solvers can solve systems of equations in the form y' = F(t, y). ode15s and ode23s can both solve equations of the form My' = F(t, y). Only ode15s can solve equations in the form M(t)y' = F(t, y). For information about ODE file syntax, see the odefile reference page.

tspan A vector specifying the interval of integration [t0 tfinal]. To obtain solutions at specific times (all increasing or all decreasing), use tspan = [t0, t1, ..., tfinal].

y0 A vector of initial conditions.

options Optional integration argument created using the odeset function. See odeset for details.

p1, p2. . . Optional parameters to be passed to F.

T, Y Solution matrix Y, where each row corresponds to a time returned in column vector T.

# Description

[T, Y] =  $sol\ ver('F', tspan, y0)$  with  $tspan = [t0\ tfinal]$  integrates the system of differential equations y' = F(t,y) from time t0 to tfinal with initial conditions y0.'F' is a string containing the name of an ODE file. Function F(t,y) must return a column vector. Each row in solution array y corresponds to a time returned in column vector t. To obtain solutions at the specific times t0, t1, ..., tfinal (all increasing or all decreasing), use  $tspan = [t0\ t1\ ...\ tfinal]$ .

 $[T,Y] = sol\,ver(\, 'F' \,,\, tspan,\, y0,\, options)$  solves as above with default integration parameters replaced by property values specified in options, an argument created with the odeset function (see odeset for details). Commonly used

properties include a scalar relative error tolerance Rel Tol (1e-3 by default) and a vector of absolute error tolerances AbsTol (all components 1e-6 by default).

[T, Y] = sol ver('F', tspan, y0, options, p1, p2...) solves as above, passing the additional parameters p1, p2... to the M-file F, whenever it is called. Use options = [] as a place holder if no options are set.

[T, Y, TE, YE, IE] =  $sol\ ver('F', tspan, y0, options)$  with the Events property in options set to 'on', solves as above while also locating zero crossings of an event function defined in the ODE file. The ODE file must be coded so that F(t, y, 'events') returns appropriate information. See odefile for details. Output TE is a column vector of times at which events occur, rows of YE are the corresponding solutions, and indices in vector IE specify which event occurred.

When called with no output arguments, the solvers call the default output function odepl ot to plot the solution as it is computed. An alternate method is to set the <code>OutputFcn</code> property to 'odepl ot'. Set the <code>OutputFcn</code> property to 'odephas2' or 'odephas3' for two- orthree-dimensional phase plane plotting. See odefile for details.

For the stiff solvers ode15s and ode23s, the Jacobian matrix  $\partial F/\partial y$  is critical to reliability and efficiency so there are special options. Set JConstant to 'on' if  $\partial F/\partial y$  is constant. Set Vectori zed to 'on' if the ODE file is coded so that  $F(t, y1 y2 \dots]$ ) returns  $[F(t, y1) F(t, y2) \dots]$ . Set Jattern to 'on' if  $\partial F/\partial y$  is a sparse matrix and the ODE file is coded so that F([], [], 'j pattern') returns a sparsity pattern matrix of 1's and 0's showing the nonzeros of  $\partial F/\partial y$ . Set Jacobi an to 'on' if the ODE file is coded so that F(t, y, 'j acobi an') returns  $\partial F/\partial y$ .

Both ode15s and ode23s can solve problems My' = F(t, y) with a constant mass matrix M that is nonsingular and (usually) sparse. Set Mass to 'on' if the ODE file is coded so that F([], [], 'mass') returns M (see fem2ode). Only ode15s can solve problems M(t)y' = F(t, y) with a time-dependent mass matrix M(t) that is nonsingular and (usually) sparse. Set Mass to 'on' if the ODE file is coded so that F(t, [], 'mass') returns M(t) (see fem1ode). For ode15s set MassConstant to 'on' if M is constant.

Solver	Problem Type	Order of Accuracy	When to Use
ode45	Nonstiff	Medium	Most of the time. This should be the first solver you try.
ode23	Nonstiff	Low	If using crude error tolerances or solving moderately stiff problems.
ode113	Nonstiff	Low to high	If using stringent error tolerances or solving a computationally intensive ODE file.
ode15s	Stiff	Low to medium	If ode45 is slow (stiff systems) or there is a mass matrix.
ode23s	Stiff	Low	If using crude error tolerances to solve stiff systems or there is a constant mass matrix.

The algorithms used in the ODE solvers vary according to order of accuracy [5] and the type of systems (stiff or nonstiff) they are designed to solve. See Algorithms on page 2-480 for more details.

It is possible to specify tspan, y0 and options in the ODE file (see odefile). If tspan or y0 is empty, then the solver calls the ODE file:

```
[tspan, y0, options] = F([], [], 'init')
```

to obtain any values not supplied in the solver's argument list. Empty arguments at the end of the call list may be omitted. This permits you to call the solvers with other syntaxes such as:

```
[T, Y] = sol ver('F')
[T, Y] = sol ver('F', [], y0)
[T, Y] = sol ver('F', tspan, [], options)
[T, Y] = sol ver('F', [], [], options)
```

Integration parameters (options) can be specified both in the ODE file and on the command line. If an option is specified in both places, the command line specification takes precedence. For information about constructing an ODE file, see the odefile reference page.

### **Options**

Different solvers accept different parameters in the options list. For more information, see odeset and  $Using\ MATLAB$ .

Parameters	ode45	ode23	ode113	ode115s	ode23s
Rel Tol, AbsTol	√	√	V	V	√
OutputFcn, OutputSel, Refine, Stats	V	V	V	V	V
Events	√	√	V	V	V
MaxStep, I ni ti al Step	V	V	V	<b>√</b>	V
JConstant, Jacobi an, JPattern, Vectori zed	_	_	_	V	1
Mass MassConstant	_	_	_	√ √	√ —
MaxOrder, BDF	_	_	_	V	<u> </u>

# **Examples**

**Example 1.** An example of a nonstiff system is the system of equations describing the motion of a rigid body without external forces:

$$y'_1 = y_2 y_3$$
  $y_1(0) = 0$   
 $y'_2 = -y_1 y_3$   $y_2(0) = 1$   
 $y'_3 = -0.51 y_1 y_2$   $y_3(0) = 1$ 

To simulate this system, create a function M-file  $\operatorname{rigid}$  containing the equations:

```
function dy = rigid(t, y)

dy = zeros(3, 1); % a column vector

dy(1) = y(2) * y(3);

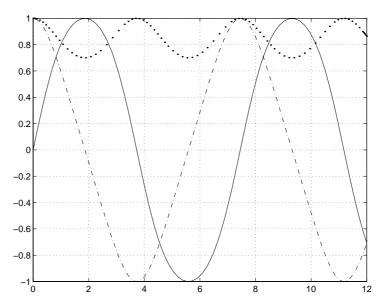
dy(2) = -y(1) * y(3);

dy(3) = -0.51 * y(1) * y(2);
```

In this example we will change the error tolerances with the odeset command and solve on a time interval of  $[0\ 12]$  with initial condition vector  $[0\ 1\ 1]$  at time  $[0\ 1]$ 

```
options = odeset('RelTol', 1e-4, 'AbsTol', [1e-4 1e-4 1e-5]);
[t, y] = ode45('rigid', [0 12], [0 1 1], options);
```

Plotting the columns of the returned array Y versus T shows the solution:



**Example 2.** An example of a stiff system is provided by the van der Pol equations governing relaxation oscillation. The limit cycle has portions where the solution components change slowly and the problem is quite stiff, alternating with regions of very sharp change where it is not stiff.

$$y'_1 = y_2$$
  $y_1(0) = 0$   
 $y'_2 = 1000(1 - y_1^2)y_2 - y_1$   $y_2(0) = 1$ 

To simulate this system, create a function M-file vdp1000 containing the equations:

```
function dy = vdp1000(t, y)

dy = zeros(2, 1); % a column vector

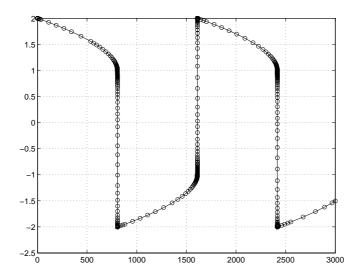
dy(1) = y(2);

dy(2) = 1000*(1 - y(1)^2)*y(2) - y(1);
```

For this problem, we will use the default relative and absolute tolerances (1e-3 and 1e-6, respectively) and solve on a time interval of  $[0\ 3000]$  with initial condition vector  $[2\ 0]$  at time  $[0\ 0]$ .

```
[T, Y] = ode15s('vdp1000', [0 3000], [2 0]);
```

Plotting the first column of the returned matrix Y versus T shows the solution:



# **Algorithms**

ode45 is based on an explicit Runge-Kutta (4,5) formula, the Dormand-Prince pair. It is a *one-step* solver – in computing  $y(t_n)$ , it needs only the solution at the immediately preceding time point,  $y(t_{n-1})$ . In general, ode45 is the best function to apply as a "first try" for most problems. [1]

ode23 is an implementation of an explicit Runge-Kutta (2,3) pair of Bogacki and Shampine. It may be more efficient than ode45 at crude tolerances and in the presence of moderate stiffness. Like ode45, ode23 is a one-step solver. [2]

ode113 is a variable order Adams-Bashforth-Moulton PECE solver. It may be more efficient than ode45 at stringent tolerances and when the ODE file function is particularly expensive to evaluate. ode113 is a *multistep* solver – it normally needs the solutions at several preceding time points to compute the current solution. [3]

The above algorithms are intended to solve non-stiff systems. If they appear to be unduly slow, try using one of the stiff solvers (ode15s and ode23s) instead.

ode15s is a variable order solver based on the numerical differentiation formulas, NDFs. Optionally, it uses the backward differentiation formulas, BDFs (also known as Gear's method) that are usually less efficient. Like ode113, ode15s is a multistep solver. If you suspect that a problem is stiff or if ode45 has failed or was very inefficient, try ode15s. [7]

ode23s is based on a modified Rosenbrock formula of order 2. Because it is a one-step solver, it may be more efficient than ode15s at crude tolerances. It can solve some kinds of stiff problems for which ode15s is not effective. [7]

#### See Also

odeset, odeget, odefile

#### References

- [1] Dormand, J. R. and P. J. Prince, "A family of embedded Runge-Kutta formulae," *J. Comp. Appl. Math.*, Vol. 6, 1980, pp 19–26.
- [2] Bogacki, P. and L. F. Shampine, "A 3(2) pair of Runge-Kutta formulas," *Appl. Math. Letters*, Vol. 2, 1989, pp 1–9.
- [3] Shampine, L. F. and M. K. Gordon, *Computer Solution of Ordinary Differential Equations: the Initial Value Problem*, W. H. Freeman, San Francisco, 1975.
- [4] Forsythe, G., M. Malcolm, and C. Moler, *Computer Methods for Mathematical Computations*, Prentice-Hall, New Jersey, 1977.
- [5] Shampine, L. F., *Numerical Solution of Ordinary Differential Equations*, Chapman & Hall, New York, 1994.

# ode45, ode23, ode113, ode15s, ode23s

[6] Kahaner, D., C. Moler, and S. Nash, *Numerical Methods and Software*, Prentice-Hall, New Jersey, 1989.

[7] Shampine, L. F. and M. W. Reichelt, "The MATLAB ODE Suite," (to appear in *SIAM Journal on Scientific Computing*, Vol. 18-1, 1997).

Define a differential equation problem for ODE solvers

## Description

odefile is not a command or function. It is a help entry that describes how to create an M-file defining the system of equations to be solved. This definition is the first step in using any of MATLAB's ODE solvers. In MATLAB documentation, this M-file is referred to as odefile, although you can give your M-file any name you like.

You can use the odefile M-file to define a system of differential equations in one of these forms:

$$y' = F(t, y)$$

$$My' = F(t, y)$$

$$M(t)y' = F(t, y)$$

#### where:

- *t* is a scalar independent variable, typically representing time.
- *y* is a vector of dependent variables.
- *F* is a function of *t* and *y* returning a column vector the same length as *y*.
- M and M(t) represent nonsingular constant or time dependent mass matrices.

The ODE file must accept the arguments t and y, although it does not have to use them. By default, the ODE file must return a column vector the same length as y.

Only the stiff solver ode15s can solve M(t)y' = F(t, y). Both ode15s and ode23s can solve equations of the form My' = F(t, y).

Beyond defining a system of differential equations, you can specify an entire initial value problem (IVP) within the ODE M-file, eliminating the need to supply time and initial value vectors at the command line (see Examples on page 2-486).

## To use the ODE file template:

- Enter the command help odefile to display the help entry.
- Cut and paste the ODE file text into a separate file.
- Edit the file to eliminate any cases not applicable to your IVP.
- Insert the appropriate information where indicated. The definition of the ODE system is required information. (See item 2 as well as Examples on page 2-486). Here is an annotated version of the result:

```
function [out1, out2, out3] = odefile(t, y, flag, p1, p2)
% ODEFILE The template for ODE files.
if nargin < 3 | isempty(flag) % Return dy/dt = F(t, y)
 out1 = < Insert a function of t and/or y, p1, and p2 here >;
else
  switch(flag)
case 'init'
                   % Return default [tspan, y0, and options]
    out1 = < Insert tspan here >;
    out2 = < Insert y0 here >;
    out3 = < Insert options = odeset(...) or [] here >;
                   % Return matrix J(t, y) = dF/dy
                                                               5
  case 'jacobi an'
    out1 = < Insert Jacobian matrix here >;
 case 'jpattern' % Return sparsity pattern matrix S	━
    out1 = < Insert Jacobian matrix sparsity pattern here >
 case 'mass'
                   % Return mass matrix M(t) or M ◀
    out1 = < Insert mass matrix here >;
 case 'events'
                   % Return event vector and info
    out1 = < Insert event function vector here >;
    out2 = < Insert logical isterminal vector here >; 	←
    out3 = < Insert direction vector here >:
 otherwise -
    error(['Unknown flag''' flag '''.']);
 end
end
```

#### Notes

- 1 The ODE file must accept t and y vectors from the ODE solvers and must return a column vector the same length as y. The optional input argument flag determines the type of output (mass matrix, Jacobian, etc.) returned by the ODE file.
- **2** The solvers repeatedly call the ODE file to evaluate the system of differential equations at various times. *This is required information*—you must define the ODE system to be solved.
- **3** The switch statement determines the type of output required, so that the ODE file can pass the appropriate information to the solver. (See steps 4 9.)
- **4** In the default *initial conditions* (' i ni t') case, the ODE file returns basic information (time span, initial conditions, options) to the solver. If you omit this case, you must supply all the basic information on the command line.
- 5 In the 'j acobi an' case, the ODE file returns a Jacobian matrix to the solver. You need only provide this case when you wish to improve the performance of the stiff solvers ode15s and ode23s.
- **6** In the 'j pattern' case, the ODE file returns the Jacobian sparsity pattern matrix to the solver. You need provide this case only when you want to generate sparse Jacobian matrices numerically for a stiff solver.
- **7** In the 'mass' case, the ODE file returns a mass matrix to the solver. You need provide this case only when you want to solve a system in either of the forms My' = F(t, y) or M(t)y' = F(t, y).
- 8 In the 'events' case, the ODE file returns to the solver the values that it needs to perform event location. When the Events property is set to 1, the ODE solvers examine any elements of the event vector for transitions to, from, or through zero. If the corresponding element of the logical i sterminal vector is set to 1, integration will halt when a zero-crossing is detected. The elements of the direction vector are -1, 1, or 0, specifying that the corresponding event must be decreasing, increasing, or that any crossing is to be detected. See the *Applying MATLAB* and also the examples ball ode and orbitode.
- **9** An unrecognized fl ag generates an error.

## **Examples**

The van der Pol equation,  $y''_1 - \mu(1-y_1^2)y'_1 + y_1 =$ is equivalent to a system of coupled first-order differential equations:

$$y'_1 = y_2$$
  
 $y'_2 = \mu(1 - y_1^2)y_2 - y_1$ 

The M-file

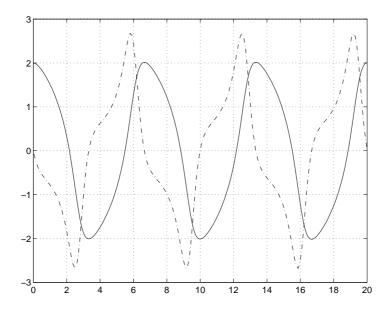
```
function out1 = vdp1(t, y)
out1 = [y(2); (1-y(1)^2)*y(2) - y(1)];
```

defines this system of equations (with  $\mu = 1$ ).

To solve the van der Pol system on the time interval  $[0\ 20]$  with initial values (at time 0) of y(1) = 2 and y(2) = 0, use:

```
[t, y] = ode45('vdp1', [0 20], [2; 0]);

plot(t, y(:, 1), '-', t, y(:, 2), '-.')
```



To specify the entire initial value problem (IVP) within the M-file, rewrite vdp1 as follows:

You can now solve the IVP without entering any arguments from the command line:

```
[T, Y] = ode23('vdp1')
```

In this example the ode23 function looks to the vdp1 M-file to supply the missing arguments. Note that, once you've called odeset to define options, the calling syntax:

```
[T, Y] = ode23('vdp1', [], [], options)
```

also works, and that any options supplied via the command line override corresponding options specified in the M-file (see odeset).

Some example ODE files we have provided include b5ode, brussode, vdpode, orbitode, and rigidode. Use type *filename* from the MATLAB command line to see the coding for a specific ODE file.

## See Also

The *Applying MATLAB* and the reference entries for the ODE solvers and their associated functions:

ode23, ode45, ode113, ode15s, ode23s, odeget, odeset

Extract properties from options structure created with odeset

Syntax

```
o = odeget(options, 'name')
o = odeget(options, 'name', default)
```

**Description** 

o = odeget(options, 'name') extracts the value of the property specified by string 'name' from integrator options structure options, returning an empty matrix if the property value is not specified in options. It is only necessary to type the leading characters that uniquely identify the property name. Case is ignored for property names. The empty matrix [] is a valid options argument.

o = odeget(options, 'name', default) returns o = default if the named property is not specified in options.

**Example** 

Having constructed an ODE options structure,

```
options = odeset('RelTol', 1e-4, 'AbsTol', [1e-3 2e-3 3e-3]);
```

you can view these property settings with odeget:

See Also

odeset

Create or alter options structure for input to ODE solvers

## Syntax

```
options = odeset('name1', value1, 'name2', value2,...)
options = odeset(oldopts, 'name1', value1,...)
options = odeset(oldopts, newopts)
odeset
```

## Description

The odeset function lets you adjust the integration parameters of the ODE solvers. See below for information about the integration parameters.

options = odeset('name1', value1, 'name2', value2...) creates an integrator options structure in which the named properties have the specified values. The odeset function sets any unspecified properties to the empty matrix [].

It is sufficient to type only the leading characters that uniquely identify the property name. Case is ignored for property names.

options = odeset(oldopts, 'name1', value1, ...) alters an existing options structure with the values supplied.

options = odeset(oldopts, newopts) alters an existing options structure oldopts by combining it with a new options structure newopts. Any new options not equal to the empty matrix overwrite corresponding options in oldopts. For example:

ol do	pts								
F	1	[]	4	's'	' s'	[]	[]	[]	
newo	pts			•					
Т	3	F	[]	٠,	[]	[]	[]	[]	
odes	et (o	l dopt	ts, ne	ewopt	(s)				,
Т	3	F	4		' s'	[]	[]	[]	

odeset by itself, displays all property names and their possible values:

odeset

```
AbsTol: [ positive scalar or vector {1e-6}]
BDF: [ on | {off} ]
Events: [ on | {off} ]
InitialStep: [ positive scalar ]
Jacobi an: [ on | {off} ]
JConstant: [ on | {off} ]
JPattern: [ on | {off} ]
Mass: [ on | {off} ]
MassConstant: [ on | off]
Max0rder: [ 1 | 2 | 3 | 4 | {5} ]
MaxStep: [ positive scalar ]
OutputFcn: [ string ]
OutputSel: [ vector of integers ]
Refine: [ positive integer ]
RelTol: [ positive scalar {1e-3} ]
Stats: [ on | {off} ]
Vectorized: [ on | {off} ]
```

## **Properties**

The available properties depend upon the ODE solver used. There are seven principal categories of properties:

- Error tolerance
- Solver output
- Jacobian
- Event location
- Mass matrix
- Step size
- ode15s

**Table 1-1: Error Tolerance Properties** 

Property	Value	Description
Rel Tol	Positive scalar {1e-3}	A relative error tolerance that applies to all components of the solution vector.
AbsTol	Positive scalar or vector {1e-6}	The absolute error tolerance. If scalar, the tolerance applies to all components of the solution vector. Otherwise the tolerances apply to corresponding components.

**Table 1-2: Solver Output Properties** 

Property	Value	Description
OutputFcn	String	The name of an installable output function (for example, odepl ot, odephas2, odephas3, and odeprint). The ODE solvers call outputfcn(TSPAN, Y0, 'init') before beginning the integration, to initialize the output function. Subsequently, the solver calls status = outputfcn(T, Y) after computing each output point (T, Y). The status return value should be 1 if integration should be halted (e.g., a <b>STOP</b> button has been pressed) and 0 otherwise. When the integration is complete, the solver calls outputfcn([], [], 'done').
OutputSel	Vector of indices	Specifies which components of the solution vector are to be passed to the output function.

**Table 1-2: Solver Output Properties** 

Property	Value	Description
Refine	Positive Integer	Produces smoother output, increasing the number of output points by a factor of n. In most solvers, the default value is 1.  However, within ode45, Refine is 4 by default to compensate for the solver's large step sizes. To override this and see only the time steps chosen by ode45, set Refine to 1.
Stats	on   {off}	Specifies whether statistics about the computational cost of the integration should be displayed.

Table 1-3: Jacobian Matrix Properties (for ode15s and ode23s)

Property	Value	Description
JConstant	on   {off}	Specifies whether the Jacobian matrix $\partial F/\partial y$ is constant (see b5ode).
Jacobi an	on   {off}	Informs the solver that the ODE file responds to the arguments (t, y, 'j acobi an') by returning $\partial F/\partial y$ (see odefile).
JPattern	on   {off}	Informs the solver that the ODE file responds to the arguments ([], [], 'j pattern') by returning a sparse matrix containing 1's showing the nonzeros of $\partial F/\partial y$ (see brussode).

Table 1-3: Jacobian Matrix Properties (for ode15s and ode23s)

Property	Value	Description
Vectori zed	on   {off}	Informs the solver that the ODE file $F(t,y)$ has been vectorized so that $F(t, [y1\ y2\ \dots])$ returns $[F(t,y1)\ F(t,y2)\ \dots]$ . That is, your ODE file can pass to the solver a whole array of column vectors at once. Your ODE file will be called by a stiff solver in a vectorized manner only if generating Jacobians numerically (the default behavior) and odeset has been used to set Vectorized to 'on'.

**Table 1-4: Event Location Property** 

Property	Value	Description
Events	on   {off}	Instructs the solver to locate events. The ODE file must respond to the arguments (t, y, 'events') by returning the appropriate values. See odefile.

Table 1-5: Mass Matrix Properties (for ode15s and ode23s)

Property	Value	Description
Mass	on   {off}	Informs the solver that the ODE file is coded so that $F(t, [], 'mass')$ returns $M$ or $M(t)$ (see odefile).
MassConstant	on   {off}	Informs the solver that the mass matrix $M(t)$ is constant.

**Table 1-6: Step Size Properties** 

Property	Value	Description
MaxStep	Positive scalar	An upper bound on the magnitude of the step size that the solver uses.
I ni ti al Step	Positive scalar	Suggested initial step size. The solver tries this first, but if too large an error results, the solver uses a smaller step size.

In addition there are two options that apply only to the ode15s solver.

**Table 1-7: ode15s Properties** 

Property	Value	Description
Max0rder	1   2   3   4   {5}	The maximum order formula used.
BDF	on   {off}	Specifies whether the Backward Differentiation Formulas (BDF's) are to be used instead of the default Numerical Differentiation Formulas (NDF's).

## See Also

odefile, odeget, ode45, ode23, ode113, ode15s,ode23s

## **Purpose** Create an array of all ones

**Syntax** Y = ones(n)

Y = ones(m, n)

 $Y = ones([m \ n])$ 

Y = ones(d1, d2, d3...)

Y = ones([d1 d2 d3...])

Y = ones(size(A))

**Description** Y = ones(n) returns an n-by-n matrix of 1s. An error message appears if n is

not a scalar.

Y = ones(m, n) or Y = ones([m n]) returns an m-by-n matrix of ones.

Y = ones(d1, d2, d3...) or Y = ones([d1 d2 d3...]) returns an array of 1s

with dimensions d1-by-d2-by-d3-by-. . . .

Y = ones(size(A)) returns an array of 1s that is the same size as A.

See Also eye Identity matrix

rand Uniformly distributed random numbers and arrays

randn Normally distributed random numbers and arrays

zeros Create an array of all zeros

# orth

**Purpose** Range space of a matrix

**Syntax** B = orth(A)

**Description** B = orth(A) returns an orthonormal basis for the range of A. The columns of

B span the same space as the columns of A, and the columns of B are orthogonal, so that B'\*B = eye(rank(A)). The number of columns of B is the rank of A.

See Also nul l Null space of a matrix

svd Singular value decomposition

rank Rank of a matrix

**Purpose** Default part of switch statement

**Description** otherwise is part of the switch statement syntax, which allows for conditional

execution. The statements following otherwise are executed only if none of the

preceding case expressions (case\\_expr) match the switch expression  $% \left( -\frac{1}{2}\right) =-\frac{1}{2}\left( -\frac{1}{2}\right) =-\frac{1}$ 

(sw\_expr).

**Examples** The general form of the switch statement is:

```
switch sw_expr
   case case_expr
   statement
   statement
   case {case_expr1, case_expr2, case_expr3}
   statement
   statement
   otherwise
   statement
   statement
   statement
   statement
   statement
   statement
   statement
end
```

See switch for more details.

See Also switch Switch among several cases based on expression

# otherwise

Purpose Consolidate workspace memory

Syntax pack

pack filename

Description

pack, by itself, frees up needed space by compressing information into the minimum memory required.

pack *filename* accepts an optional *filename* for the temporary file used to hold the variables. Otherwise it uses the file named pack. tmp.

Remarks

The pack command doesn't affect the amount of memory allocated to the MATLAB process. You must quit MATLAB to free up this memory.

Since MATLAB uses a heap method of memory management, extended MATLAB sessions may cause memory to become fragmented. When memory is fragmented, there may be plenty of free space, but not enough contiguous memory to store a new large variable.

If you get the Out of memory message from MATLAB, the pack command may find you some free memory without forcing you to delete variables.

The pack command frees space by:

- Saving all variables on disk in a temporary file called pack. tmp.
- Clearing all variables and functions from memory.
- $\bullet$  Reloading the variables back from pack. tmp.
- Deleting the temporary file pack. tmp.

# pack

If you use pack and there is still not enough free memory to proceed, you must clear some variables. If you run out of memory often, here are some system-specific tips:

- **MS-Windows:** Increase the swap space by opening the Control Panel, double-clicking on the 386 Enhanced icon, and pressing the **Virtual Memory** button.
- **Macintosh**: Change the application memory size by using **Get Info** on the program icon. You may also want to turn on virtual memory via the Memory Control Panel.
- **VAX/VMS**: Ask your system manager to increase your working set and/or pagefile quota.
- UNIX: Ask your system manager to increase your swap space.

See Also

cl ear

Remove items from memory

Partial pathname

## **Description**

A partial pathname is a MATLABPATH relative pathname used to locate private and method files, which are usually hidden, or to restrict the search for files when more than one file with the given name exists.

A partial pathname contains the last component, or last several components, of the full pathname separated by /. For example, matfun/trace, pri vate/children, inline/formula, and demos/clown. mat are valid partial pathnames. Specifying the @ in method directory names is optional, so funfun/inline/formula is also a valid partial pathname.

Partial pathnames make it easy to find toolbox or MATLAB relative files on your path in a portable way independent of the location where MATLAB is installed.

# pascal

**Purpose** 

Pascal matrix

**Syntax** 

A = pascal(n)

A = pascal(n, 1)

A = pascal(n, 2)

**Description** 

A = pascal (n, 1) returns the lower triangular Cholesky factor (up to the signs of the columns) of the Pascal matrix. It is *involutary*, that is, it is its own inverse.

A = pascal(n, 2) returns a transposed and permuted version of pascal (n, 1). A is a cube root of the identity matrix.

**Examples** 

pascal (4) returns

A = pascal (3, 2) produces

**See Also** 

chol

Cholesky factorization

## **Purpose** Control MATLAB's directory search path

## **Syntax**

path

p = path

path('newpath')

path(path, 'newpath')
path('newpath', path)

## Description

path prints out the current setting of MATLAB's search path. On all platforms except the Macintosh, the path resides in pathdef. m (in tool box/local). The Macintosh stores its path in the Matlab Settings File (usually in the Preferences folder).

p = path returns the current search path in string variable p.

path('newpath') changes the path to the string 'newpath'.

path(path, 'newpath') appends a new directory to the current path.

path('newpath', path) prepends a new directory to the current path.

#### Remarks

MATLAB has a *search path*. If you enter a name, such as fox, the MATLAB interpreter:

- 1 Looks for fox as a variable.
- **2** Checks for fox as a built-in function.
- 3 Looks in the current directory for fox. mex and fox. m.
- 4 Searches the directories specified by path for fox. mex and fox. m.

### **Examples**

Add a new directory to the search path on various operating systems:

UNIX: path(path, '/home/myfri end/goodstuff')

VMS: path(path, 'DI SKS1: [MYFRI END. GOODSTUFF]')

MS-DOS: path(path, 'T00LS\G00DSTUFF')

Macintosh: path(path, 'Tools: GoodStuff')

# path

**See Also** addpath Add directories to MATLAB's search path

cd Change working directory

di r Directory listing

rmpath Remove directories from MATLAB's search path what Directory listing of M-files, MAT-files, and MEX-files

**Purpose** Halt execution temporarily

Syntax pause

pause(n)
pause on
pause of f

**Description** pause, by itself, causes M-files to stop and wait for you to press any key before

continuing.

 $pause(n) \ \ pauses \ execution \ for \ n \ seconds \ before \ continuing.$ 

pause on allows subsequent pause commands to pause execution.

pause off ensures that any subsequent pause or pause(n) statements do not pause execution. This allows normally interactive scripts to run unattended.

**See Also** The drawnow command in the *MATLAB Graphics Guide*.

**Preconditioned Conjugate Gradients method** 

## Syntax

```
x = pcg(A, b)
pcg(A, b, tol)
pcg(A, b, tol, maxit)
pcg(A, b, tol, maxit, M)
pcg(A, b, tol, maxit, M1, M2)
pcg(A, b, tol, maxit, M1, M2, x0)
x = pcg(A, b, tol, maxit, M1, M2, x0)
[x, flag] = pcg(A, b, tol, maxit, M1, M2, x0)
[x, flag, relres] = pcg(A, b, tol, maxit, M1, M2, x0)
[x, flag, relres, iter] = pcg(A, b, tol, maxit, M1, M2, x0)
[x, flag, relres, iter, resvec] = pcg(A, b, tol, maxit, M1, M2, x0)
```

## Description

x = pcg(A, b) attempts to solve the system of linear equations A\*x = b for x. The coefficient matrix A must be symmetric and positive definite and the right hand side (column) vector b must have length n, where A is n-by-n. pcg will start iterating from an initial estimate that by default is an all zero vector of length n. Iterates are produced until the method either converges, fails, or has computed the maximum number of iterations. Convergence is achieved when an iterate x has relative residual norm(b-A\*x)/norm(b) less than or equal to the tolerance of the method. The default tolerance is 1e-6. The default maximum number of iterations is the minimum of n and 20. No preconditioning is used.

pcg(A, b, tol) specifies the tolerance of the method, tol.

pcg(A, b, tol, maxit) additionally specifies the maximum number of iterations. maxit.

pcg(A, b, tol, maxit, M) and pcg(A, b, tol, maxit, M1, M2) use left preconditioner Mor M=M1 \*M2 and effectively solve the system i nv(M) \*A\*x = i nv(M) \*b for x. If M1 or M2 is given as the empty matrix ([]), it is considered to be the identity matrix, equivalent to no preconditioning at all. Since systems of equations of the form M\*y=r are solved using backslash within pcg, it is wise to factor

preconditioners into their Cholesky factors first. For example, replace pcg(A, b, tol, maxit, M) with:

```
R = \text{chol}(M);

pcg(A, b, tol, maxit, R', R).
```

The preconditioner M must be symmetric and positive definite.

pcg(A, b, tol, maxit, M1, M2, x0) specifies the initial estimate x0. If x0 is given as the empty matrix ([]), the default all zero vector is used.

x = pcg(A, b, tol, maxit, M1, M2, x0) returns a solution x. If pcg converged, a message to that effect is displayed. If pcg failed to converge after the maximum number of iterations or halted for any reason, a warning message is printed displaying the relative residual norm(b-A\*x)/norm(b) and the iteration number at which the method stopped or failed.

[x, flag] = pcg(A, b, tol, maxit, M1, M2, x0) returns a solution x and a flag which describes the convergence of pcg:

Flag	Convergence
0	pcg converged to the desired tolerance tol within maxit iterations without failing for any reason.
1	pcg iterated maxit times but did not converge.
2	One of the systems of equations of the form $M^*y=r$ involving the preconditioner was ill-conditioned and did not return a useable result when solved by $\setminus$ (backslash).
3	The method stagnated. (Two consecutive iterates were the same.)
4	One of the scalar quantities calculated during $\ensuremath{pcg}$ became too small or too large to continue computing

Whenever  ${\tt fl}$  ag is not 0, the solution x returned is that with minimal norm residual computed over all the iterations. No messages are displayed if the  ${\tt fl}$  ag output is specified.

[x, flag, rel res] = pcg(A, b, tol, maxit, M1, M2, x0) also returns the relative residual norm(b-A\*x)/norm(b). If flag is 0, then rel res  $\leq tol$ .

[x, flag, relres, iter] = pcg(A, b, tol, maxit, M1, M2, x0) also returns the iteration number at which x was computed. This always satisfies  $0 \le iter \le maxit$ .

[x, flag, rel res, i ter, resvec] = pcg(A, b, tol, maxit, M1, M2, x0) also returns a vector of the residual norms at each iteration, starting from resvec(1) = norm(b-A\*x0). If flag is 0, resvec is of length i ter+1 and  $resvec(end) \le tol*norm(b)$ .

## **Examples**

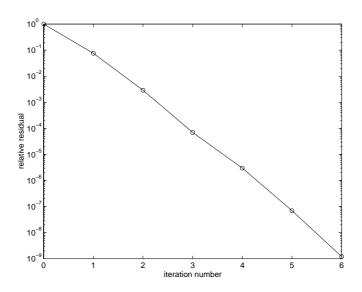
```
A = del sq(numgri d('C', 25))
b = ones(length(A), 1)
[x, flag] = pcg(A, b)
```

flag is 1 since pcg will not converge to the default tolerance of 1e-6 within the default 20 iterations.

```
R = \text{cholinc}(A, 1e-3)
[x2, flag2, relres2, iter2, resvec2] = pcg(A, b, 1e-8, 10, R', R)
```

fl ag2 is 0 since pcg will converge to the tolerance of 1. 2e-9 (the value of rel res2) at the sixth iteration (the value of i ter2) when preconditioned by the incomplete Cholesky factorization with a drop tolerance of 1e-3. resvec2(1) = norm(b) and resvec2(7) = norm(b-A\*x2). You may follow the progress of pcg

by plotting the relative residuals at each iteration starting from the initial estimate (iterate number 0) with semilogy(0: i ter2, resvec2/norm(b), '-o').



#### See Also

bi cg
bi cgstab
bi cgstab
BiConjugate Gradients Stabilized method
cgs
Conjugate Gradients Squared method
chol i nc
Incomplete Cholesky factorizations
gmres
Generalized Minimum Residual method (with restarts)
qmr
Quasi-Minimal Residual method
Matrix left division

#### References

Templates for the Solution of Linear Systems: Building Blocks for Iterative Methods, SIAM, Philadelphia, 1994.

# pcode

**Purpose** Create preparsed pseudocode file (P-file)

Syntax pcode fun

 $pcode \ *.\ m$ 

pcode fun1 fun2 ...
pcode... -i npl ace

current directory. The original M-file can be anywhere on the search path.

pcode \*.m creates P-files for all the M-files in the current directory.

pcode fun1 fun2 ... creates P-files for the listed functions.

 $pcode. \ . \ . \ \cdot i \ npl \ ace \ creates \ P-files \ in \ the \ same \ directory \ as \ the \ M-files. An$ 

error occurs if the files can't be created.

**Purpose** All possible permutations

**Syntax** P = perms(v)

**Description** P = perms(v), where v is a row vector of length n, creates a matrix whose rows

consist of all possible permutations of the n elements of v. Matrix P contains n!

rows and n columns.

**Examples** The command perms (2: 2: 6) returns *all* the permutations of the numbers 2, 4,

and 6:

6 2 4 2 4 6 6 4 2 6 4 6 4 2 2 6 4

**Limitations** This function is only practical for situations where n is less than about 15.

**See Also** nchoosek All combinations of the n elements in y taken k at a

time

permute Rearrange the dimensions of a multidimensional array

randperm Random permutation

## permute

**Purpose** 

Rearrange the dimensions of a multidimensional array

**Syntax** 

B = permute(A, order)

**Description** 

B = permute(A, order) rearranges the dimensions of A so that they are in the order specified by the vector order. B has the same values of A but the order of the subscripts needed to access any particular element is rearranged as specified by order. All the elements of order must be unique.

Remarks

permute and i permute are a generalization of transpose (. ') for multidimensional arrays.

**Examples** 

Given any matrix A, the statement

```
permute(A, [2 1])
```

is the same as A'.

For example:

The following code permutes a three-dimensional array:

```
X = rand(12, 13, 14);
Y = permute(X, [2 3 1]);
size(Y)
ans =
    13    14    12
```

See Also

i permute

Inverse permute the dimensions of a multidimensional array

**Purpose** Ratio of a circle's circumference to its diameter,  $\pi$ 

Syntax pi

**Description** pi returns the floating-point number nearest the value of  $\pi$ . The expressions

4\*atan(1) and i mag(l og(-1)) provide the same value.

**Examples** The expression sin(pi) is not exactly zero because pi is not exactly  $\pi$ :

sin(pi) ans = 1.2246e-16

**See Also** ans The most recent answer

eps Floating-point relative accuracy

i Imaginary unit

Inf Infinity

j Imaginary unit NaN Not-a-Number

Moore-Penrose pseudoinverse of a matrix

## Syntax

$$B = pi nv(A)$$
  
 $B = pi nv(A, tol)$ 

## **Definition**

The Moore-Penrose pseudoinverse is a matrix B of the same dimensions as A' satisfying four conditions:

The computation is based on svd(A) and any singular values less than toll are treated as zero.

## **Description**

B = pi nv(A) returns the Moore-Penrose pseudoinverse of A.

 $B = pi \, nv(A, tol)$  returns the Moore-Penrose pseudoinverse and overrides the default tolerance,  $max(si \, ze(A)) * norm(A) * eps$ .

## **Examples**

If A is square and not singular, then  $pi \, nv(A)$  is an expensive way to compute  $i \, nv(A)$ . If A is not square, or is square and singular, then  $i \, nv(A)$  does not exist. In these cases,  $pi \, nv(A)$  has some of, but not all, the properties of  $i \, nv(A)$ .

If A has more rows than columns and is not of full rank, then the overdetermined least squares problem

```
minimize norm(A*x-b)
```

does not have a unique solution. Two of the infinitely many solutions are

$$x = pi nv(A)*b$$
 and

$$y = A \setminus b$$

These two are distinguished by the facts that norm(x) is smaller than the norm of any other solution and that y has the fewest possible nonzero components.

For example, the matrix generated by

```
A = magic(8); A = A(:, 1:6)
```

is an 8-by-6 matrix that happens to have rank(A) = 3.

A =	=					
	64	2	3	61	60	6
	9	55	54	12	13	51
	17	47	46	20	21	43
	40	26	27	37	36	30
	32	34	35	29	28	38
	41	23	22	44	45	19
	49	15	14	52	53	11
	8	58	59	5	4	62

The right-hand side is b = 260\*ones(8, 1),

The scale factor 260 is the 8-by-8 magic sum. With all eight columns, one solution to A\*x = b would be a vector of all 1's. With only six columns, the equations are still consistent, so a solution exists, but it is not all 1's. Since the matrix is rank deficient, there are infinitely many solutions. Two of them are

```
x = pi nv(A) *b
```

# pinv

## which is

x =
1. 1538
1. 4615
1. 3846
1. 3846
1. 4615
1. 1538

and

$$y = A \setminus b$$

### which is

Both of these are exact solutions in the sense that norm(A\*x-b) and norm(A\*y-b) are on the order of roundoff error. The solution x is special because

$$norm(x) = 3.2817$$

is smaller than the norm of any other solution, including  $% \left( 1\right) =\left( 1\right) \left( 1\right) \left($ 

$$norm(y) = 5.0990$$

On the other hand, the solution  $\boldsymbol{y}$  is special because it has only three nonzero components.

### See Also

Matrix inverse
Orthogonal-triangular decomposition
Rank of a matrix
Singular value decomposition

Transform polar or cylindrical coordinates to Cartesian

**Syntax** 

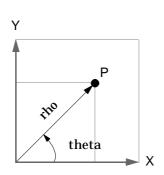
Description

 $[X,Y] = \text{pol}\ 2\text{cart}\ (\text{THETA}, \text{RHO})\$  transforms the polar coordinate data stored in corresponding elements of THETA and RHO to two-dimensional Cartesian, or xy, coordinates. The arrays THETA and RHO must be the same size (or either can be scalar). The values in THETA must be in radians.

[X,Y,Z] = pol 2cart (THETA, RHO, Z) transforms the cylindrical coordinate data stored in corresponding elements of THETA, RHO, and Z to three-dimensional Cartesian, or xyz, coordinates. The arrays THETA, RHO, and Z must be the same size (or any can be scalar). The values in THETA must be in radians.

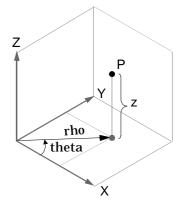
**Algorithm** 

The mapping from polar and cylindrical coordinates to Cartesian coordinates is:



Polar to Cartesian Mapping

theta = 
$$atan2(y, x)$$
  
rho =  $sqrt(x.^2 + y.^2)$ 



Cylindrical to Cartesian Mapping

theta = atan2(y, x)  
rho = sqrt(x.
$$^2 + y.^2$$
)  
z = z

See Also

cart2pol Transform Cartesian coordinates to polar or cylindrical cart2sph Transform Cartesian coordinates to spherical sph2cart Transform spherical coordinates to Cartesian

Polynomial with specified roots

**Syntax** 

$$p = pol y(A)$$
  
 $p = pol y(r)$ 

**Description** 

p = pol y(A) where A is an n-by-n matrix returns an n+1 element row vector whose elements are the coefficients of the characteristic polynomial, det(sI-A). The coefficients are ordered in descending powers: if a vector c has n+1 components, the polynomial it represents is  $c_1s^n + \ldots + c_ns + c_{n+1}$ .

p = pol y(r) where r is a vector returns a row vector whose elements are the coefficients of the polynomial whose roots are the elements of r.

**Remarks** 

Note the relationship of this command to

$$r = roots(p)$$

which returns a column vector whose elements are the roots of the polynomial specified by the coefficients row vector p. For vectors, roots and poly are inverse functions of each other, up to ordering, scaling, and roundoff error.

**Examples** 

MATLAB displays polynomials as row vectors containing the coefficients ordered by descending powers. The characteristic equation of the matrix

is returned in a row vector by pol y:

$$p = pol y(A)$$
 $p = 1 -6 -72 -27$ 

The roots of this polynomial (eigenvalues of matrix A) are returned in a column vector by roots:

```
r = roots(p)
r =
12.1229
-5.7345
-0.3884
```

### **Algorithm**

The algorithms employed for pol y and roots illustrate an interesting aspect of the modern approach to eigenvalue computation. pol y(A) generates the characteristic polynomial of A, and roots(pol y(A)) finds the roots of that polynomial, which are the eigenvalues of A. But both pol y and roots use EISPACK eigenvalue subroutines, which are based on similarity transformations. The classical approach, which characterizes eigenvalues as roots of the characteristic polynomial, is actually reversed.

If A is an n-by-n matrix, pol y(A) produces the coefficients c(1) through c(n+1), with c(1) = 1, in

$$det(\lambda I - A) = c_1 \lambda^n + \dots + c_n \lambda + c_{n+1}$$

The algorithm is expressed in an M-file:

```
\begin{array}{lll} z &=& eig(A)\,;\\ c &=& zeros(n+1,\,1)\,; & c(1) &=& 1;\\ for &j &=& 1:\,n\\ &c(2\!:\!j+\!1) &=& c(2\!:\!j+\!1)\!-\!z(j)\!*\!c(1\!:\!j)\,;\\ end \end{array}
```

This recursion is easily derived by expanding the product.

$$(\lambda - \lambda_1)(\lambda - \lambda_2)...(\lambda - \lambda_n)$$

It is possible to prove that poly(A) produces the coefficients in the characteristic polynomial of a matrix within roundoff error of A. This is true even if the eigenvalues of A are badly conditioned. The traditional algorithms for obtaining the characteristic polynomial, which do not use the eigenvalues, do not have such satisfactory numerical properties.

# poly

**See Also** conv Convolution and polynomial multiplication

pol yval Polynomial evaluation

resi due Convert between partial fraction expansion and poly-

nomial coefficients

roots Polynomial roots

Area of polygon

#### **Syntax**

A = pol yarea(X, Y) A = pol yarea(X, Y, dim)

### Description

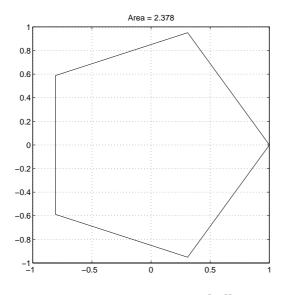
 $A = pol \ yarea(X, Y)$  returns the area of the polygon specified by the vertices in the vectors X and Y.

If X and Y are matrices of the same size, then pol yarea returns the area of polygons defined by the columns X and Y.

If X and Y are multidimensional arrays, pol yarea returns the area of the polygons in the first nonsingleton dimension of X and Y.

A = polyarea(X, Y, dim) operates along the dimension specified by scalar dim.

## **Examples**



#### See Also

convhul l Convex hull i npol ygon Detect points inside a polygonal region

## polyder

**Purpose** 

Polynomial derivative

**Syntax** 

k = pol yder(p)
k = pol yder(a, b)
[q, d] = pol yder(b, a)

**Description** 

The polyder function calculates the derivative of polynomials, polynomial products, and polynomial quotients. The operands a, b, and p are vectors whose elements are the coefficients of a polynomial in descending powers.

k = polyder(p) returns the derivative of the polynomial p.

k = pol yder(a, b) returns the derivative of the product of the polynomials a and b.

[q, d] = polyder(b, a) returns the numerator q and denominator d of the derivative of the polynomial quotient b/a.

**Examples** 

The derivative of the product

$$(3x^2+6x+9)(x^2+2x)$$

is obtained with

a = [3 6 9]; b = [1 2 0]; k = polyder(a, b) k = 12 36 42 18

This result represents the polynomial

$$12\,x^3 + 36\,x^2 + 42\,x + 18$$

See Also

conv deconv Convolution and polynomial multiplication Deconvolution and polynomial division

Polynomial eigenvalue problem

Syntax

[X, e] = pol yeig(A0, A1, ... Ap)

**Description** 

[X, e] = pol yeig(A0, A1, ... Ap) solves the polynomial eigenvalue problem of degree p:

$$(A_0 + \lambda A_1 + \dots + \lambda^P A_p)x = 0$$

where polynomial degree p is a non-negative integer, and A0, A1, . . . Ap are input matrices of order n. Output matrix X, of size n-by-n\*p, contains eigenvectors in its columns. Output vector e, of length n\*p, contains eigenvalues.

Remarks

Based on the values of p and n, polyeig handles several special cases:

- p = 0, or polyeig(A) is the standard eigenvalue problem: eig(A).
- p = 1, or polyei g(A, B) is the generalized eigenvalue problem: ei g(A, -B).
- n = 1, or polyei g(a0,a1,...ap) for scalars a0, a1 ..., ap is the standard polynomial problem: roots([ap ... a1 a0]).

**Algorithm** 

If both AO and Ap are singular, the problem is potentially ill posed; solutions might not exist or they might not be unique. In this case, the computed solutions may be inaccurate. pol yei g attempts to detect this situation and display an appropriate warning message. If either one, but not both, of AO and Ap is singular, the problem is well posed but some of the eigenvalues may be zero or infinite (I nf).

The pol yei g function uses the QZ factorization to find intermediate results in the computation of generalized eigenvalues. It uses these intermediate results to determine if the eigenvalues are well-determined. See the descriptions of eig and qz for more on this, as well as the <code>EISPACK Guide</code>.

See Also

ei g Eigenvalues and eigenvectors

qz QZ factorization for generalized eigenvalues

Polynomial curve fitting

#### **Syntax**

$$p = polyfit(x, y, n)$$
  
[p, s] = polyfit(x, y, n)

### Description

 $p = pol\ yfit(x,y,n)$  finds the coefficients of a polynomial p(x) of degree n that fits the data, p(x(i)) to y(i), in a least squares sense. The result p is a row vector of length n+1 containing the polynomial coefficients in descending powers:

$$p(x) = p_1 x^n + p_2 x^{n-1} + ... + p_n x + p_{n+1}$$

[p,s] = polyfit(x,y,n) returns the polynomial coefficients p and a structure S for use with polyval to obtain error estimates or predictions. If the errors in the data Y are independent normal with constant variance; polyval will produce error bounds that contain at least 50% of the predictions.

## **Examples**

This example involves fitting the error function,  $\operatorname{erf}(x)$ , by a polynomial in x. This is a risky project because  $\operatorname{erf}(x)$  is a bounded function, while polynomials are unbounded, so the fit might not be very good.

First generate a vector of x-points, equally spaced in the interval [0, 2.5]; then evaluate erf(x) at those points.

```
x = (0: 0.1: 2.5)';

y = erf(x);
```

The coefficients in the approximating polynomial of degree 6 are

```
p = polyfit(x, y, 6)
p =
0.0084 -0.0983 0.4217 -0.7435 0.1471 1.1064 0.0004
```

There are seven coefficients and the polynomial is

$$0.0084x^{6} - 0.0983x^{5} + 0.4217x^{4} - 0.7435x^{3} + 0.1471x^{2} + 1.1064x + 0.0004$$

To see how good the fit is, evaluate the polynomial at the data points with

```
f = pol yval (p, x);
```

A table showing the data, fit, and error is

```
table = [x y f y-f]
table =
                                     -0.0004
   0
                           0.0004
   0.1000
               0.1125
                           0.1119
                                      0.0006
   0.2000
               0.2227
                           0.2223
                                      0.0004
   0.3000
               0.3286
                           0.3287
                                     -0.0001
   0.4000
               0.4284
                           0.4288
                                     -0.0004
   . . .
   2.1000
               0.9970
                           0.9969
                                      0.0001
   2.2000
               0.9981
                           0.9982
                                     -0.0001
   2.3000
               0.9989
                           0.9991
                                     -0.0003
   2.4000
               0.9993
                           0.9995
                                     -0.0002
   2.5000
               0.9996
                           0.9994
                                      0.0002
```

So, on this interval, the fit is good to between three and four digits. Beyond this interval the graph shows that the polynomial behavior takes over and the approximation quickly deteriorates.

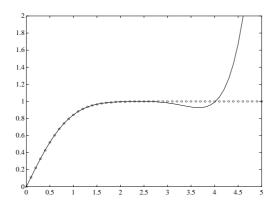
```
x = (0: 0.1: 5)';

y = erf(x);

f = pol yval(p, x);

plot(x, y, 'o', x, f, '-')

axis([0  5  0  2])
```



# polyfit

**Algorithm** 

The M-file forms the Vandermonde matrix, *V*, whose elements are powers of *x*.

$$V_{i,j} = x_i^{n-j}$$

It then uses the backslash operator, \, to solve the least squares problem

$$V_p \cong y$$

The M-file can be modified to use other functions of *x* as the basis functions.

**See Also** 

pol yval Polynomial evaluation roots Polynomial roots

Polynomial evaluation

**Syntax** 

$$y = pol yval (p, x)$$
  
[y, delta] = pol yval (p, x, S)

**Description** 

y = pol yval (p, x) returns the value of the polynomial p evaluated at x. Polynomial p is a vector whose elements are the coefficients of a polynomial in descending powers.

 ${\bf x}$  can be a matrix or a vector. In either case, pol yval evaluates  ${\bf p}$  at each element of  ${\bf x}$ .

[y, delta] = pol yval (p, x, S) uses the optional output structure S generated by pol yfit to generate error estimates,  $y\pm delta$ . If the errors in the data input to pol yfit are independent normal with constant variance,  $y\pm delta$  contains at least 50% of the predictions.

Remarks

The pol yval m(p,x) function, with x a matrix, evaluates the polynomial in a matrix sense. See pol yval m for more information.

**Examples** 

The polynomial  $p(x) = 3x^2 + 2x + 1$  is evaluated at x = 5, 7, and 9 with

which results in

For another example, see polyfit.

See Also

pol yfi t Polynomial curve fitting pol yval m Matrix polynomial evaluation

## polyvalm

**Purpose** 

Matrix polynomial evaluation

**Syntax** 

$$Y = pol yval m(p, X)$$

**Description** 

Y = pol yval m(p, X) evaluates a polynomial in a matrix sense. This is the same as substituting matrix X in the polynomial p.

Polynomial p is a vector whose elements are the coefficients of a polynomial in descending powers, and X must be a square matrix.

**Examples** 

The Pascal matrices are formed from Pascal's triangle of binomial coefficients. Here is the Pascal matrix of order 4.

Its characteristic polynomial can be generated with the poly function.

$$p = pol y(X)$$
 $p = 1 -29 72 -29 1$ 

This represents the polynomial  $x^4 - 29x^3 + 72x^2 - 29x + 1$ .

Pascal matrices have the curious property that the vector of coefficients of the characteristic polynomial is palindromic; it is the same forward and backward.

Evaluating this polynomial at each element is not very interesting.

But evaluating it in a matrix sense is interesting.

The result is the zero matrix. This is an instance of the Cayley-Hamilton theorem: a matrix satisfies its own characteristic equation.

See Also

polyfit	Polynomial curve fitting
pol yval	Polynomial evaluation

## pow2

**Purpose** Base 2 power and scale floating-point numbers

**Syntax** X = pow2(Y)

X = pow2(F, E)

**Description** X = pow2(Y) returns an array X whose elements are 2 raised to the power Y.

X = pow2(F, E) computes  $x = f \cdot 2^e$  for corresponding elements of F and E.The result is computed quickly by simply adding E to the floating-point exponent of

F. Arguments F and E are real and integer arrays, respectively.

**Remarks** This function corresponds to the ANSI C function 1 dexp() and the IEEE

floating-point standard function scal bn().

**Examples** For IEEE arithmetic, the statement X = pow2(F, E) yields the values:

F E X 1/2 1 1 pi/42 рi -3/42 -31/2 -51eps real max 1-eps/21024 1/2-1021real min

**See Also** log2 Base 2 logarithm and dissect floating-point numbers

into exponent and mantissa

^ Matrix power
. ^ Array power
exp Exponential

hex2num Hexadecimal to double number conversion real max Largest positive floating-point number real min Smallest positive floating-point number

**Purpose** Generate list of prime numbers

**Syntax** p = primes(n)

**Description** p = primes(n) returns a row vector of the prime numbers less than or equal

to n. A prime number is one that has no factors other than 1 and itself.

**Examples** p = primes(37)

p =

2 3 5 7 11 13 17 19 23 29 31 37

**See Also** factor Prime factors

## prod

**Purpose** 

Product of array elements

**Syntax** 

**Description** 

B = prod(A) returns the products along different dimensions of an array.

If A is a vector, prod(A) returns the product of the elements.

If A is a matrix, prod(A) treats the columns of A as vectors, returning a row vector of the products of each column.

If A is a multidimensional array, prod(A) treats the values along the first non-singleton dimension as vectors, returning an array of row vectors.

B = prod(A, dim) takes the products along the dimension of A specified by scalar dim

**Examples** 

The magic square of order 3 is

The product of the elements in each column is

The product of the elements in each row can be obtained by:

See Also

cumprodCumulative productdiffDifferencesumSum of array elements

Measure and display M-file execution profiles

#### Syntax

profile function
profile report
profile report n
profile report frac
profile on
profile off
profile done
profile reset
info = profile

#### Description

The profiler utility helps you debug and optimize M-files by tracking the cumulative execution time of each line of code. The utility creates a vector of "bins," one bin for every line of code in the M-file being profiled. As MATLAB executes the M-file code, the profiler updates each bin with running counts of the time spent executing the corresponding line.

profile *function* starts the profiler for *function*. *function* must be the name of an M-file function or a MATLABPATH relative partial pathname.

profile report displays a profile summary report for the M-file currently being profiled.

profile report n, where n is an integer, displays a report showing the n lines that take the most time.

profile report frac, where frac is a number between 0.0 and 1.0, displays a report of each line that accounts for more than frac of the total time.

profile on and profile off enable and disable profiling, respectively.

profile done turns off the profiler and clears its data.

 $\label{lem:profile} \begin{tabular}{ll} \textbf{profile reset erases the bin contents without disabling profiling or changing the $M$-file under inspection.} \end{tabular}$ 

info = profile returns a structure with the fields:

file	Full path to the function being profiled.
functi on	Name of function being profiled.
interval	Sampling interval in seconds.
count	Vector of sample counts
state	on if the profiler is running and off otherwise.

#### **Remarks**

You can also profile built-in functions. The profiler tracks the number of intervals in which the built-in function was called (an estimate of how much time was spent executing the built-in function).

The profiler's behavior is defined by root object properties and can be manipulated using the set and get commands. See the *Applying MATLAB* for more details.

#### Limitations

The profiler utility can accommodate only one M-file at a time.

## See Also

See also partial path.

Quasi-Minimal Residual method

#### Syntax

```
x = qmr(A, b)
qmr(A, b, tol)
qmr(A, b, tol, maxi t)
qmr(A, b, tol, maxi t, M1)
qmr(A, b, tol, maxi t, M1, M2)
qmr(A, b, tol, maxi t, M1, M2, x0)
x = qmr(A, b, tol, maxi t, M1, M2, x0)
[x, flag] = qmr(A, b, tol, maxi t, M1, M2, x0)
[x, flag, rel res] = qmr(A, b, tol, maxi t, M1, M2, x0)
[x, flag, rel res, i ter] = qmr(A, b, tol, maxi t, M1, M2, x0)
[x, flag, rel res, i ter, resvec] = qmr(A, b, tol, maxi t, M1, M2, x0)
```

#### Description

x = qmr(A, b) attempts to solve the system of linear equations A\*x=b for x. The coefficient matrix A must be square and the right hand side (column) vector b must have length n, where A is n-by-n. qmr will start iterating from an initial estimate that by default is an all zero vector of length n. Iterates are produced until the method either converges, fails, or has computed the maximum number of iterations. Convergence is achieved when an iterate x has relative residual norm(b-A\*x) / norm(b) less than or equal to the tolerance of the method. The default tolerance is 1e-6. The default maximum number of iterations is the minimum of n and 20. No preconditioning is used.

qmr(A, b, tol) specifies the tolerance of the method, tol.

qmr(A, b, tol, maxit) additionally specifies the maximum number of iterations, maxit.

qmr(A, b, tol, maxit, M1) and qmr(A, b, tol, maxit, M1, M2) use left and right preconditioners M1 and M2 and effectively solve the system i nv(M1) \*A\*i nv(M2) \*y = i nv(M1) \*b for y, where x = i nv(M2) \*y. If M1 or M2 is given as the empty matrix ([]), it is considered to be the identity matrix, equivalent to no preconditioning at all. Since systems of equations of the form M1\*y = r are solved using backslash within qmr, it is wise to factor precondi-

tioners into their LU factorizations first. For example, replace qmr(A, b, tol, maxit, M, []) or qmr(A, b, tol, maxit, [], M) with:

```
[M1, M2] = lu(M);

qmr(A, b, tol, maxit, M1, M2).
```

qmr(A, b, tol, maxit, M1, M2, x0) specifies the initial estimate x0. If x0 is given as the empty matrix ([]), the default all zero vector is used.

x = qmr(A, b, tol, maxit, M1, M2, x0) returns a solution x. If qmr converged, a message to that effect is displayed. If qmr failed to converge after the maximum number of iterations or halted for any reason, a warning message is printed displaying the relative residual norm(b-A\*x)/norm(b) and the iteration number at which the method stopped or failed.

[x, flag] = qmr(A, b, tol, maxit, M1, M2, x0) returns a solution x and a flag which describes the convergence of qmr:

Flag	Convergence
0	qmr converged to the desired tolerance tol within maxit iterations without failing for any reason.
1	qmr iterated maxi t times but did not converge.
2	One of the systems of equations of the form $M^*y=r$ involving one of the preconditioners was ill-conditioned and did not return a useable result when solved by \ (backslash).
3	The method stagnated. (Two consecutive iterates were the same.)
4	One of the scalar quantities calculated during $\ensuremath{qmr}\xspace$ became too small or too large to continue computing.

Whenever  ${\tt fl}$  ag is not 0, the solution x returned is that with minimal norm residual computed over all the iterations. No messages are displayed if the  ${\tt fl}$  ag output is specified.

[x, flag, relres] = qmr(A, b, tol, maxit, M1, M2, x0) also returns the relative residual norm(b-A\*x)/norm(b). If flag is 0, then relres  $\leq$  tol.

[x, flag, relres, iter] = qmr(A, b, tol, maxit, M1, M2, x0) also returns the iteration number at which x was computed. This always satisfies  $0 \le iter \le maxit$ .

[x, flag, rel res, i ter, resvec] = qmr(A, b, tol, maxi t, M1, M2, x0) also returns a vector of the residual norms at each iteration, starting from resvec(1) = norm(b-A\*x0). If flag is 0, resvec is of length i ter+1 and resvec(end)  $\leq$  tol\*norm(b).

#### **Examples**

```
load west0479
A = west0479
b = sum(A, 2)
[x, flag] = qmr(A, b)
```

fl ag is 1 since qmr will not converge to the default tolerance  $1\mathrm{e}{-6}$  within the default 20 iterations.

```
[L1, U1] = luinc(A, 1e-5)

[x1, flag1] = qmr(A, b, 1e-6, 20, L1, U1)
```

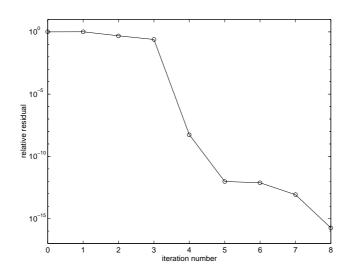
fl ag1 is 2 since the upper triangular U1 has a zero on its diagonal so qmr fails in the first iteration when it tries to solve a system such as U1\*y = r for y with backslash.

```
[L2, U2] = luinc(A, 1e-6)
[x2, flag2, relres2, iter2, resvec2] = qmr(A, b, 1e-15, 10, L2, U2)
```

fl ag2 is 0 since qmr will converge to the tolerance of 1. 9e-16 (the value of rel res2) at the eighth iteration (the value of i ter2) when preconditioned by the incomplete LU factorization with a drop tolerance of 1e-6. resvec2(1) = norm(b) and resvec2(9) = norm(b-A\*x2). You may follow the progress of qmr

## qmr

by plotting the relative residuals at each iteration starting from the initial estimate (iterate number 0) with semilogy(0: i ter2, resvec2/norm(b), '-o').



### See Also

bi cg	BiConjugate Gradients method
bicgstab	BiConjugate Gradients Stabilized method
cgs	Conjugate Gradients Squared method
gmres	Generalized Minimum Residual method (with restarts)
l ui nc	Incomplete LU matrix factorizations
pcg	Preconditioned Conjugate Gradients method
\	Matrix left division

#### References

Freund, Roland W. and Nöel M. Nachtigal,  $\mathit{QMR}$ : A quasi-minimal residual method for non-Hermitian linear systems, Journal: Numer. Math. 60, 1991, pp. 315-339

Templates for the Solution of Linear Systems: Building Blocks for Iterative Methods, SIAM, Philadelphia, 1994.

Orthogonal-triangular decomposition

**Syntax** 

$$[Q, R] = qr(X)$$
  
 $[Q, R, E] = qr(X)$   
 $[Q, R] = qr(X, 0)$   
 $[Q, R, E] = qr(X, 0)$   
 $A = qr(X)$ 

### Description

The qr function performs the orthogonal-triangular decomposition of a matrix. This factorization is useful for both square and rectangular matrices. It expresses the matrix as the product of a real orthonormal or complex unitary matrix and an upper triangular matrix.

[Q, R] = qr(X) produces an upper triangular matrix R of the same dimension as X and a unitary matrix Q so that X = Q\*R.

[Q,R,E]=qr(X) produces a permutation matrix E, an upper triangular matrix R with decreasing diagonal elements, and a unitary matrix Q so that X\*E=Q\*R. The column permutation E is chosen so that abs(diag(R)) is decreasing.

[Q, R] = qr(X, 0) and [Q, R, E] = qr(X, 0) produce "economy-size" decompositions in which E is a permutation vector, so that Q\*R = X(:, E). The column permutation E is chosen so that abs(diag(R)) is decreasing.

A = qr(X) returns the output of the LINPACK subroutine ZQRDC. triu(qr(X)) is R.

## **Examples**

Start with

This is a rank-deficient matrix; the middle column is the average of the other two columns. The rank deficiency is revealed by the factorization:

$$\begin{array}{l} [\,Q,\,R\,] \ = \ qr\,(A) \\ Q \ = \\ -0.\ 0776 \ -0.\ 8331 \ 0.\ 5444 \ 0.\ 0605 \\ -0.\ 3105 \ -0.\ 4512 \ -0.\ 7709 \ 0.\ 3251 \\ -0.\ 5433 \ -0.\ 0694 \ -0.\ 0913 \ -0.\ 8317 \\ -0.\ 7762 \ 0.\ 3124 \ 0.\ 3178 \ 0.\ 4461 \\ R \ = \\ -12.\ 8841 \ -14.\ 5916 \ -16.\ 2992 \\ 0 \ -1.\ 0413 \ -2.\ 0826 \\ 0 \ 0 \ 0.\ 0000 \\ 0 \ 0 \ 0 \end{array}$$

The triangular structure of R gives it zeros below the diagonal; the zero on the diagonal in R(3, 3) implies that R, and consequently A, does not have full rank.

The QR factorization is used to solve linear systems with more equations than unknowns. For example

The linear system Ax = b represents four equations in only three unknowns. The best solution in a least squares sense is computed by

$$x = A \setminus b$$

which produces

```
Warning: Rank deficient, rank = 2, tol = 1.4594E-014

x =

0.5000

0

0.1667
```

The quantity tol is a tolerance used to decide if a diagonal element of R is negligible. If [Q, R, E] = qr(A), then

```
tol = max(size(A))*eps*abs(R(1, 1))
```

The solution x was computed using the factorization and the two steps

$$y = Q' *b;$$
  
 $x = R \setminus y$ 

The computed solution can be checked by forming Ax. This equals b to within roundoff error, which indicates that even though the simultaneous equations Ax = b are overdetermined and rank deficient, they happen to be consistent. There are infinitely many solution vectors x; the QR factorization has found just one of them.

### **Algorithm**

The qr function uses the LINPACK routines ZQRDC and ZQRSL. ZQRDC computes the QR decomposition, while ZQRSL applies the decomposition.

#### See Also

Matrix left division (backslash)

Matrix right division (slash)

lu LU matrix factorization

nul l Null space of a matrix

orth Range space of a matrix

qrdel ete Delete column from QR factorization qri nsert Insert column in QR factorization

#### References

Dongarra, J.J., J.R. Bunch, C.B. Moler, and G.W. Stewart, *LINPACK Users' Guide*, SIAM, Philadelphia, 1979.

## qrdelete

**Purpose** Delete column from QR factorization

**Syntax** [Q, R] = qrdelete(Q, R, j)

**Description** [Q, R] = qrdel ete(Q, R, j) changes Q and R to be the factorization of the

matrix A with its jth column, A(:, j), removed.

Inputs Q and R represent the original QR factorization of matrix A, as returned

by the statement [Q, R] = qr(A). Argument j specifies the column to be

removed from matrix A.

**Algorithm** The grdel ete function uses a series of Givens rotations to zero out the appro-

priate elements of the factorization.

See Also qr Orthogonal-triangular decomposition

qri nsert Insert column in QR factorization

Purpose Insert column in QR factorization

**Syntax** [Q, R] = qri nsert(Q, R, j, x)

 $\label{eq:decomposition} \textbf{Description} \qquad \quad [\,\textbf{Q},\,\textbf{R}\,] \ = \ qri \ nsert \, (\,\textbf{Q},\,\textbf{R},\,\textbf{j}\,,\,\textbf{x}) \quad changes \, \textbf{Q} \ and \, \textbf{R} \ to \ be \ the \ factorization \ of \ the$ 

matrix obtained by inserting an extra column, x, before A(:,j). If A has n columns and j = n+1, then qri nsert inserts x after the last column of A.

Inputs Q and R represent the original QR factorization of matrix A, as returned by the statement [Q, R] = qr(A). Argument x is the column vector to be inserted into matrix A. Argument j specifies the column before which x is

inserted.

**Algorithm** The qri nsert function inserts the values of x into the jth column of R. It then

uses a series of Givens rotations to zero out the nonzero elements of R on and

below the diagonal in the jth column.

See Also qr Orthogonal-triangular decomposition

qrdel et e Delete column from QR factorization

Purpose Write QuickTime movie file to disk

qtwrite(..., options)

### **Description**

qtwri te(d, si z, map, 'fil ename') writes the indexed image deck d with size si z and colormap map to the QuickTime movie file 'fil ename'. If 'fil ename' already exists, it will be replaced.

qtwrite(mov, map, 'filename') writes the MATLAB movie matrix mov with colormap map to the QuickTime movie file 'filename'.

qtwrite(..., options) can be used to set the frame rate, spacial quality, and compressor type:

options(1): frame rate (frames per second) (10 fps default)

options(2): compressor type:

1 - video (default), 2 - jpeg, 3 - animation

options(3): spacial quality:

1 - minimum, 2 - low, 3 - normal (default), 4 - high,

5 - maximum, 6 - lossless

 $\ensuremath{\mbox{qtwri}}$  te requires QuickTime and works only on the Macintosh.

Numerical evaluation of integrals

#### Syntax

```
q = quad('fun', a, b)
q = quad('fun', a, b, tol)
q = quad('fun', a, b, tol, trace)
q = quad('fun', a, b, tol, trace, P1, P2, ...)
q = quad8(...)
```

## Description

*Quadrature* is a numerical method of finding the area under the graph of a function, that is, computing a definite integral.

$$q = \int_{a}^{b} f(x) \, dx$$

q = quad('fun', a, b) returns the result of numerically integrating 'fun' between the limits a and b. 'fun' must return a vector of output values when given a vector of input values.

q = quad('fun', a, b, tol) iterates until the relative error is less than tol. The default value for tol is 1. e-3. Use a two element tolerance vector, tol =  $[rel\_tol\_abs\_tol]$ , to specify a combination of relative and absolute error.

q = quad('fun', a, b, tol, trace) integrates to a relative error of tol, and for non-zero trace, plots a graph showing the progress of the integration.

q = quad('fun', a, b, tol, trace, P1, P2, ...) allows coefficients P1, P2, ... to be passed directly to the specified function: G = fun(X, P1, P2, ...). To use default values for tol or trace, pass in the empty matrix, for example: quad('fun', a, b, [], [], P1).

#### Remarks

quad8, a higher-order method, has the same calling sequence as quad.

## **Examples**

Integrate the sine function from 0 to  $\pi$ :

```
a = quad('sin',0,pi)
a =
2.0000
```

## quad, quad8

## **Algorithm**

quad and quad8 implement two different quadrature algorithms. quad implements a low order method using an adaptive recursive Simpson's rule. quad8 implements a higher order method using an adaptive recursive Newton-Cotes 8 panel rule. quad8 is better than quad at handling functions with soft singularities, for example:

$$\int_0^1 \sqrt{x} \ dx$$

## **Diagnostics**

quad and quad8 have recursion level limits of 10 to prevent infinite recursion for a singular integral. Reaching this limit in one of the integration intervals produces the warning message:

Recursion level limit reached in quad. Singularity likely.

and sets q = i nf.

#### Limitations

Neither quad nor quad8 is set up to handle integrable singularities, such as:

$$\int_0^1 \frac{1}{\sqrt{X}} \, dx$$

If you need to evaluate an integral with such a singularity, recast the problem by transforming the problem into one in which you can explicitly evaluate the integrable singularities and let quad or quad8 take care of the remainder.

#### References

[1] Forsythe, G.E., M.A. Malcolm and C.B. Moler, *Computer Methods for Mathematical Computations*, Prentice-Hall, 1977.

Purpose Terminate MATLAB

**Syntax** qui t

**Description** quit terminates MATLAB without saving the workspace. To save your work-

space variables, use the save command before quitting.

See Also save Save workspace variables on disk

startup MATLAB startup M-file

QZ factorization for generalized eigenvalues

**Syntax** 

$$[AA, BB, Q, Z, V] = qz(A, B)$$

**Description** 

The qz function gives access to what are normally only intermediate results in the computation of generalized eigenvalues.

[AA, BB, Q, Z, V] = qz(A,B) produces upper triangular matrices AA and BB, and matrices Q and Z containing the products of the left and right transformations, such that

$$Q*A*Z = AA$$
$$Q*B*Z = BB$$

The qz function also returns the generalized eigenvector matrix V.

The generalized eigenvalues are the diagonal elements of AA and BB so that

$$A*V*di ag(BB) = B*V*di ag(AA)$$

**Arguments** 

A, B Square matrices.

AA, BB Upper triangular matrices.

Q, Z Transformation matrices.

V Matrix whose columns are eigenvectors.

**Algorithm** 

Complex generalizations of the EISPACK routines QZHES, QZIT, QZVAL, and QZVEC implement the QZ algorithm.

See Also

ei g

Eigenvalues and eigenvectors

References

[1] Moler, C. B. and G.W. Stewart, "An Algorithm for Generalized Matrix Eigenvalue Problems", *SIAM J. Numer. Anal.*, Vol. 10, No. 2, April 1973.

Uniformly distributed random numbers and arrays

#### **Syntax**

```
Y = rand(n)
Y = rand(m, n)
Y = rand([m n])
Y = rand([m n, p, ...))
Y = rand([m n p...])
Y = rand(size(A))
rand
s = rand('state')
```

#### Description

The rand function generates arrays of random numbers whose elements are uniformly distributed in the interval (0,1).

Y = rand(n) returns an n-by-n matrix of random entries. An error message appears if n is not a scalar.

Y = rand(m, n) or Y = rand([m n]) returns an m-by-n matrix of random entries.

Y = rand(m, n, p, ...) or  $Y = rand([m \ n \ p...])$  generates random arrays.

Y = rand(si ze(A)) returns an array of random entries that is the same size as A.

 $\ensuremath{\mathsf{rand}},\ \ensuremath{\mathsf{by}}$  itself, returns a scalar whose value changes each time it's referenced.

s = rand('state') returns a 35-element vector containing the current state of the uniform generator. To change the state of the generator:

rand('state',s)	Resets the state to s.
rand('state',0)	Resets the generator to its initial state.
<pre>rand('state',j)</pre>	For integer $j$ , resets the generator to its $j$ -th state.
rand('state', sum(100*clock))	Resets it to a different state each time.

#### Remarks

MATLAB 5 uses a new multiseed random number generator that can generate all the floating-point numbers in the closed interval  $[2^{-53},1-2^{-53}].$  Theoretically, it can generate over  $2^{1492}$  values before repeating itself. MATLAB 4 used random number generators with a single seed. rand('seed',0) and rand('seed',j) use the MATLAB 4 generator. rand('seed') returns the current seed of the MATLAB 4 uniform generator. rand('state',j) and rand('state',s) use the MATLAB 5 generator.

## **Examples**

R = rand(3, 4) may produce

This code makes a random choice between two equally probable alternatives.

```
if rand < .5
   'heads'
else
   'tails'
end</pre>
```

#### See Also

randn Normally distributed random numbers and arrays randperm Random permutation sprand Sparse uniformly distributed random matrix sprandn Sparse normally distributed random matrix

Normally distributed random numbers and arrays

#### **Syntax**

```
Y = randn(n)
Y = randn(m, n)
Y = randn([m n])
Y = randn(m, n, p, ...)
Y = randn([m n p...])
Y = randn(size(A))
randn
s = randn('state')
```

#### Description

The randn function generates arrays of random numbers whose elements are normally distributed with mean 0 and variance 1.

Y = randn(n) returns an n-by-n matrix of random entries. An error message appears if n is not a scalar.

Y = randn(m, n) or Y = randn([m n]) returns an m-by-n matrix of random entries.

Y = randn(m, n, p, ...) or  $Y = randn([m \ n \ p...])$  generates random arrays.

Y = randn(size(A)) returns an array of random entries that is the same size as A.

randn, by itself, returns a scalar whose value changes each time it's referenced.

s = randn('state') returns a 2-element vector containing the current state of the normal generator. To change the state of the generator:

```
 randn('state',s) \qquad \qquad Resets \ the \ state \ to \ s.   randn('state',0) \qquad \qquad Resets \ the \ generator \ to \ its \ initial \ state.   randn('state',j) \qquad \qquad For \ integer \ j \ , \ resets \ the \ generator \ to \ its \ j \ th \ state.   randn('state',sum(100*clock)) \qquad Resets \ it \ to \ a \ different \ state \ each \ time.
```

## randn

#### Remarks

MATLAB 5 uses a new multiseed random number generator that can generate all the floating-point numbers in the closed interval  $[2^{-53}, 1-2^{-53}].$  Theoretically, it can generate over  $2^{1492}$  values before repeating itself. MATLAB 4 used random number generators with a single seed. randn('seed',0) and randn('seed',j) use the MATLAB 4 generator. randn('seed') returns the current seed of the MATLAB 4 normal generator. randn('state',j) and randn('state',s) use the MATLAB 5 generator.

## **Examples**

R = randn(3, 4) may produce

For a histogram of the randn distribution, see hi st.

#### See Also

rand	Uniformly distributed random numbers and arrays
randperm	Random permutation
sprand	Sparse uniformly distributed random matrix
sprandn	Sparse normally distributed random matrix

## randperm

**Purpose** Random permutation

**Syntax** p = randperm(n)

**Description** p = randperm(n) returns a random permutation of the integers 1: n.

**Remarks** The randperm function calls rand and therefore changes rand's seed value.

**Examples** randperm(6) might be the vector

[3 2 6 4 1 5]

or it might be some other permutation of 1: 6.

**See Also** permute Rearrange the dimensions of a multidimensional array

Purpose Rank of a matrix

**Syntax** k = rank(A)

k = rank(A, tol)

### **Description**

The rank function provides an estimate of the number of linearly independent rows or columns of a matrix.

k = rank(A) returns the number of singular values of A that are larger than the default tolerance, max(si ze(A))\*norm(A)\*eps.

k = rank(A, tol) returns the number of singular values of A that are larger than tol.

### **Algorithm**

There are a number of ways to compute the rank of a matrix. MATLAB uses the method based on the singular value decomposition, or SVD, described in Chapter 11 of the *LINPACK Users' Guide*. The SVD algorithm is the most time consuming, but also the most reliable.

The rank algorithm is

```
s = svd(A);
tol = max(size(A))*s(1)*eps;
r = sum(s > tol);
```

#### References

[1] Dongarra, J.J., J.R. Bunch, C.B. Moler, and G.W. Stewart, *LINPACK Users' Guide*, SIAM, Philadelphia, 1979.

Rational fraction approximation

**Syntax** 

### Description

Even though all floating-point numbers are rational numbers, it is sometimes desirable to approximate them by simple rational numbers, which are fractions whose numerator and denominator are small integers. The rat function attempts to do this. Rational approximations are generated by truncating continued fraction expansions. The rats function calls rat, and returns strings.

[N, D] = rat(X) returns arrays N and D so that N. /D approximates X to within the default tolerance, 1. e-6\*norm(X(:), 1).

[N, D] = rat(X, tol) returns N. /D approximating X to within tol.

 $\operatorname{rat}(X)$ , with no output arguments, simply displays the continued fraction.

S = rats(X, strlen) returns a string containing simple rational approximations to the elements of X. Asterisks are used for elements that cannot be printed in the allotted space, but are not negligible compared to the other elements in X. strlen is the length of each string element returned by the rats function. The default is strlen = 13, which allows 6 elements in 78 spaces.

S = rats(X) returns the same results as those printed by MATLAB with format rat.

# **Examples**

Ordinarily, the statement

$$s = 1 - 1/2 + 1/3 - 1/4 + 1/5 - 1/6 + 1/7$$

produces

```
However, with
```

format rat

or with

rats(s)

the printed result is

$$s = 319/420$$

This is a simple rational number. Its denominator is 420, the least common multiple of the denominators of the terms involved in the original expression. Even though the quantity s is stored internally as a binary floating-point number, the desired rational form can be reconstructed.

To see how the rational approximation is generated, the statement  $\operatorname{rat}(s)$  produces

$$1 + 1/(-4 + 1/(-6 + 1/(-3 + 1/(-5))))$$

And the statement

$$[n, d] = rat(s)$$

produces

$$n = 319, d = 420$$

The mathematical quantity  $\pi$  is certainly not a rational number, but the MATLAB quantity pi that approximates it is a rational number. With IEEE floating-point arithmetic, pi is the ratio of a large integer and  $2^{52}$ :

```
14148475504056880/4503599627370496
```

However, this is not a simple rational number. The value printed for pi with format rat, or with rats(pi), is

```
355/113
```

This approximation was known in Euclid's time. Its decimal representation is

3. 14159292035398

and so it agrees with pi to seven significant figures. The statement

produces

$$3 + 1/(7 + 1/(16))$$

This shows how the 355/113 was obtained. The less accurate, but more familiar approximation 22/7 is obtained from the first two terms of this continued fraction.

**Algorithm** 

The rat (X) function approximates each element of X by a continued fraction of the form:

$$\frac{n}{d} = d_1 + \frac{1}{d_2 + \frac{1}{\left(d_3 + \dots + \frac{1}{d_k}\right)}}$$

The *d*'s are obtained by repeatedly picking off the integer part and then taking the reciprocal of the fractional part. The accuracy of the approximation increases exponentially with the number of terms and is worst when X = sqrt(2). For x = sqrt(2), the error with k terms is about 2.  $68*(.173)^k$ , so each additional term increases the accuracy by less than one decimal digit. It takes 21 terms to get full floating-point accuracy.

# rcond

Purpose Matrix reciprocal condition number estimate

**Syntax** c = rcond(A)

**Description** c = rcond(A) returns an estimate for the reciprocal of the condition of A in

1-norm using the LINPACK condition estimator. If A is well conditioned, rcond(A) is near 1.0. If A is badly conditioned, rcond(A) is near 0.0. Compared to cond, rcond is a

more efficient, but less reliable, method of estimating the condition of a matrix.

**Algorithm** The roond function uses the condition estimator from the LINPACK routine ZGECO.

See Also Condition number with respect to inversion

condest 1-norm matrix condition number estimate

norm Vector and matrix norms

normest 2-norm estimate rank Rank of a matrix

svd Singular value decomposition

**References** [1] Dongarra, J.J., J.R. Bunch, C.B. Moler, and G.W. Stewart, *LINPACK* 

Users' Guide, SIAM, Philadelphia, 1979.

**Purpose** Read snd resources and files

**Syntax** [y, Fs] = readsnd(filename)

**Description** [y, Fs] = readsnd(*filename*) reads the sound data from the first 'snd'

resource in the file filename. The sampled sound data is returned in y, while

the frequency of the sampled sound is placed in Fs.

**Example** [y, Fs] = readsnd('gong. snd')

# real

**Purpose** Real part of complex number

Syntax X = real(Z)

**Description** X = real(Z) returns the real part of the elements of the complex array Z.

**Examples** real (2+3\*i) is 2.

See Also abs Absolute value and complex magnitude

angle Phase angle

 $\begin{array}{ccc} conj & & Complex \ conjugate \\ i\,,\,j & & Imaginary \ unit \ (\sqrt{-1}\,) \end{array}$ 

i mag Imaginary part of a complex number

**Purpose** Largest positive floating-point number

**Syntax** n = real max

**Description** n = real max returns the largest floating-point number representable on a

particular computer. Anything larger overflows.

**Examples** On machines with IEEE floating-point format, real max is one bit less than

2<sup>1024</sup> or about 1. 7977e+308.

Algorithm The real max function is equivalent to pow2(2-eps, maxexp), where maxexp is

the largest possible floating-point exponent.

Execute type real max to see maxexp for various computers.

**See Also** eps Floating-point relative accuracy

real min Smallest positive floating-point number

# realmin

**Purpose** Smallest positive floating-point number

Syntax n = real min

**Description** n = real min returns the smallest positive normalized floating-point number

on a particular computer. Anything smaller underflows or is an IEEE

"denormal."

**Examples** On machines with IEEE floating-point format, real min is 2^(-1022) or about

2. 2251e-308.

Algorithm The real min function is equivalent to pow2(1, minexp) where minexp is the

smallest possible floating-point exponent.

Execute type real min to see minexp for various computers.

**See Also** eps Floating-point relative accuracy

real max Largest positive floating-point number

# **Purpose** Record sound **Syntax** y = recordsound(seconds) y = recordsound(seconds, samplerate) y = recordsound(seconds, numchannels) y = recordsound(seconds, samplerate, numchannels) Description y = recordsound(seconds) records a monophonic sound for seconds number of seconds at the lowest sampling rate (usually 11 or 22 kHz) and highest resolution (usually 8 or 16 bits) that the Macintosh supports. y = recordsound(seconds, sample rate) records a sound at a sampling rate greater than or equal to sample rate, or at the maximum sampling rate that the Macintosh supports. y = recordsound(seconds, numchannels) records a sound with numchannels (usually 1 or 2) channels. If numchannels is 2 and the Macintosh does not support stereo recording, a monophonic sound is recorded instead. y = recordsound(seconds, sample rate, numchannels) records a sound a the specified sampling rate and with the specified number of channels. **Examples** y = recordsound(10)y = recordsound(5, 22050)

y = recordsound(5, 2)

y = recordsound(5, 44100, 2)

### rem

**Purpose** Remainder after division

**Syntax** R = rem(X, Y)

**Description** R = rem(X, Y) returns  $X - fix(X, /Y) \cdot *Y$ , where fix(X, /Y) is the integer part

of the quotient, X. /Y.

**Remarks** So long as operands X and Y are of the same sign, the statement rem(X, Y)

returns the same result as does mod(X, Y). However, for positive X and Y,

rem(-x, y) = mod(-x, y) - y

The rem function returns a result that is between 0 and sign(X) \*abs(Y). If Y

is zero, rem returns NaN.

**Limitations** Arguments X and Y should be integers. Due to the inexact representation of

floating-point numbers on a computer, real (or complex) inputs may lead to

unexpected results.

See Also mod Modulus (signed remainder after division)

Replicate and tile an array

### **Syntax**

```
B = repmat(A, m, n)
B = repmat(A, [m n])
B = repmat(A, [m n p...])
repmat(A, m, n)
```

# Description

B = repmat(A, m, n) creates a large matrix B consisting of an m-by-n tiling of copies of A. The statement repmat (A, n) creates an n-by-n tiling.

B = repmat(A, [m n]) accomplishes the same result as repmat(A, m, n).

 $B = repmat(A, [m \ n \ p...])$  produces a multidimensional (m-by-n-by-p-by-...) array composed of copies of A. A may be multidimensional.

repmat (A, m, n) when A is a scalar, produces an m-by-n matrix filled with A's value. This can be much faster than a\*ones(m, n) when m or n is large.

### **Examples**

In this example, repmat replicates 12 copies of the second-order identity matrix, resulting in a "checkerboard" pattern.

$$B = repmat(eye(2), 3, 4)$$

The statement N = repmat(NaN, [2 3]) creates a 2-by-3 matrix of NaNs.

# reshape

### **Purpose**

### Reshape array

### **Syntax**

B = reshape(A, m, n)

B = reshape(A, m, n, p, ...)

B = reshape(A, [m n p...])

B = reshape(A, siz)

# Description

B = reshape(A, m, n) returns the m-by-n matrix B whose elements are taken column-wise from A. An error results if A does not have m\*n elements.

 $B = reshape(A, m, n, p, \dots) \ or \ B = reshape(A, [m \ n \ p, \dots]) \ returns \ an \ N-D$  array with the same elements as X but reshaped to have the size m-by-n-by-p-by-...  $m^*n^*p^*... \ must \ be \ the \ same \ as \ prod(size(x)).$ 

B = reshape(A, siz) returns an N-D array with the same elements as A, but reshaped to siz, a vector representing the dimensions of the reshaped array. The quantity prod(siz) must be the same as prod(size(A)).

# **Examples**

Reshape a 3-by-4 matrix into a 2-by-6 matrix:

B = reshape(A, 2, 6)

#### See Also

: (colon) Colon :

shift dimensions

squeeze Remove singleton dimensions

Convert between partial fraction expansion and polynomial coefficients

**Syntax** 

Description

The residue function converts a quotient of polynomials to pole-residue representation, and back again.

[r, p, k] = residue(b, a) finds the residues, poles, and direct term of a partial fraction expansion of the ratio of two polynomials, b(s) and a(s), of the form:

$$\frac{b(s)}{a(s)} = \frac{b_1 + b_2 s^{-1} + b_3 s^{-2} + \dots + b_{m+1} s^{-m}}{a_1 + a_2 s^{-1} + a_3 s^{-2} + \dots + a_{m+1} s^{-m}}$$

[b,a] = residue(r,p,k) converts the partial fraction expansion back to the polynomials with coefficients in b and a.

**Definition** 

If there are no multiple roots, then:

$$\frac{b(s)}{a(s)} = \frac{r_1}{s - p_1} + \frac{r_2}{s - p_2} + \dots + \frac{r_n}{s - p_n} + k(s)$$

The number of poles n is

$$n = l \operatorname{ength}(a) - 1 = l \operatorname{ength}(r) = l \operatorname{ength}(p)$$

The direct term coefficient vector is empty if  $l \, ength(b) \, < \, l \, ength(a)$ ; otherwise

$$l ength(k) = l ength(b) - l ength(a) + 1$$

If  $p(j) = \dots = p(j+m-1)$  is a pole of multiplicity m, then the expansion includes terms of the form

$$\frac{r_j}{s - p_j} + \frac{r_{j+1}}{(s - p_j)^2} + \dots + \frac{r_{j+m-1}}{(s - p_j)^m}$$

# residue

### **Arguments**

- b, a Vectors that specify the coefficients of the polynomials in descending powers of *s*
- r Column vector of residues
- p Column vector of poles
- k Row vector of direct terms

### **Algorithm**

The resi due function is an M-file. It first obtains the poles with roots. Next, if the fraction is nonproper, the direct term k is found using deconv, which performs polynomial long division. Finally, the residues are determined by evaluating the polynomial with individual roots removed. For repeated roots, the M-file resi 2 computes the residues at the repeated root locations.

#### Limitations

Numerically, the partial fraction expansion of a ratio of polynomials represents an ill-posed problem. If the denominator polynomial, a(s), is near a polynomial with multiple roots, then small changes in the data, including roundoff errors, can make arbitrarily large changes in the resulting poles and residues. Problem formulations making use of state-space or zero-pole representations are preferable.

#### See Also

deconv Deconvolution and polynomial division poly Polynomial with specified roots

roots Polynomial roots

#### References

[1] Oppenheim, A.V. and R.W. Schafer, *Digital Signal Processing*, Prentice-Hall, 1975, p. 56.

**Purpose** Return to the invoking function

Syntax return

**Description** return causes a normal return to the invoking function or to the keyboard. It

also terminates keyboard mode.

**Examples** If the determinant function were an M-file, it might use a return statement in handling the special case of an empty matrix as follows:

```
function d = det(A)
%DET det(A) is the determinant of A.
if isempty(A)
    d = 1;
    return
else
    ...
end
```

See Also brea

break Break out of flow control structures

di sp Display text or array

end Terminate for, while, switch, and if statements or

indicate last index

error Display error messages

for Repeat statements a specific number of times

i f Conditionally execute statements keyboard Invoke the keyboard in an M-file

switch Switch among several cases based on expression while Repeat statements an indefinite number of times

# rmfield

**Purpose** Remove structure fields **Syntax** s = rmfield(s, 'field')s = rmfield(s, FIELDS)s = rmfield(s, 'field') removes the specified field from the structure array Description s. s = rmfield(s, FIELDS) removes more than one field at a time when FIELDS is a character array of field names or cell array of strings. See Also fields Field names of a structure Get field of structure array getfi el d Set field of structure array setfield Vertical concatenation of strings strvcat

**Purpose** Remove directories from MATLAB's search path

**Syntax** rmpath directory

**Description** rmpath directory removes the specified directory from MATLAB's current

search path.

**Remarks** The function syntax form is also acceptable:

rmpath('directory')

**Examples** rmpath /usr/local/matlab/mytools

See Also addpath Add directories to MATLAB's search path

path Control MATLAB's directory search path

Polynomial roots

**Syntax** 

r = roots(c)

**Description** 

r = roots(c) returns a column vector whose elements are the roots of the polynomial c.

Row vector  $_{\rm C}$  contains the coefficients of a polynomial, ordered in descending powers. If  $_{\rm C}$  has  $_{\rm n+1}$  components, the polynomial it represents is

$$c_1 s^n + \ldots + c_n s + c_{n+1}$$
.

Remarks

Note the relationship of this function to  $p = pol \, y(r)$ , which returns a row vector whose elements are the coefficients of the polynomial. For vectors, roots and pol y are inverse functions of each other, up to ordering, scaling, and roundoff error.

**Examples** 

The polynomial  $s^3 - 6s^2 - 72s - 27$  is represented in MATLAB as

$$p = [1 -6 -72 -27]$$

The roots of this polynomial are returned in a column vector by

**Algorithm** 

The algorithm simply involves computing the eigenvalues of the companion matrix:

```
A = di ag(ones(n-2, 1), -1);

A(1,:) = -c(2: n-1)./c(1);

ei g(A)
```

It is possible to prove that the results produced are the exact eigenvalues of a matrix within roundoff error of the companion matrix A, but this does not mean that they are the exact roots of a polynomial with coefficients within roundoff error of those in  $_{\rm C}$ .

See A	ISO
-------	-----

 $\begin{array}{ccc} fzero & Zero \ of \ a \ function \ of \ one \ variable \\ pol \ y & Polynomial \ with \ specified \ roots \end{array}$ 

resi due Convert between partial fraction expansion and poly-

nomial coefficients

# rot90

**Purpose** 

Rotate matrix 90°

**Syntax** 

B = rot 90(A) B = rot 90(A, k)

Description

B = rot 90(A) rotates matrix A counterclockwise by 90 degrees.

 $B = {\tt rot}\,90(A,k)~{\tt rotates}\,matrix\,A$  counterclockwise by k\*90 degrees, where k is an integer.

**Examples** 

The matrix

rotated by 90 degrees is

Y = rot90(X) Y = 3 6 9 2 5 8 1 4 7

See Also

 $\begin{array}{ll} \hbox{fl\,i\,pdi\,m} & \hbox{Flip array along a specified dimension} \\ \hbox{fl\,i\,pl\,r} & \hbox{Flip matrices left-right} \\ \hbox{fl\,i\,pud} & \hbox{Flip matrices up-down} \end{array}$ 

**Purpose** Round to nearest integer

**Syntax** Y = round(X)

**Description** Y = round(X) rounds the elements of X to the nearest integers. For complex X,

the imaginary and real parts are rounded independently.

**Examples** a =

Columns 1 through 4

-1. 9000 -0. 2000

3.4000

5.6000

Columns 5 through 6

7. 0000 2. 4000 + 3. 6000i

round(a)

ans =

Columns 1 through 4

**-2**. 0000 0 3. 0000 6. 0000

Columns 5 through 6

7. 0000 2. 0000 + 4. 0000i

See Also ceil Round toward infinity

fix Round towards zero

floor Round towards minus infinity

# rref, rrefmovie

### **Purpose**

Reduced row echelon form

### **Syntax**

### Description

R = rref(A) produces the reduced row echelon form of A using Gauss Jordan elimination with partial pivoting. A default tolerance of (max(size(A))\*eps\*norm(A, inf)) tests for negligible column elements.

[R, jb] = rref(A) also returns a vector jb so that:

- r = l ength(jb) is this algorithm's idea of the rank of A,
- x(jb) are the bound variables in a linear system Ax = b,
- A(:, j b) is a basis for the range of A,
- R(1: r, j b) is the r-by-r identity matrix.

[R, jb] = rref(A, tol) uses the given tolerance in the rank tests.

Roundoff errors may cause this algorithm to compute a different value for the rank than rank, orth and null.

rrefmovie(A) shows a movie of the algorithm working.

# **Examples**

Use rref on a rank-deficient magic square:

# rref, rrefmovie

See Also inv	Matrix inverse
--------------	----------------

lu LU matrix factorization

rank Rank of a matrix

Convert real Schur form to complex Schur form

**Syntax** 

$$[U, T] = rsf2csf(U, T)$$

**Description** 

The *complex Schur form* of a matrix is upper triangular with the eigenvalues of the matrix on the diagonal. The *real Schur form* has the real eigenvalues on the diagonal and the complex eigenvalues in 2-by-2 blocks on the diagonal.

[U, T] = rsf2csf(U, T) converts the real Schur form to the complex form.

Arguments U and T represent the unitary and Schur forms of a matrix A, respectively, that satisfy the relationships: A = U\*T\*U' and U'\*U = eye(size(A)). See schur for details.

**Examples** 

Given matrix A,

1	1	1	3
1	2	1	1
1	1	3	1
-2	1	1	4

with the eigenvalues

```
1.9202 - 1.4742i 1.9202 + 1.4742i 4.8121 1.3474
```

Generating the Schur form of A and converting to the complex Schur form

```
[u, t] = schur(A);
[U, T] = rsf2csf(u, t)
```

yields a triangular matrix T whose diagonal consists of the eigenvalues of A.

U =

```
-0.4576 + 0.3044i
                    0.5802 - 0.4934i
                                        -0.0197
                                                  -0.3428
0.1616 + 0.3556i
                    0.4235 + 0.0051i
                                        0.1666
                                                   0.8001
 0.3963 + 0.2333i
                    0.1718 + 0.2458i
                                        0.7191
                                                  -0.4260
-0.4759 - 0.3278i
                   -0.2709 - 0.2778i
                                         0.6743
                                                    0.2466
```

See Also schur Schur decomposition

Save workspace variables on disk

### **Syntax**

save

save filename

save filename variables save filename options

save filename variables options

### Description

save, by itself, stores all workspace variables in a binary format in the file named matl ab. mat. The data can be retrieved with load.

save filename stores all workspace variables in filename. mat instead of the default matlab. mat. If filename is the special string stdio, the save command sends the data as standard output.

save filename variables saves only the workspace variables you list after the filename.

### **Options**

The forms of the save command that use *options* are:

save filename options

save filename variables options,

Each specifies a particular ASCII data format, as opposed to the binary MAT-file format, in which to save data. Valid option combinations are:

With these options	Data is stored in:
-asci i	8-digit ASCII format
-asci i -doubl e	16-digit ASCII format
-ascii -tabs	8-digit ASCII format, tab-separated
-asci i -doubl e -tabs	16-digit ASCII format, tab-separated

Variables saved in ASCII format merge into a single variable that takes the name of the ASCII file. Therefore, loading the file *filename* shown above

results in a single workspace variable named *filename*. Use the colon operator to access individual variables.

### Limitations

Saving complex data with the -ascii keyword causes the imaginary part of the data to be lost, as MATLAB cannot load nonnumeric data (' i').

#### Remarks

The save and load commands retrieve and store MATLAB variables on disk. They can also import and export numeric matrices as ASCII data files.

MAT-files are double-precision binary MATLAB format files created by the save command and readable by the 1 oad command. They can be created on one machine and later read by MATLAB on another machine with a different floating-point format, retaining as much accuracy and range as the disparate formats allow. They can also be manipulated by other programs, external to MATLAB.

**Alternative syntax:** The function form of the syntax, save ('filename'), is also permitted.

### **Algorithm**

The binary formats used by save depend on the size and type of each array. Arrays with any noninteger entries and arrays with 10,000 or fewer elements are saved in floating-point formats requiring eight bytes per real element. Arrays with all integer entries and more than 10,000 elements are saved in the formats shown, requiring fewer bytes per element.

Element Range	Bytes per Element
0 to 255	1
0 to 65535	2
-32767 to 32767	2
$-2^{31}+1$ to $2^{31}-1$	4
other	8

The Application Program Interface Libraries contain C and Fortran routines to read and write MAT-files from external programs. It is important to use recommended access methods, rather than rely upon the specific file format, which is likely to change in the future.

See Also	fprintf	Write formatted data to file
	fwrite	Write binary data to a file

fwrite Write binary data to a file load Retrieve variables from disk

Schur decomposition

**Syntax** 

Description

The schur command computes the Schur form of a matrix.

[U, T] = schur(A) produces a Schur matrix T, and a unitary matrix U so that A = U\*T\*U' and U'\*U = eye(size(A)).

T = schur(A) returns just the Schur matrix T.

**Remarks** 

The *complex Schur form* of a matrix is upper triangular with the eigenvalues of the matrix on the diagonal. The *real Schur form* has the real eigenvalues on the diagonal and the complex eigenvalues in 2-by-2 blocks on the diagonal.

If the matrix A is real, schur returns the real Schur form. If A is complex, schur returns the complex Schur form. The function rsf2csf converts the real form to the complex form.

**Examples** 

H is a 3-by-3 eigenvalue test matrix:

$$\begin{array}{ccccc} H & = & & & \\ & -149 & & -50 & & -154 \\ & 537 & & 180 & & 546 \\ & -27 & & -9 & & -25 \end{array}$$

Its Schur form is

The eigenvalues, which in this case are 1, 2, and 3, are on the diagonal. The fact that the off-diagonal elements are so large indicates that this matrix has poorly conditioned eigenvalues; small changes in the matrix elements produce relatively large changes in its eigenvalues.

Algorithm

For real matrices, schur uses the EISPACK routines <code>ORTRAN</code>, <code>ORTHES</code>, and <code>HQR2</code>. <code>ORTHES</code> converts a real general matrix to Hessenberg form using <code>orthogonal</code>

similarity transformations. ORTRAN accumulates the transformations used by ORTHES. HQR2 finds the eigenvalues of a real upper Hessenberg matrix by the QR method.

The EISPACK subroutine HQR2 has been modified to allow access to the Schur form, ordinarily just an intermediate result, and to make the computation of eigenvectors optional.

When schur is used with a complex argument, the solution is computed using the QZ algorithm by the EISPACK routines QZHES, QZIT, QZVAL, and QZVEC. They have been modified for complex problems and to handle the special case B = I.

For detailed descriptions of these algorithms, see the *EISPACK Guide*.

#### See Also

ei g Eigenvalues and eigenvectors hess Hessenberg form of a matrix

qz QZ factorization for generalized eigenvalues rsf2csf Convert real Schur form to complex Schur form

#### References

[1] Garbow, B. S., J. M. Boyle, J. J. Dongarra, and C. B. Moler, *Matrix Eigensystem Routines – EISPACK Guide Extension*, Lecture Notes in Computer Science, Vol. 51, Springer-Verlag, 1977.

[2] Moler, C.B. and G. W. Stewart, "An Algorithm for Generalized Matrix Eigenvalue Problems," *SIAM J. Numer. Anal.*, Vol. 10, No. 2, April 1973.

[3] Smith, B. T., J. M. Boyle, J. J. Dongarra, B. S. Garbow, Y. Ikebe, V. C. Klema, and C. B. Moler, *Matrix Eigensystem Routines – EISPACK Guide*, Lecture Notes in Computer Science, Vol. 6, second edition, Springer-Verlag, 1976.

# script

**Purpose** 

Script M-files

Description

A script file is an external file that contains a sequence of MATLAB statements. By typing the filename, subsequent MATLAB input is obtained from the file. Script files have a filename extension of . m and are often called M-files.

Scripts are the simplest kind of M-file. They are useful for automating blocks of MATLAB commands, such as computations you have to perform repeatedly from the command line. Scripts can operate on existing data in the workspace, or they can create new data on which to operate. Although scripts do not return output arguments, any variables that they create remain in the workspace so you can use them in further computations. In addition, scripts can produce graphical output using commands like pl ot.

Scripts can contain any series of MATLAB statements. They require no declarations or begin/end delimiters.

Like any M-file, scripts can contain comments. Any text following a percent sign (%) on a given line is comment text. Comments can appear on lines by themselves, or you can append them to the end of any executable line.

See Also

echo Echo M-files during execution

function Function M-files

type List file

Secant and hyperbolic secant

**Syntax** 

Y = sec(X)Y = sech(X)

**Description** 

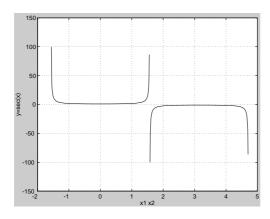
The sec and sech commands operate element-wise on arrays. The functions' domains and ranges include complex values. All angles are in radians.

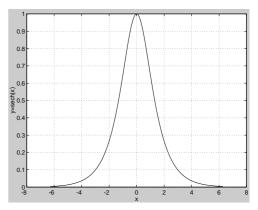
Y = sec(X) returns an array the same size as X containing the secant of the elements of X.

Y = sech(X) returns an array the same size as X containing the hyperbolic secant of the elements of X.

**Examples** 

Graph the secant over the domains  $-\pi/2 < x < \pi/2$  and  $\pi/2 < x < 3\pi/2$ , and the hyperbolic secant over the domain  $-2\pi \le x \le 2\pi$ .





# sec, sech

The expression  $\sec(pi/2)$  does not evaluate as infinite but as the reciprocal of the floating-point accuracy eps, because pi is a floating-point approximation to the exact value of  $\pi$ .

**Algorithm** 

$$\sec(z) = \frac{1}{\cos(z)}$$
  $\operatorname{sech}(z) = \frac{1}{\cosh(z)}$ 

See Also

asec, asech

Inverse secant and inverse hyperbolic secant

Return the set difference of two vectors

# **Syntax**

```
c = setdiff(a, b)
c = setdiff(A, B, 'rows')
[c, i] = setdiff(...)
```

A = magic(5);

# **Description**

 $c = set di \, ff(a, b)$  returns the values in a that are not in b. The resulting vector is sorted is ascending order. In set theoretic terms, c = a - b.

c = (A, B, 'rows') when A and B are matrices with the same number of columns returns the rows from A that are not in B.

[c, i] = setdiff(...) also returns an index vector i ndex such that c = a(i) or c = a(i, :).

### **Examples**

```
B = magic(4);
[c, i] = setdiff(A, B);
        17
                            20
                                               23
               18
                     19
                                  21
                                         22
                                                      24
                                                            25
i' =
        1
               10
                            18
                                  19
                                         23
                                                2
                     14
                                                       6
                                                            15
```

#### See Also

et intersection of two vectors
rue for a set member
t exclusive-or of two vectors
t union of two vectors
nique elements of a vector

Set field of structure array

**Syntax** 

```
s = setfield(s, 'field', v)

s = setfield(s, \{i, j\}, 'field', \{k\}, v)
```

**Description** 

s = setfield(s, 'field', v), where s is a 1-by-1 structure, sets the contents of the specified field to the value v. This is equivalent to the syntax s, field = v.

 $s = setfield(s, \{i, j\}, 'field', \{k\}, v)$  sets the contents of the specified field to the value v. This is equivalent to the syntax s(i, j). field(k) = v. All subscripts must be passed as cell arrays—that is, they must be enclosed in curly braces (similar to $\{i, j\}$  and  $\{k\}$  above). Pass field references as strings.

**Examples** 

Given the structure:

```
mystr(1, 1).name = 'alice';
mystr(1, 1).ID = 0;
mystr(2, 1).name = 'gertrude';
mystr(2, 1).ID = 1
```

Then the command mystr = setfield(mystr, {2, 1}, 'name', 'ted') yields

```
mystr =
2x1 struct array with fields:
   name
   ID
```

See Also

 $\begin{array}{ll} \mbox{fiel ds} & \mbox{Field names of a structure} \\ \mbox{get fiel d} & \mbox{Get field of structure array} \end{array}$ 

# setstr

Purpose Set string flag

**Description** This MATLAB 4 function has been renamed char in MATLAB 5.

**See Also** char Create character array (string)

Set exclusive-or of two vectors

## **Syntax**

```
c = setxor(a, b)
c = setxor(A, B, 'rows')
[c, ia, ib] = setxor(...)
```

## Description

c = setxor(a, b) returns the values that are not in the intersection of a and b. The resulting vector is sorted.

c = setxor(A, B, 'rows') when A and B are matrices with the same number of columns returns the rows that are not in the intersection of A and B.

[c, ia, ib] = setxor(...) also returns index vectors ia and ib such that c is a sorted combination of the elements c = a(ia) and c = b(ib) or, for row combinations, c = a(ia, :) and c = b(ib, :).

## **Examples**

#### See Also

intersect	Set intersection of two vectors
ismember	True for a set member
setdi ff	Set difference of two vectors
uni on	Set union of two vectors
uni que	Unique elements of a vector

Shift dimensions

Syntax

```
B = shiftdim(X, n)
[B, nshifts] = shiftdim(X)
```

Description

 $B = \sinh ft \dim(X, n)$  shifts the dimensions of X by n. When n is positive, shi  $ft \dim m$  shifts the dimensions to the left and wraps the n leading dimensions to the end. When n is negative, shi  $ft \dim m$  shifts the dimensions to the right and pads with singletons.

[B, nshifts] = shiftdim(X) returns the array B with the same number of elements as X but with any leading singleton dimensions removed. A singleton dimension is any dimension for which size(A, dim) = 1. nshifts is the number of dimensions that are removed.

If X is a scalar, shift dim has no effect.

**Examples** 

The shiftdim command is handy for creating functions that, like sum or diff, work along the first nonsingleton dimension.

```
a = rand(1, 1, 3, 1, 2);
[b, n] = shiftdim(a); % b is 3-by-1-by-2 and n is 2.
c = shiftdim(b, -n); % c == a.
d = shiftdim(a, 3); % d is 1-by-2-by-1-by-1-by-3.
```

See Also

reshape Reshape array squeeze Remove singleton dimensions

# sign

**Purpose** Signum function

Syntax Y = sign(X)

**Description** Y = sign(X) returns an array Y the same size as X, where each element of Y is:

• 1 if the corresponding element of X is greater than zero

• 0 if the corresponding element of X equals zero

ullet -1 if the corresponding element of X is less than zero

For nonzero complex X,  $sign(X) = X \cdot /abs(X)$ .

See Also abs Absolute value and complex magnitude

conj Complex conjugate

i mag Imaginary part of a complex number

real Real part of complex number

Sine and hyperbolic sine

**Syntax** 

$$Y = \sin n(X)$$
  
 $Y = \sin n(X)$ 

Description

The  $si\ n$  and  $si\ nh$  commands operate element-wise on arrays. The functions' domains and ranges include complex values. All angles are in radians.

 $Y = \sin n(X)$  returns the circular sine of the elements of X.

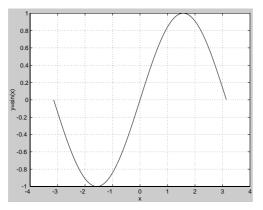
Y = sinh(X) returns the hyperbolic sine of the elements of X.

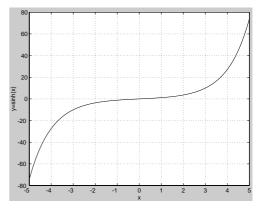
**Examples** 

Graph the sine function over the domain  $-\pi \le x \le \pi$ , and the hyperbolic sine function over the domain  $-5 \le x \le 5$ .

```
x = -pi : 0.01: pi; plot(x, sin(x))

x = -5: 0.01: 5; plot(x, sinh(x))
```





The expression  $\sin n(pi)$  is not exactly zero, but rather a value the size of the floating-point accuracy eps, because pi is only a floating-point approximation to the exact value of  $\pi$ .

# sin, sinh

**Algorithm** 

$$\sin(x+iy) = \sin(x)\cos(y) + i\cos(x)\sin(y)$$

$$\sin(z) = \frac{e^{iz} - e^{-iz}}{2i}$$

$$\sinh(z) = \frac{e^{z} - e^{-z}}{2}$$

See Also

asi n, asi nh

Inverse sine and inverse hyperbolic sine

Array dimensions

## **Syntax**

$$\begin{array}{l} d = size(X) \\ [m, n] = size(X) \\ m = size(X, dim) \\ [d1, d2, d3, ..., dn] = size(X) \end{array}$$

## Description

d = si ze(X) returns the sizes of each dimension of array X in a vector d with ndi ms(X) elements.

[m, n] = size(X) returns the size of matrix X in variables m and n.

m = size(X, dim) returns the size of the dimension of X specified by scalar dim.

 $[d1, d2, d3, \ldots, dn] = si ze(X)$  returns the sizes of the various dimensions of array X in separate variables.

If the number of output arguments n does not equal ndims(X), then:

If n > ndims(X) Ones are returned in the "extra" variables dndims(X)+1 through dn.

 $\begin{array}{ll} If \ n \ < \ ndi \ ms \, (X) & The \ final \ variable \ dn \ contains \ the \ product \ of \ the \ sizes \ of \\ all \ the \ "remaining" \ dimensions \ of \ X, \ that \ is, \ dimensions \\ n+1 \ through \ ndi \ ms \, (X) \ . \end{array}$ 

## **Examples**

The size of the second dimension of rand(2, 3, 4) is 3.

Here the size is output as a single vector.

## size

Here the size of each dimension is assigned to a separate variable.

If X = ones(3, 4, 5), then

$$[d1, d2, d3] = size(X)$$

$$d1 = d2 = d3 = 3$$

but when the number of output variables is less than ndims(X):

$$[d1, d2] = size(X)$$

$$d1 = d2 = 3$$

1

The "extra" dimensions are collapsed into a single product.

If  $n > ndi\,ms(X)$ , the "extra" variables all represent singleton dimensions:

1

$$[d1, d2, d3, d4, d5, d6] = size(X)$$

$$d1 = d2 = d3 = 5$$
 $d4 = d5 = d6 = d6$ 

1

#### See Also

exi st Check if a variable or file exists
l ength Length of vector
whos List directory of variables in memory

Sort elements in ascending order

Syntax

B = sort(A)

[B, INDEX] = sort(A) B = sort(A, di m)

Description

B = sort(A) sorts the elements along different dimensions of an array, and arranges those elements in ascending order.

Real, complex, and string elements are permitted. For identical values in A, the location in the input array determines location in the sorted list. When A is complex, the elements are sorted by magnitude, and where magnitudes are equal, further sorted by phase angle on the interval  $[-\pi,\pi]$ . If A includes any NaN elements, sort places these at the end.

If A is a vector, sort (A) arranges those elements in ascending order.

If A is a matrix, sort (A) treats the columns of A as vectors, returning sorted columns.

If A is a multidimensional array, sort (A) treats the values along the first non-singleton dimension as vectors, returning an array of sorted vectors.

[B, INDEX] = sort(A) also returns an array of indices. INDEX is an array of size(A), each column of which is a permutation vector of the corresponding column of A. If A has repeated elements of equal value, indices are returned that preserve the original relative ordering.

B = sort(A, dim) sorts the elements along the dimension of A specified by scalar dim.

If dim is a vector, sort works iteratively on the specified dimensions. Thus,  $sort(A, [1\ 2])$  is equivalent to sort(sort(A, 2), 1).

See Also

max Maximum elements of an array mean Average or mean value of arrays

median Median value of arrays

min Minimum elements of an array sortrows Sort rows in ascending order

## sortrows

**Purpose** 

Sort rows in ascending order

**Syntax** 

```
B = sortrows(A)
B = sortrows(A, col umn)
[B, index] = sortrows(A)
```

**Description** 

B = sortrows(A) sorts the rows of A as a group in ascending order. Argument A must be either a matrix or a column vector.

For strings, this is the familiar dictionary sort. When A is complex, the elements are sorted by magnitude, and, where magnitudes are equal, further sorted by phase angle on the interval  $[-\pi, \pi]$ .

B = sortrows(A, col umn) sorts the matrix based on the columns specified in the vector col umn. For example,  $\text{sortrows}(A, [2\ 3])$  sorts the rows of A by the second column, and where these are equal, further sorts by the third column.

[B, index] = sortrows(A) also returns an index vector index.

If A is a column vector, then B = A(i ndex).

If A is an m-by-n matrix, then B = A(i ndex, :).

**Examples** 

Given the 5-by-5 string matrix,

```
A = ['one ';'two ';'three';'four ';'five '];
```

The commands B = sortrows(A) and C = sortrows(A, 1) yield

 $\begin{array}{lll} B = & C = \\ \text{five} & \text{four} \\ \text{four} & \text{five} \\ \text{one} & \text{one} \\ \text{three} & \text{two} \\ \end{array}$ 

See Also

sort

Sort elements in ascending order

**Purpose** Convert vector into sound

 $\textbf{Syntax} \qquad \qquad \text{sound}(y, Fs)$ 

sound(y)

sound(y, Fs, bits)

**Description** sound(y, Fs), sends the signal in vector y (with sample frequency Fs) to the

speaker on PC, Macintosh, and most UNIX platforms. Values in y are assumed to be in the range  $-1.0 \le y \le 1.0$ . Values outside that range are clipped. Stereo sound is played on platforms that support it when y is an n-by-2 matrix.

sound(y) plays the sound at the default sample rate or 8192 Hz.

sound(y, Fs, bits) plays the sound using bits bits/sample if possible. Most

platforms support bits = 8 or bits = 16.

**Remarks** MATLAB supports all Windows-compatible sound devices.

See Also auread Read NeXT/SUN (. au) sound file

auwrite Write NeXT/SUN (. au) sound file

soundsc Scale data and play as sound

wavread Read Microsoft WAVE (. wav) sound file waywrite Write Microsoft WAVE (. wav) sound file

# soundcap

**Purpose** Sound capabilities

Syntax soundcap

**Description** soundcap prints the computer's sound capabilities, including whether or not

the computer can play stereo sound and record sound, the sampling rates supported for recording, and the resolution supported for recording and play-

back.

**Purpose** Scale data and play as sound

Syntax soundsc(y, Fs)

soundsc(y)

soundsc(y, Fs, bits)soundsc(y, ..., slim)

**Description** soundsc(y, Fs) sends the signal in vector y (with sample frequency Fs) to the

speaker on PC, Macintosh, and most UNIX platforms. The signal y is scaled to the range  $-1.0 \le y \le 1.0$  before it is played, resulting in a sound that is played

as loud as possible without clipping.

soundsc(y) plays the sound at the default sample rate or 8192 Hz.

 $soundsc(y,Fs,bi\,ts)\ \ plays\ the\ sound\ using\ bi\ ts\ bits/sample\ if\ possible.\ Most$ 

platforms support bits = 8 or bits = 16.

soundsc(y, ..., slim) where slim = [slow shigh] maps the values in y

between  $\operatorname{sl}\nolimits$  ow and  $\operatorname{shi}\nolimits$  gh to the full sound range. The default value is

slim = [min(y) max(y)].

**Remarks** MATLAB supports all Windows-compatible sound devices.

See Also auread Read NeXT/SUN (. au) sound file

auwri te Write NeXT/SUN (. au) sound file

sound Convert vector into sound

wavread Read Microsoft WAVE (. wav) sound file wavwrite Write Microsoft WAVE (. wav) sound file

# spalloc

**Purpose** 

Allocate space for sparse matrix

**Syntax** 

```
S = spalloc(m, n, nzmax)
```

**Description** 

 $S = spall\,oc(m, n, nzmax)$  creates an all zero sparse matrix S of size m-by-n with room to hold nzmax nonzeros. The matrix can then be generated column by column without requiring repeated storage allocation as the number of nonzeros grows.

```
spalloc(m, n, nzmax) is shorthand for
sparse([], [], [], m, n, nzmax)
```

**Examples** 

To generate efficiently a sparse matrix that has an average of at most three nonzero elements per column

```
 \begin{split} S &= spalloc(n, n, 3*n); \\ for &j = 1: n \\ &S(:,j) = [zeros(n-3, 1)' \ round(rand(3, 1))']'; \\ end \end{aligned}
```

Create sparse matrix

## **Syntax**

```
S = sparse(A)
```

S = sparse(i, j, s, m, n, nzmax)

S = sparse(i, j, s, m, n)

S = sparse(i, j, s)

S = sparse(m, n)

## **Description**

The sparse function generates matrices in MATLAB's sparse storage organization.

S = sparse(A) converts a full matrix to sparse form by squeezing out any zero elements. If S is already sparse, sparse(S) returns S.

S = sparse(i, j, s, m, n, nzmax) uses vectors i, j, and s to generate an m-by-n sparse matrix with space allocated for nzmax nonzeros. Any elements of s that are zero are ignored, along with the corresponding values of i and j. Vectors i, j, and s are all the same length.

To simplify this six-argument call, you can pass scalars for the argument s and one of the arguments i or j—in which case they are expanded so that i, j, and s all have the same length.

```
S = sparse(i, j, s, m, n) uses nzmax = length(s).
```

S = sparse(i, j, s) uses m = max(i) and n = max(j). The maxima are computed before any zeros in s are removed, so one of the rows of  $[i \ j \ s]$  might be  $[m \ n \ 0]$ .

S = sparse(m, n) abbreviates sparse([], [], [], m, n, 0). This generates the ultimate sparse matrix, an m-by-n all zero matrix.

#### Remarks

All of MATLAB's built-in arithmetic, logical, and indexing operations can be applied to sparse matrices, or to mixtures of sparse and full matrices. Operations on sparse matrices return sparse matrices and operations on full matrices return full matrices.

In most cases, operations on mixtures of sparse and full matrices return full matrices. The exceptions include situations where the result of a mixed operation is structurally sparse, for example, A. \*S is at least as sparse as S.

## **Examples**

S = sparse(1: n, 1: n, 1) generates a sparse representation of the n-by-n identity matrix. The same S results from S = sparse(eye(n, n)), but this would also temporarily generate a full n-by-n matrix with most of its elements equal to zero.

B = sparse(10000, 10000, pi) is probably not very useful, but is legal and works; it sets up a 10000-by-10000 matrix with only one nonzero element. Don't try full (B); it requires 800 megabytes of storage.

This dissects and then reassembles a sparse matrix:

```
[i,j,s] = find(S);
[m,n] = size(S);
S = sparse(i,j,s,m,n);
```

So does this, if the last row and column have nonzero entries:

```
[i,j,s] = find(S);

S = sparse(i,j,s);
```

#### See Also

The sparfun directory, and:

di ag Diagonal matrices and diagonals of a matrix find Find indices and values of nonzero elements

ful l Convert sparse matrix to full matrix nnz Number of nonzero matrix elements

nonzeros Nonzero matrix elements

nzmax Amount of storage allocated for nonzero matrix

elements

spones Replace nonzero sparse matrix elements with ones

sprandn Sparse normally distributed random matrix

sprandsym Sparse symmetric random matrix

spy Visualize sparsity pattern

Import matrix from sparse matrix external format

#### **Syntax**

S = spconvert(D)

## Description

spconvert is used to create sparse matrices from a simple sparse format easily produced by non-MATLAB sparse programs. spconvert is the second step in the process:

- 1 Load an ASCII data file containing [i,j,v] or [i,j,re,im] as rows into a MATLAB variable.
- **2** Convert that variable into a MATLAB sparse matrix.

S = spconvert(D) converts a matrix D with rows containing [i,j,s] or [i,j,r,s] to the corresponding sparse matrix. D must have an nnz or nnz+1 row and three or four columns. Three elements per row generate a real matrix and four elements per row generate a complex matrix. A row of the form  $[m\ n\ 0]$  or  $[m\ n\ 0\ 0]$  anywhere in D can be used to specify  $si\ ze(S)$ . If D is already sparse, no conversion is done, so spconvert can be used after D is loaded from either a MAT-file or an ASCII file.

## **Examples**

Suppose the ASCII file uphill. dat contains

```
1
     1
          1.0000000000000000
1
     2
          0.500000000000000
2
     2
          0. 333333333333333
1
     3
          0.333333333333333
2
     3
          0. 250000000000000
3
     3
          0.200000000000000
1
          0.250000000000000
2
     4
          0.200000000000000
3
     4
          0.166666666666667
4
     4
          0. 142857142857143
          0.000000000000000
```

#### Then the statements

```
load uphill.dat
H = spconvert(uphill)
```

# spconvert

recreate sparse(triu(hilb(4))), possibly with roundoff errors. In this case, the last line of the input file is not necessary because the earlier lines already specify that the matrix is at least 4-by-4.

Extract and create sparse band and diagonal matrices

## **Syntax**

[B, d] = spdi ags(A) B = spdi ags(A, d) A = spdi ags(B, d, A) A = spdi ags(B, d, m, n)

## Description

The spdi ags function generalizes the function di ag. Four different operations, distinguished by the number of input arguments, are possible:

 $[B,d] = spdi \, ags(A)$  extracts all nonzero diagonals from the m-by-n matrix A. B is a mi n(m,n)-by-p matrix whose columns are the p nonzero diagonals of A. d is a vector of length p whose integer components specify the diagonals in A.

B = spdi ags(A, d) extracts the diagonals specified by d.

 $A = spdi \, ags(B, d, A)$  replaces the diagonals specified by d with the columns of B. The output is sparse.

A = spdi ags(B, d, m, n) creates an m-by-n sparse matrix by taking the columns of B and placing them along the diagonals specified by d.

#### Remarks

If a column of B is longer than the diagonal it's replacing, spdi ags takes elements from B's tail.

## **Arguments**

The spdi ags function deals with three matrices, in various combinations, as both input and output:

- A An m-by-n matrix, usually (but not necessarily) sparse, with its nonzero or specified elements located on p diagonals.
- B A  $mi \ n(m, n)$ -by-p matrix, usually (but not necessarily) full, whose columns are the diagonals of A.
- d A vector of length  $\boldsymbol{p}$  whose integer components specify the diagonals in A.

Roughly, A, B, and d are related by

```
for k = 1: p

B(:, k) = diag(A, d(k))

end
```

Some elements of B, corresponding to positions outside of A, are not defined by these loops. They are not referenced when B is input and are set to zero when B is output.

## **Examples**

This example generates a sparse tridiagonal representation of the classic second difference operator on n points.

```
e = ones(n, 1);
A = spdiags([e -2*e e], -1:1, n, n)
```

Turn it into Wilkinson's test matrix (see gal l ery):

$$A = \text{spdiags}(abs(-(n-1)/2: (n-1)/2)', 0, A)$$

Finally, recover the three diagonals:

$$B = spdiags(A)$$

The second example is not square.

Here m = 7, n = 4, and p = 3.

The statement  $[B, d] = spdi ags(A) produces d = [-3 \ 0 \ 2]'$  and

$$B = \begin{bmatrix} 41 & 11 & 0 \\ 52 & 22 & 0 \\ 63 & 33 & 13 \\ 74 & 44 & 24 \end{bmatrix}$$

# spdiags

Conversely, with the above B and d, the expression spdi ags (B, d, 7, 4) reproduces the original A.

See Also

di ag

Diagonal matrices and diagonals of a matrix

# speak

Purpose Speak text string

Syntax speak(y)

speak(y, voi ce)

**Description** speak(y) speaks the text string y using the default voice.

speak(y, voi ce) speaks the text string y using the voice specified by voi ce.

 $\ensuremath{\mathsf{speak}}$  requires the Speech Manager and works only on the Macintosh.

**Examples** speak('I like math.')

speak('I really like matlab','good news')

**Purpose** Sparse identity matrix

**Syntax** S = speye(m, n)

S = speye(n)

**Description** S = speye(m, n) forms an m-by-n sparse matrix with 1s on the main diagonal.

S = speye(n) abbreviates speye(n, n).

**Examples** I = speye (1000) forms the sparse representation of the 1000-by-1000 identity

matrix, which requires only about 16 kilobytes of storage. This is the same final result as I = sparse(eye(1000, 1000)), but the latter requires eight mega-

bytes for temporary storage for the full representation.

See Also spall oc Allocate space for sparse matrix

spones Replace nonzero sparse matrix elements with ones spdi ags Extract and create sparse band and diagonal matrices

sprand Sparse uniformly distributed random matrix sprandn Sparse normally distributed random matrix

Apply function to nonzero sparse matrix elements

#### **Syntax**

f = spfun('function', S)

## Description

The spf un function selectively applies a function to only the *nonzero* elements of a sparse matrix, preserving the sparsity pattern of the original matrix (except for underflow).

f = spfun('function', S) evaluates function(S) on the nonzero elements of S. function must be the name of a function, usually defined in an M-file, which can accept a matrix argument, S, and evaluate the function at each element of S.

#### Remarks

Functions that operate element-by-element, like those in the elfun directory, are the most appropriate functions to use with spfun.

## **Examples**

Given the 4-by-4 sparse diagonal matrix

$$S = (1, 1) & 1 \\ (2, 2) & 2 \\ (3, 3) & 3 \\ (4, 4) & 4$$

f = spfun('exp', S) has the same sparsity pattern as S:

$$\begin{array}{lll} f &=& & \\ & (1,1) & 2.7183 \\ & (2,2) & 7.3891 \\ & (3,3) & 20.0855 \\ & (4,4) & 54.5982 \end{array}$$

full(exp(S))

whereas exp(S) has 1s where S has 0s.

```
ans =
    2.7183
               1.0000
                          1.0000
                                     1.0000
    1.0000
                          1.0000
               7. 3891
                                     1.0000
    1.0000
               1.0000
                         20.0855
                                     1.0000
    1.0000
               1.0000
                          1.0000
                                    54. 5982
```

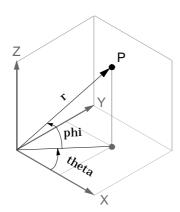
**Purpose** Transform spherical coordinates to Cartesian

**Syntax** [x, y, z] = sph2cart(THETA, PHI, R)

**Description** [x, y, z] = sph2cart (THETA, PHI, R) transforms the corresponding elements

of spherical coordinate arrays to Cartesian, or xyz, coordinates. THETA, PHI, and R must all be the same size. THETA and PHI are angular displacements in radians from the positive x-axis and from the x-y plane, respectively.

**Algorithm** The mapping from spherical coordinates to three-dimensional Cartesian coordinates is:



See Also

cart2pol Transform Cartesian coordinates to polar or cylindrical cart2sph Transform Cartesian coordinates to spherical pol 2cart Transform polar or cylindrical coordinates to Cartesian

Cubic spline interpolation

#### Syntax

```
yi = spline(x, y, xi)

pp = spline(x, y)
```

## Description

The spline function interpolates between data points using cubic spline fits.

yi = spline(x, y, xi) accepts vectors x and y that contain coarsely spaced data, and vector xi that specifies a new, more finely spaced abscissa. The function uses cubic spline interpolation to find a vector yi corresponding to xi.

pp = spline(x, y) returns the pp-form of the cubic spline interpolant, for later use with ppval and other spline functions.

## **Examples**

The two vectors

represent the census years from 1900 to 1990 and the corresponding United States population in millions of people. The expression

```
spl i ne(t, p, 2000)
```

uses the cubic spline to extrapolate and predict the population in the year 2000. The result is

```
ans = 270.6060
```

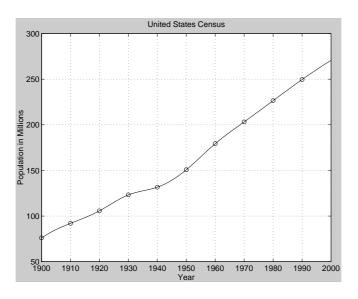
The statements

```
x = 1900: 1: 2000;

y = spline(t, p, x);

plot(t, p, 'o', x, y)
```

interpolate the data with a cubic spline, evaluate that spline for each year from 1900 to 2000, and plot the result.



## **Algorithm**

spl i ne is a MATLAB M-file. It uses the M-files ppval, mkpp, and unmkpp. These routines form a small suite of functions for working with piecewise polynomials. spl i ne uses these functions in a fairly simple fashion to perform cubic spline interpolation. For access to the more advanced features, see the M-files and the Spline Toolbox.

See Also

interp1 One-dimensional data interpolation (table lookup)
ppval Evaluate piecewise polynomial

References

[1] de Boor, C., A Practical Guide to Splines, Springer-Verlag, 1978.

## spones

**Purpose** Replace nonzero sparse matrix elements with ones

**Syntax** R = spones(S)

**Description** R = spones(S) generates a matrix R with the same sparsity structure as S, but

with 1's in the nonzero positions.

**Examples** c = sum(spones(S)) is the number of nonzeros in each column.

r = sum(spones(S'))' is the number of nonzeros in each row.

sum(c) and sum(r) are equal, and are equal to nnz(S).

**See Also** nnz Number of nonzero matrix elements

spall oc Allocate space for sparse matrix

spfun Apply function to nonzero sparse matrix elements

Set parameters for sparse matrix routines

## **Syntax**

```
spparms('key', value)
spparms
values = spparms
[keys, values] = spparms
spparms(values)
value = spparms('key')
spparms('default')
spparms('tight')
```

'spumoni'

## Description

spparms(' key', val ue) sets one or more of the *tunable* parameters used in the sparse linear equation operators,  $\setminus$  and /, and the minimum degree orderings, col mmd and symmmd. In ordinary use, you should never need to deal with this function.

The meanings of the key parameters are

Sparse Monitor flag.

<b>Зришотт</b>	0 produces no diagnostic output, the default. 1 produces information about choice of algorithm based on matrix structure, and about storage allocation. 2 also produces very detailed information about the minimum degree algorithms.
'thr_rel', 'thr_abs'	$\label{lem:mindegree} \mbox{Minimum degree threshold is $thr\_rel*mindegree+thr\_abs.}$
' exact_d'	Nonzero to use exact degrees in minimum degree. Zero to use approximate degrees.
'supernd'	If positive, minimum degree amalgamates the supernodes every supernd stages.
'rreduce'	If positive, minimum degree does row reduction every ${\tt rreduce}$ stages.
'wh_frac'	Rows with densi ty > wh_frac are ignored in col mmd.

' aut ommd' Nonzero to use minimum degree orderings with  $\setminus$  and  $\wedge$ .

'aug\_rel', Residual scaling parameter for augmented equations is 'aug\_abs' aug\_rel\*max(max(abs(A))) + aug\_abs.

For example, aug\_rel = 0, aug\_abs = 1 puts an unscaled identity matrix in the (1,1) block of the augmented matrix.

spparms, by itself, prints a description of the current settings.

values = spparms returns a vector whose components give the current settings.

[keys, values] = spparms returns that vector, and also returns a character matrix whose rows are the keywords for the parameters.

spparms(values), with no output argument, sets all the parameters to the values specified by the argument vector.

value = spparms(' key') returns the current setting of one parameter.

spparms('default') sets all the parameters to their default settings.

spparms('tight') sets the minimum degree ordering parameters to their *tight* settings, which can lead to orderings with less fill-in, but which make the ordering functions themselves use more execution time.

The key parameters for default and tight settings are

	Keyword	Default	Tight
values(1)	'spumoni'	0.0	
values(2)	'thr_rel'	1.1	1.0
values(3)	'thr_abs'	1.0	0.0
values(4)	' exact_d'	0.0	1.0
values(5)	'supernd'	3.0	1.0
values(6)	'rreduce'	3.0	1.0
values(7)	'wh_frac'	0.5	0.5
values(8)	'autommd'	1.0	
values(9)	'aug_rel'	0.001	
values(10)	'aug_abs'	0.0	

## See Also

\	Matrix left division (backslash)
col mmd	Sparse column minimum degree permutation
symmmd	Sparse symmetric minimum degree ordering

## References

[1] Gilbert, John R., Cleve Moler and Robert Schreiber, "Sparse Matrices in MATLAB: Design and Implementation," *SIAM Journal on Matrix Analysis and Applications* 13, 1992, pp. 333-356.

# sprand

**Purpose** Sparse uniformly distributed random matrix

**Syntax** R = sprand(S)

R = sprand(m, n, densi ty)
R = sprand(m, n, densi ty, rc)

**Description** R = sprand(S) has the same sparsity structure as S, but uniformly distrib-

uted random entries.

 $R = sprand(m, n, densi\ ty)$  is a random, m-by-n, sparse matrix with approxi-

mately densi ty\*m\*n uniformly distributed nonzero entries

 $(0 \le \text{density} \le 1)$ .

 $R = sprand(m, n, densi\ ty, rc)$  also has reciprocal condition number approximately equal to rc. R is constructed from a sum of matrices of rank one.

If rc is a vector of length l r, where l r  $\leq$  mi n(m, n), then R has rc as its first l r singular values, all others are zero. In this case, R is generated by random plane rotations applied to a diagonal matrix with the given singular values. It has a great deal of topological and algebraic structure.

See Also sprandn Sparse normally distributed random matrix

sprandsym Sparse symmetric random matrix

**Purpose** Sparse normally distributed random matrix

**Syntax**  $R = \operatorname{sprandn}(S)$ 

R = sprandn(m, n, density)
R = sprandn(m, n, density, rc)

**Description** R = sprandn(S) has the same sparsity structure as S, but normally distrib-

uted random entries with mean 0 and variance 1.

R = sprandn(m, n, density) is a random, m-by-n, sparse matrix with approximately density\*m\*n normally distributed nonzero entries  $(0 \le density \le 1)$ .

R = sprandn(m, n, density, rc) also has reciprocal condition number approximately equal to rc. R is constructed from a sum of matrices of rank one.

If rc is a vector of length l r, where l r  $\leq$  mi n(m, n), then R has rc as its first l r singular values, all others are zero. In this case, R is generated by random plane rotations applied to a diagonal matrix with the given singular values. It has a great deal of topological and algebraic structure.

**See Also** Sparse uniformly distributed random matrix

sprandn Sparse normally distributed random matrix

# sprandsym

## **Purpose**

Sparse symmetric random matrix

## **Syntax**

R = sprandsym(S)

R = sprandsym(n, density)

R = sprandsym(n, density, rc)

R = sprandsym(n, density, rc, kind)

## Description

R = sprandsym(S) returns a symmetric random matrix whose lower triangle and diagonal have the same structure as S. Its elements are normally distributed, with mean 0 and variance 1.

R = sprandsym(n, density) returns a symmetric random, n-by-n, sparse matrix with approximately density\*n\*n nonzeros; each entry is the sum of one or more normally distributed random samples, and  $(0 \le density \le 1)$ .

R = sprandsym(n, density, rc) returns a matrix with a reciprocal condition number equal to rc. The distribution of entries is nonuniform; it is roughly symmetric about 0; all are in [-1, 1].

If rc is a vector of length n, then R has eigenvalues rc. Thus, if rc is a positive (nonnegative) vector then R is a positive definite matrix. In either case, R is generated by random Jacobi rotations applied to a diagonal matrix with the given eigenvalues or condition number. It has a great deal of topological and algebraic structure.

R = sprandsym(n, density, rc, kind) returns a positive definite matrix. Argument kind can be:

- 1 to generate R by random Jacobi rotation of a positive definite diagonal matrix. R has the desired condition number exactly.
- 2 to generate an R that is a shifted sum of outer products. R has the desired condition number only approximately, but has less structure.
- 3 to generate an R that has the same structure as the matrix S and approximate condition number 1/rc. density is ignored.

#### See Also

sprand sprandn Sparse uniformly distributed random matrix Sparse normally distributed random matrix

Write formatted data to a string

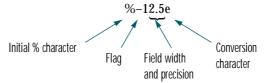
Syntax

```
s = sprintf(format, A, ...)
[s, errrmsg] = sprintf(format, A, ...)
```

Description

s = sprintf(format, A, ...) formats the data in matrix A (and in any additional matrix arguments) under control of the specified format string, and returns it in the MATLAB string variable s. sprintf is the same as fprintf except that it returns the data in a MATLAB string variable rather than writing it to a file.

The *format* string specifies notation, alignment, significant digits, field width, and other aspects of output format. It can contain ordinary alphanumeric characters; along with escape characters, conversion specifiers, and other characters, organized as shown below:



For more information see "Tables" and "References."

[s, errmsg] = sprintf(format, A, ...) returns an error message string errmsg if an error occurred or an empty matrix if an error did not occur.

# sprintf

#### Remarks

The sprintf function behaves like its ANSI C language sprintf() namesake with certain exceptions and extensions. These include:

- 1 The following nonstandard subtype specifiers are supported for conversion specifiers ‰, ‰u, ‰x, and ‰X.
  - t The underlying C data type is a float rather than an unsigned integer.
  - b The underlying C data type is a double rather than an unsigned integer.

For example, to print a double-precision value in hexadecimal, use a format like  $\mbox{''}bx'$ .

2 sprintf is *vectorized* for the case when input matrix A is nonscalar. The format string is cycled through the elements of A (columnwise) until all the elements are used up. It is then cycled in a similar manner, without reinitializing, through any additional matrix arguments.

### **Tables**

The following tables describe the nonalphanumeric characters found in format specification strings.

## **Escape Characters**

Character	Description
\n	New line
\t	Horizontal tab
\b	Backspace
\r	Carriage return
\f	Form feed
\\	Backslash
\" or "	Single quotation mark
%%	Percent character

Conversion characters specify the notation of the output.

# **Conversion Specifiers**

Specifier	Description
%c	Single character
%d	Decimal notation (signed)
%e	Exponential notation (using a lowercase e as in 3. 1415e+00)
%E	Exponential notation (using an uppercase E as in 3. 1415E+00)
%f	Fixed-point notation
%g	The more compact of %e or %f, as defined in [2]. Insignificant zeros do not print.
%G	Same as %g, but using an uppercase E
%o	Octal notation (unsigned)
%s	String of characters
%u	Decimal notation (unsigned)
% <b>x</b>	Hexadecimal notation (using lowercase letters a-f)
%X	Hexadecimal notation (using uppercase letters A–F)

Other characters can be inserted into the conversion specifier between the % and the conversion character.

## **Other Characters**

Character	Description	Example
A minus sign (–)	Left-justifies the converted argument in its field.	%–5. 2d
A plus sign (+)	Always prints a sign character (+ or −).	%+5. 2d
Zero (0)	Pad with zeros rather than spaces.	%05. 2d
Digits (field width)	A digit string specifying the minimum number of digits to be printed.	%6f
Digits (precision)	A digit string including a period (.) specifying the number of digits to be printed to the right of the decimal point.	%6. 2f

## **Examples**

Command	Result
$sprintf('\%0.5g',(1{+}sqrt(5))/2)$	1. 618
sprintf('%0.5g',1/eps)	4. 5036e+15
sprintf('%15.5f',1/eps)	4503599627370496. 00000
<pre>sprintf('%d', round(pi))</pre>	3
sprintf('%s','hello')	hello
sprintf('The array is %dx%d.',2,3)	The array is 2x3
sprintf('\n')	Line termination character on all platforms

## See Also

int2str, num2str,sscanf

### References

[1] Kernighan, B.W. and D.M. Ritchie, *The C Programming Language*, Second Edition, Prentice-Hall, Inc., 1988.

[2] ANSI specification X3.159-1989: "Programming Language C," ANSI, 1430 Broadway, New York, NY 10018.

**Purpose** Visualize sparsity pattern

Syntax spy(S)

spy(S, markersize)
spy(S, 'LineSpec')

spy(S, 'LineSpec', markersize)

**Description** spy(S) plots the sparsity pattern of any matrix S.

spy(S, marksize), where markersize is an integer, plots the sparsity pattern using markers of the specified point size.

 $\operatorname{spy}(S, '\operatorname{LineSpec}')$ , where  $\operatorname{LineSpec}$  is a string, uses the specified plot marker type and color.

 $spy(S, '\it{Li\,neSpec}', markersi\,ze)$  uses the specified type, color, and size for the plot markers.

S is usually a sparse matrix, but full matrices are acceptable, in which case the locations of the nonzero elements are plotted.

spy replaces format +, which takes much more space to display essentially the same information.

**See Also** The gpl ot and Li neSpec reference entries in the *MATLAB Graphics Guide*,

and:

find Find indices and values of nonzero elements symmmd Sparse symmetric minimum degree ordering symrom Sparse reverse Cuthill-McKee ordering

# sqrt

**Purpose** Square root

Syntax B = sqrt(A)

**Description**  $B = \operatorname{sqrt}(A)$  returns the square root of each element of the array X. For the

elements of X that are negative or complex, sqrt(X) produces complex results.

**Remarks** See sqrtm for the matrix square root.

**Examples** sqrt((-2: 2)')

ans =

0 + 1. 4142i 0 + 1. 0000i

0

1. 0000 1. 4142

See Also sqrtm

Matrix square root

Matrix square root

**Syntax** 

**Description** 

Y = sqrtm(X) is the matrix square root of X. Complex results are produced if X has negative eigenvalues. A warning message is printed if the computed Y\*Y is not close to X.

[Y, esterr] = sqrtm(X) does not print any warning message, but returns an estimate of the relative residual, norm(Y\*Y-X) / norm(X).

Remarks

If X is real, symmetric and positive definite, or complex, Hermitian and positive definite, then so is the computed matrix square root.

Some matrices, like  $X = [0 \ 1; \ 0 \ 0]$ , do not have any square roots, real or complex, and sqrtm cannot be expected to produce one.

**Examples** 

A matrix representation of the fourth difference operator is

This matrix is symmetric and positive definite. Its unique positive definite square root, Y = sqrtm(X), is a representation of the second difference operator.

# sqrtm

The matrix

$$X = 7 \quad 10 \\ 15 \quad 22$$

has four square roots. Two of them are

and

$$Y2 = 1 2 3 4$$

The other two are -Y1 and -Y2. All four can be obtained from the eigenvalues and vectors of X.

$$[V, D] = eig(X);$$

$$D = 0.1386 0$$

$$0 28.8614$$

The four square roots of the diagonal matrix  $\ensuremath{\mathtt{D}}$  result from the four choices of sign in

$$S = \pm 0.3723$$
 0 0  $\pm 5.3723$ 

All four Ys are of the form

$$Y = V*S/V$$

The sqrtm function chooses the two plus signs and produces Y1, even though Y2 is more natural because its entries are integers.

Finally, the matrix

$$X = 0 \quad 1 \quad 0 \quad 0$$

does not have any square roots. There is no matrix Y, real or complex, for which Y\*Y = X. The statement

```
Y = sqrtm(X)
```

produces several warning messages concerning accuracy and the answer

## **Algorithm**

The function  $\operatorname{sqrtm}(X)$  is an abbreviation for  $\operatorname{funm}(X, '\operatorname{sqrt}')$ . The algorithm used by  $\operatorname{funm}$  is based on a Schur decomposition. It can fail in certain situations where X has repeated eigenvalues. See  $\operatorname{funm}$  for details.

## See Also

expm	Matrix exponentiai
funm	Evaluate functions of a matrix
logm	Matrix logarithm

# squeeze

**Purpose** 

Remove singleton dimensions

**Syntax** 

B = squeeze(A)

**Description** 

 $B={\rm squeeze}(A)\;$  returns an array B with the same elements as A, but with all singleton dimensions removed. A singleton dimension is any dimension for which

size(A, dim) = 1.

**Examples** 

Consider the 2-by-1-by-3 array Y = rand(2, 1, 3). This array has a singleton column dimension — that is, there's only one column per page.

Y =

$$Y(:,:,1) = Y(:,:,2) = 0.5194 0.0346 0.8310 0.0535$$

The command Z = squeeze(Y) yields a 2-by-3 matrix:

See Also

reshape Reshape array shiftdim Shift dimensions

Read string under format control

### Syntax

```
A = sscanf(s, format)
A = sscanf(s, format, size)
[A, count, errmsg, nextindex] = sscanf(...)
```

### Description

A = sscanf(s, format) reads data from the MATLAB string variable s, converts it according to the specified format string, and returns it in matrix A. format is a string specifying the format of the data to be read. See "Remarks" for details. sscanf is the same as fscanf except that it reads the data from a MATLAB string variable rather than reading it from a file.

A = sscanf(s, *format*, si ze) reads the amount of data specified by si ze and converts it according to the specified *format* string. si ze is an argument that determines how much data is read. Valid options are:

n Read n elements into a column vector.

inf Read to the end of the file, resulting in a column vector containing the same number of elements as are in the file.

[m, n] Read enough elements to fill an m-by-n matrix, filling the matrix in column order. n can be Inf, but not m.

If the matrix A results from using character conversions only and  $si\ ze$  is not of the form [M, N], a row vector is returned.

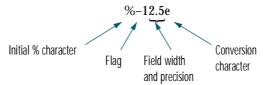
sscanf differs from its C language namesakes scanf() and fscanf() in an important respect — it is *vectorized* in order to return a matrix argument. The *format* string is cycled through the file until an end-of-file is reached or the amount of data specified by size is read in.

[A, count, errmsg, nextindex] = sscanf(...) reads data from MATLAB string variable s, converts it according to the specified *format* string, and returns it in matrix A. count is an optional output argument that returns the number of elements successfully read. errmsg is an optional output argument that returns an error message string if an error occurred or an empty matrix if an error did not occur. nextindex is an optional output argument specifying one more than the number of characters scanned in s.

#### Remarks

When MATLAB reads a specified file, it attempts to match the data in the file to the format string. If a match occurs, the data is written into the matrix in column order. If a partial match occurs, only the matching data is written to the matrix, and the read operation stops.

The *format* string consists of ordinary characters and/or conversion specifications. Conversion specifications indicate the type of data to be matched and involve the character %, optional width fields, and conversion characters, organized as shown below:



Add one or more of these characters between the % and the conversion character:

An asterisk (\*) Skip over the matched value, if the value is matched but

not stored in the output matrix.

A digit string Maximum field width.

A letter The size of the receiving object; for example, h for short as

in %hd for a short integer, or 1 for long as in %l d for a long

integer or %l g for a double floating-point number.

Valid conversion characters are:

%c Sequence of characters; number specified by field width

%d Decimal numbers

%e, %f, %g Floating-point numbers

%i Signed integer

%0 Signed octal integer

%s A series of non-whitespace characters

%u Signed decimal integer

%x Signed hexadecimal integer

[...] Sequence of characters (scanlist)

If %s is used, an element read may use several MATLAB matrix elements, each holding one character. Use %c to read space characters; the format %s skips all white space.

Mixing character and numeric conversion specifications cause the resulting matrix to be numeric and any characters read to appear as their ASCII values, one character per MATLAB matrix element.

For more information about format strings, refer to the scanf() and fscanf() routines in a C language reference manual.

## Examples

The statements

```
s = '2.7183 \ 3.1416';

A = sscanf(s, '%f')
```

create a two-element vector containing poor approximations to e and pi.

#### See Also

eval Interpret strings containing MATLAB expressions sprintf Write formatted data to a string

# startup

**Purpose** MATLAB startup M-file

Syntax startup

**Description** At startup time, MATLAB automatically executes the master M-file

matlabrc. m and, if it exists, startup. m. On multiuser or networked systems, matlabrc. m is reserved for use by the system manager. The file matlabrc. m

invokes the file startup. m if it exists on MATLAB's search path.

You can create a startup file in your own MATLAB directory. The file can include physical constants, handle graphics defaults, engineering conversion

factors, or anything else you want predefined in your workspace.

Algorithm Only matlabrc. m is actually invoked by MATLAB at startup. However,

matlabrc. m contains the statements

if exist('startup') == 2
 startup
end

that invoke  $startup.\ m.$  You can extend this process to create additional startup M-files, if required.

Willes, ii required

See Also
! Operating system command
exist Check if a variable or file exists

matlabre MATLAB startup M-file

path Control MATLAB's directory search path

qui t Terminate MATLAB

Standard deviation

**Syntax** 

$$s = std(X)$$

$$s = std(X, flag)$$

$$s = std(X, flag, dim)$$

**Definition** 

There are two common textbook definitions for the standard deviation  ${\bf s}$  of a data vector  ${\bf X}$ :

(1) 
$$s = \left(\frac{1}{n-1}\sum_{i=1}^{n}(x_i-\bar{x})^2\right)^{\frac{1}{2}}$$
 and (2)  $s = \left(\frac{1}{n}\sum_{i=1}^{n}(x_i-\bar{x})^2\right)^{\frac{1}{2}}$ 

where

$$\bar{x} = \frac{1}{n} \sum_{i=1}^{n} x_i$$

and n is the number of elements in the sample. The two forms of the equation differ only in n-1 versus n in the divisor.

Description

s = std(X), where X is a vector, returns the standard deviation using (1) above. If X is a random sample of data from a normal distribution,  $s^2$  is the best *unbiased* estimate of its variance.

If X is a matrix, std(X) returns a row vector containing the standard deviation of the elements of each column of X. If X is a multidimensional array, std(X) is the standard deviation of th elements along the first nonsingleton dimension of X.

s = std(X, flag) for flag = 0, is the same as std(X). For flag = 1, std(X, 1) returns the standard deviation using (2) above, producing the second moment of the sample about its mean.

s = std(X, flag, dim) computes the standard deviations along the dimension of X specified by scalar dim.

# **Examples**

For matrix X

$$X = \begin{bmatrix} 1 & 5 & 9 \\ 7 & 15 & 22 \end{bmatrix}$$

$$S = std(X, 0, 1)$$

$$S = \begin{bmatrix} 4.2426 & 7.0711 & 9.1924 \end{bmatrix}$$

$$S = std(X, 0, 2)$$

$$S = \begin{bmatrix} 4.000 \\ 7.5056 \end{bmatrix}$$

See Also

corrcoef, cov, mean, medi an

String to number conversion

Syntax

x = str2num('str')

Description

x = str2num('str') converts the string str, which is an ASCII character representation of a numeric value, to MATLAB's numeric representation. The string can contain:

- Digits
- · A decimal point
- A leading + or sign
- A letter e preceding a power of 10 scale factor
- A letter i indicating a complex or imaginary number.

The str2num function can also convert string matrices.

## **Examples**

str2num(' 3. 14159e0') is approximately  $\pi$ .

To convert a string matrix:

```
str2num(['1 2';'3 4'])
ans =

1 2
3 4
```

#### See Also

[] (special characters) Build arrays

; (special characters) End array rows; suppress printing; separate state-

ments.

hex2num Hexadecimal to double number conversion

num2str Number to string conversion

sparse Create sparse matrix

sscanf Read string under format control

String concatenation

### Syntax

t = strcat(s1, s2, s3, ...)

## **Description**

t = strcat(s1, s2, s3, ...) horizontally concatenates corresponding rows of the character arrays s1, s2, s3, etc. The trailing padding is ignored. All the inputs must have the same number of rows (or any can be a single string). When the inputs are all character arrays, the output is also a character array.

When any of the inputs is a cell array of strings, strcat returns a cell array of strings formed by concatenating corresponding elements of s1,s2, etc. The inputs must all have the same size (or any can be a scalar). Any of the inputs can also be a character array.

## **Examples**

Given two 1-by-2 cell arrays a and b,

```
a = b = 
'abcde' 'fghi' 'jkl' 'mm'
```

the command t = strcat(a, b) yields:

```
t =
'abcdej kl' 'fghi mn'
```

Given the 1-by-1 cell array  $c = \{ (Q) \}$ , the command t = strcat(a, b, c) yields:

```
t =  'abcdej kl Q' 'fghi mnQ'
```

## Remarks

strcat and matrix operation are different for strings that contain trailing spaces:

```
a = 'hello'
b = 'goodby'
strcat(a, b)
ans =
hellogoodby
[a b]
ans =
hello goodby
```

See Also cat Concatenate arrays

cellstr Create cell array of strings from character array

strvcat Vertical concatenation of strings

# strcmp

**Purpose** Compare strings

**Syntax** k = strcmp('str1', 'str2')

TF = strcmp(S, T)

**Description** k = strcmp('str1', 'str2') compares the strings str1 and str2 and returns

logical true (1) if the two are identical, and logical false (0) otherwise.

TF = strcmp(S, T) where either S or T is a cell array of strings, returns an array TF the same size as S and T containing 1 for those elements of S and T that match, and 0 otherwise. S and T must be the same size (or one can be a scalar cell). Either one can also be a character array with the right number of rows.

**Remarks** Note that the value returned by strcmp is not the same as the C language

convention. In addition, the strcmp function is case sensitive; any leading and trailing blanks in either of the strings are explicitly included in the comparison.

## **Examples**

```
strcmp('Yes','No') =
strcmp('Yes','Yes') =
A =
    ' MATLAB'
                           'SIMULINK'
    'Tool boxes'
                           'The MathWorks'
B =
    'Handle Graphics'
                           'Real Time Workshop'
    'Tool boxes'
                           'The MathWorks'
C =
    'Signal Processing'
                             'Image Processing'
    ' MATLAB'
                              'SIMULINK'
strcmp(A, B)
ans =
     0
           0
     1
            1
strcmp(A, C)
ans =
     0
           0
     0
            0
```

### See Also

findstr Find one string within another strncmp Compare the first n characters of two strings strmatch Find possible matches for a string

# strings

Purpose MATLAB string handling

**Syntax** S = 'Any Characters'

S = string(X)
X = numeric(S)

Description

 $S = 'Any\ Characters'$  is a vector whose components are the numeric codes for the characters (the first 127 codes are ASCII). The actual characters displayed depend on the character set encoding for a given font. The length of S is the number of characters. A quote within the string is indicated by two quotes.

S = string(X) can be used to convert an array that contains positive integers representing numeric codes into a MATLAB character array.

X = doubl e(S) converts the string to its equivalent numeric codes.

isstr(S) tells if S is a string variable.

Use the strcat function for concatenating cell arrays of strings, for arrays of multiple strings, and for padded character arrays. For concatenating two single strings, it is more efficient to use square brackets, as shown in the example, than to use strcat.

**Example** 

$$s = ['It is 1 o''clock', 7]$$

See Also

char Create character array (string) strcat String concatenation

# strjust

**Purpose** Justify a character array

Syntax strjust(S)

**Description** strj ust (S) returns a right-justified version of the character array S.

**See Also** debl ank Strip trailing blanks from the end of a string

## strmatch

**Purpose** Find possible matches for a string

**Syntax** i = strmatch('str', STRS)

i = strmatch('str', STRS, 'exact')

**Description** i = strmatch('str', STRS) looks through the rows of the character array or

cell array of strings STRS to find strings that begin with string str, returning the matching row indices. strmatch is fastest when STRS is a character array.

i = strmatch('str', STRS, 'exact') returns only the indices of the strings in

STRS matching *str* exactly.

**Examples** The statement

i = strmatch('max', strvcat('max', 'minimax', 'maximum'))

returns i = [1; 3] since rows 1 and 3 begin with 'max'. The statement

i = strmatch('max', strvcat('max', 'mi ni max', 'maxi mum'), 'exact')

returns i = 1, since only row 1 matches 'max' exactly.

**See Also** findstr Find one string within another

strcmp Compare strings

strncmp Compare the first n characters of two strings

strvcat Vertical concatenation of strings

**Purpose** Compare the first n characters of two strings

**Syntax** k = strncmp('str1', 'str2', n)

TF = strncmp(S, T, n)

**Description** k = strncmp('str1', 'str2', n) returns logical true (1) if the first n charac-

ters of the strings str1 and str2 are the same, and returns logical false (0) otherwise. Arguments str1 and str2 may also be cell arrays of strings.

TF = strncmp(S, T, N) where either S or T is a cell array of strings, returns an array TF the same size as S and T containing 1 for those elements of S and T that match (up to n characters), and 0 otherwise. S and T must be the same size (or one can be a scalar cell). Either one can also be a character array with the right

number of rows.

**Remarks** The command strncmp is case sensitive. Any leading and trailing blanks in

either of the strings are explicitly included in the comparison.

**See Also** findstr Find one string within another

strcmp Compare strings

strmatch Find possible matches for a string

# strrep

**Purpose** 

String search and replace

Syntax

str = strrep(str1, str2, str3)

**Description** 

str = strrep(str1, str2, str3) replaces all occurrences of the string str2 within string str1 with the string str3.

strrep(str1, str2, str3), when any of str1, str2, or str3 is a cell array of strings, returns a cell array the same size as str1, str2 and str3 obtained by performing a strrep using corresponding elements of the inputs. The inputs must all be the same size (or any can be a scalar cell). Any one of the strings can also be a character array with the right number of rows.

## **Examples**

```
s1 = 'This is a good example.';
str = strrep(s1, 'good', 'great')
str =
This is a great example.
A =
    ' MATLAB'
                           'SIMULINK'
    'Tool boxes'
                           'The MathWorks'
B =
    'Handle Graphics'
                           'Real Time Workshop'
    'Tool boxes'
                            'The MathWorks'
C =
    'Signal Processing'
                              'Image Processing'
    ' MATLAB'
                              'SIMULINK'
strrep(A, B, C)
ans =
    ' MATLAB'
                  'SIMULINK'
    ' MATLAB'
                  'SIMULINK'
```

See Also

findstr

Find one string within another

## **Purpose** First token in string

#### **Syntax**

```
token = strtok('str', delimiter)
token = strtok('str')
[token, rem] = strtok(...)
```

### Description

token = strtok('str', delimiter) returns the first token in the text string str, that is, the first set of characters before a delimiter is encountered. The vector delimiter contains valid delimiter characters.

token = strtok('str') uses the default delimiters, the white space characters. These include tabs (ASCII 9), carriage returns (ASCII 13), and spaces (ASCII 32).

[token, rem] = strtok(...) returns the remainder rem of the original string. The remainder consists of all characters from the first delimiter on.

## **Examples**

```
s = 'This is a good example.';
[token, rem] = strtok(s)
token =
This
rem =
  is a good example.
```

#### See Also

findstr Find one string within another strmatch Find possible matches for a string

Create structure array

#### **Syntax**

```
s = struct('field1', values1, 'field2', values2,...)
```

## **Description**

 $s = struct('field1', values1, 'field2', values2, \dots)$  creates a structure array with the specified fields and values. The value arrays values1, values2, etc. must be cell arrays of the same size or scalar cells. Corresponding elements of the value arrays are placed into corresponding structure array elements. The size of the resulting structure is the same size as the value cell arrays or 1-by-1 if none of the values is a cell.

## **Examples**

The command

```
s = struct('type', \{'big', 'little'\}, 'color', \{'red'\}, 'x', \{34\})
```

produces a structure array s:

```
s =
1x2 struct array with fields:
    type
    color
    x
```

The value arrays have been distributed among the fields of s:

```
s(1)
ans =
          type: 'big'
          color: 'red'
          x: 3
s(2)
ans =
          type: 'little'
          color: 'red'
          x: 4
```

#### See Also

field names of a structure getfield Get field of structure array rmfield Remove structure fields setfield Set field of structure array

**Purpose** Structure to cell array conversion

**Description** c = struct2cell(s) converts the m-by-n structure s (with p fields) into a

p-by-m-by-n cell array c.

If structure s is multidimensional, cell array c has size  $[p \ size(s)]$ .

### **Examples** The commands

```
clear s, s. category = 'tree';
s. height = 37. 4; s. name = 'birch';
```

### create the structure

```
s =
category: 'tree'
height: 37.4000
name: 'birch'
```

## Converting the structure to a cell array,

```
c = struct2cell(s)
c =
    'tree'
    [37.4000]
    'birch'
```

### See Also

cell2struct, fields

**Purpose** Vertical concatenation of strings

**Syntax** S = strvcat(t1, t2, t3, ...)

**Description** S = strvcat(t1, t2, t3, ...) forms the character array S containing the text

strings (or string matrices) t1, t2, t3, ... as rows. Spaces are appended to each string as necessary to form a valid matrix. Empty arguments are ignored.

Remarks If each text parameter, ti, is itself a character array, strycat appends them

vertically to create arbitrarily large string matrices.

**Examples** The command strvcat('Hello','Yes') is the same as ['Hello';'Yes'],

except that strvcat performs the padding automatically.

t1 = 'first'; t2 = 'string'; t3 = 'matrix'; t4 = 'second';

S1 = strvcat(t1, t2, t3)S2 = strvcat(t4, t2, t3)

S1 =S2 =

first second string string matri x matrix

S3 = strvcat(S1, S2)

S3 =first string matrix second string matrix

See Also cat Concatenate arrays

> Integer to string conversion int2str Convert a matrix into a string mat2str Number to string conversion num2str Convert numeric values to string string

Single index from subscripts

**Syntax** 

IND = sub2i nd(siz, I, J)

IND = sub2i nd(siz, I1, I2, ..., In)

Description

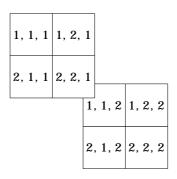
The  $\,\mathrm{sub2i}\,\mathrm{nd}$  command determines the equivalent single index corresponding to a set of subscript values.

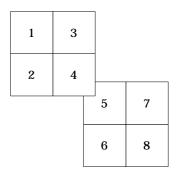
IND = sub2i nd(siz, I, J) returns the linear index equivalent to the row and column subscripts in the arrays I and J for an matrix of size siz.

IND = sub2i nd(siz, I1, I2, ..., In) returns the linear index equivalent to the n subscripts in the arrays I1, I2, ..., In for an array of size siz.

**Examples** 

The mapping from subscripts to linear index equivalents for a 2-by-2-by-2 array is:





See Also

i nd2sub fi nd Subscripts from linear index
Find indices and values of nonzero elements

# subsasgn

**Purpose** 

Overloaded method for A(i) = B,  $A\{i\} = B$ , and A. fi el d = B

**Syntax** 

A = subsasgn(A, S, B)

**Description** 

A = subsasgn(A, S, B) is called for the syntax A(i) = B,  $A\{i\} = B$ , or A. i = B when A is an object. S is a structure array with the fields:

- type: A string containing '()', '{}', or'.', where '()' specifies integer subscripts; '{}' specifies cell array subscripts, and '.' specifies subscripted structure fields.
- subs: A cell array or string containing the actual subscripts.

**Examples** 

The syntax A(1:2,:) = B calls A = subsasgn(A, S, B) where S is a 1-by-1 structure with S. type='()' and S. subs =  $\{1:2, ':'\}$ . A colon used as a subscript is passed as the string ':'.

The syntax  $A\{1: 2\} = B \text{ calls } A = \text{subsasgn}(A, S, B) \text{ where } S. \text{ type='}\{\}'$ .

The syntax A. field=B calls subsasgn(A, S, B) where S. type='.' and S. subs=' field'.

These simple calls are combined in a straightforward way for more complicated subscripting expressions. In such cases  $l \, \text{ength}(S)$  is the number of subscripting levels. For instance, A(1,2).  $name(3:5) = B \, calls$  A = subsasgn(A, S, B) where S is 3-by-1 structure array with the following values:

See Also

subsref Overloaded method for A(i),  $A\{i\}$  and A. field See Using MATLAB for more information about overloaded methods and subsasgn.

# subsindex

**Purpose** Overloaded method for X(A)

**Syntax** i = subsindex(A)

**Description** i = subsindex(A) is called for the syntax ' X(A)' when A is an object.

subsi ndex must return the value of the object as a zero-based integer index (i must contain integer values in the range 0 to  $prod(si\ ze(X))-1$ ). subsi ndex is called by the default subsref and subsasgn functions, and you can call it if you

overload these functions.

**See Also** Subsasgn Overloaded method for A(i) = B,  $A\{i\} = B$ , and A. A = A = B

subsref Overloaded method for A(i),  $A\{i\}$  and A. field

## subsref

**Purpose** 

Overloaded method for A(I),  $A\{I\}$  and A. field

**Syntax** 

B = subsref(A, S)

**Description** 

B = subsref(A, S) is called for the syntax A(i),  $A\{i\}$ , or A. i when A is an object. S is a structure array with the fields:

- type: A string containing ' () ' , ' {}' , or ' . ' , where ' () ' specifies integer subscripts; ' {}' specifies cell array subscripts, and ' . ' specifies subscripted structure fields.
- subs: A cell array or string containing the actual subscripts.

**Examples** 

The syntax A(1:2,:) calls subsref(A, S) where S is a 1-by-1 structure with S. type='()' and S. subs =  $\{1:2, ':'\}$ . A colon used as a subscript is passed as the string ':'.

The syntax A{1: 2} calls subsref(A, S) where S. type='{}'.

The syntax A. field calls subsref(A, S) where S. type='.' and S. subs='field'.

These simple calls are combined in a straightforward way for more complicated subscripting expressions. In such cases  $l \, ength(S)$  is the number of subscripting levels. For instance, A(1,2). name(3:5) calls subsref(A, S) where S is 3-by-1 structure array with the following values:

See Also

subsasgn Overloaded method for A(i) = B,  $A\{i\} = B$ , and A,  $fi \ el \ d = B$ 

See  $\mathit{Using\ MATLAB}$  for more information about overloaded methods and subsref.

Angle between two subspaces

Syntax

theta = subspace(A, B)

**Description** 

theta = subspace(A, B) finds the angle between two subspaces specified by the columns of A and B. If A and B are column vectors of unit length, this is the same as acos(A'\*B).

Remarks

If the angle between the two subspaces is small, the two spaces are nearly linearly dependent. In a physical experiment described by some observations A, and a second realization of the experiment described by B, subspace(A, B) gives a measure of the amount of new information afforded by the second experiment not associated with statistical errors of fluctuations.

**Examples** 

Consider two subspaces of a Hadamard matrix, whose columns are orthogonal.

```
H = hadamard(8);
A = H(:, 2:4);
B = H(:, 5:8);
```

Note that matrices A and B are different sizes— A has three columns and B four. It is not necessary that two subspaces be the same size in order to find the angle between them. Geometrically, this is the angle between two hyperplanes embedded in a higher dimensional space.

```
theta = subspace(A, B)
theta =
   1.5708
```

That A and B are orthogonal is shown by the fact that theta is equal to  $\pi/2$ .

```
theta – pi/2 ans = 0
```

Sum of array elements

**Syntax** 

$$B = sum(A)$$
  
 $B = sum(A, dim)$ 

**Description** 

B = sum(A) returns sums along different dimensions of an array.

If A is a vector, sum(A) returns the sum of the elements.

If A is a matrix, sum(A) treats the columns of A as vectors, returning a row vector of the sums of each column.

If A is a multidimensional array, sum(A) treats the values along the first non-singleton dimension as vectors, returning an array of row vectors.

B = sum(A, dim) sums along the dimension of A specified by scalar dim.

**Remarks** 

sum(diag(X)) is the trace of X.

**Examples** 

The magic square of order 3 is

$$\begin{aligned} M &= magi \, c \, (3) \\ M &= & & & \\ & 8 & 1 & 6 \\ & 3 & 5 & 7 \\ & 4 & 9 & 2 \end{aligned}$$

This is called a magic square because the sums of the elements in each column are the same.

as are the sums of the elements in each row, obtained by transposing:

$$sum(M') = 15 15 15$$

See Also

cumsum Cumulative sum

diff Differences and approximate derivatives

prod Product of array elements trace Sum of diagonal elements

**Purpose** Superior class relationship

**Syntax** superiorto('class1', 'class2',...)

**Description** The superi orto function establishes a hierarchy that determines the order in

which MATLAB calls object methods.

superiorto('class1', 'class2',...) invoked within a class constructor method (say myclass. m) indicates that myclass's method should be invoked if a function is called with an object of class myclass and one or more objects of

class class1, class2, and so on.

**Remarks** Suppose A is of class 'class a', B is of class 'class b' and C is of class

'class\_c'. Also suppose the constructor class\_c. m contains the statement: superiorto('class\_a'). Then e = fun(a, c) or e = fun(c, a) invokes

class\_c/fun.

If a function is called with two objects having an unspecified relationship, the two objects are considered to have equal precedence, and the leftmost object's

method is called. So, fun(b, c) calls class\_b/fun, while fun(c, b) calls

class\_c/fun.

**See Also** inferior to Inferior class relationship

# svd

### **Purpose**

Singular value decomposition

## **Syntax**

### **Description**

The svd command computes the matrix singular value decomposition.

s = svd(X) returns a vector of singular values.

[U, S, V] = svd(X) produces a diagonal matrix S of the same dimension as X, with nonnegative diagonal elements in decreasing order, and unitary matrices U and V so that X = U\*S\*V'.

[U, S, V] = svd(X, 0) produces the "economy size" decomposition. If X is m-by-n with m > n, then svd computes only the first n columns of U and S is n-by-n.

# **Examples**

For the matrix

the statement

$$[U, S, V] = svd(X)$$

### produces

$$S = \begin{bmatrix} 14.2691 & 0 \\ 0 & 0.6268 \\ 0 & 0 \\ 0 & 0 \end{bmatrix}$$

$$V = \begin{bmatrix} 0.6414 & -0.7672 \\ 0.7672 & 0.6414 \end{bmatrix}$$

The economy size decomposition generated by

$$[U, S, V] = svd(X, 0)$$

### produces

### **Algorithm**

The svd command uses the LINPACK routine ZSVDC.

# **Diagnostics**

If the limit of  $75~\mathrm{QR}$  step iterations is exhausted while seeking a singular value, this message appears:

Solution will not converge.

### References

[1] Dongarra, J.J., J.R. Bunch, C.B. Moler, and G.W. Stewart, *LINPACK Users' Guide*, SIAM, Philadelphia, 1979.

A few singular values

### **Syntax**

```
s = svds(A)

s = svds(A, k)

s = svds(A, k, 0)

[U, S, V] = svds(A, ...)
```

### Description

svds(A) computes the five largest singular values and associated singular vectors of the matrix A.

svds(A, k) computes the k largest singular values and associated singular vectors of the matrix A.

 $svds(A,\,k,\,0)-$  computes the k smallest singular values and associated singular vectors.

With one output argument, s is a vector of singular values. With three output arguments and if A is m-by-n:

- U is m-by-k with orthonormal columns
- S is k-by-k diagonal
- V is n-by-k with orthonormal columns
- U\*S\*V' is the closest rank k approximation to A

### **Algorithm**

svds(A, k) uses eigs to find the k largest magnitude eigenvalues and corresponding eigenvectors of B = [0 A; A' 0].

svds(A, k, 0) uses  $ei\ gs$  to find the 2k smallest magnitude eigenvalues and corresponding eigenvectors of  $B = [0\ A;\ A'\ 0]$ , and then selects the k positive eigenvalues and their eigenvectors.

# Example

west 0479 is a real 479-by-479 sparse matrix. svd calculates all 479 singular values. svds picks out the largest and smallest singular values.

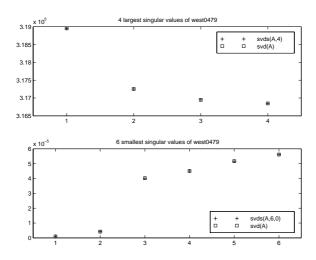
```
load west0479

s = svd(full(west0479))

sl = svds(west0479, 4)

ss = svds(west0479, 6, 0)
```

These plots show some of the singular values of west 0479 as computed by svd and svds.



The largest singular value of west 0479 can be computed a few different ways:

svds(west0479, 1) = 3. 189517598808622e+05

 $\max(\text{svd}(\text{full}(\text{west0479}))) =$ 

3. 18951759880862e+05

norm(full(west0479)) =

3. 189517598808623e+05

and estimated:

normest(west0479) =

3. 189385666549991e+05

See Also

svd ei gs Singular value decomposition Find a few eigenvalues and eigenvectors

Switch among several cases based on expression

### **Syntax**

```
switch switch_expr
  case case_expr
    statement,..., statement
  case {case_expr1, case_expr2, case_expr3,...}
    statement,..., statement
...
  otherwise
    statement,..., statement
end
```

#### Discussion

The switch statement syntax is a means of conditionally executing code. In particular, switch executes one set of statements selected from an arbitrary number of alternatives. Each alternative is called a *case*, and consists of:

- The case statement
- One or more case expressions
- One or more statements

In its most basic syntax, switch executes only the statements associated with the first case where switch\_expr == case\_expr. When the case expression is a cell array (as in the second case above), the case\_expr matches if any of the elements of the cell array match the switch expression. If none of the case expressions matches the switch expression, then control passes to the otherwise case (if it exists). Only one case is executed, and program execution resumes with the statement after the end.

The switch\_expr can be a scalar or a string. A scalar switch\_expr matches a case\_expr if switch\_expr==case\_expr. A string switch\_expr matches a case\_expr if strcmp(switch\_expr, case\_expr) returns 1 (true).

# **Examples** Assume method exists as a string variable:

```
switch lower(method)
   case {'linear','bilinear'}, disp('Method is linear')
   case 'cubic', disp('Method is cubic')
   case 'nearest', disp('Method is nearest')
   otherwise, disp('Unknown method.')
end
```

# **See Also** case, end, if, otherwise, while

# symmmd

**Purpose** 

Sparse symmetric minimum degree ordering

Syntax

p = symmmd(S)

**Description** 

p = symmmd(S) returns a symmetric minimum degree ordering of S. For a symmetric positive definite matrix S, this is a permutation p such that S(p,p) tends to have a sparser Cholesky factor than S. Sometimes symmetric indefinite matrices too.

Remarks

The minimum degree ordering is automatically used by  $\setminus$  and / for the solution of symmetric, positive definite, sparse linear systems.

Some options and parameters associated with heuristics in the algorithm can be changed with spparms.

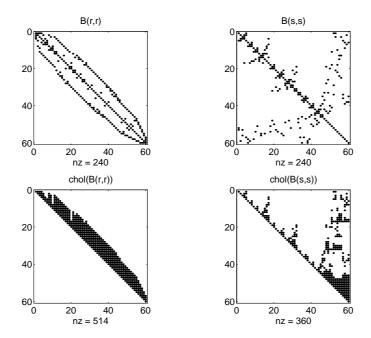
**Algorithm** 

The symmetric minimum degree algorithm is based on the column minimum degree algorithm. In fact,  $\operatorname{symmmd}(A)$  just creates a nonzero structure K such that K' \*K has the same nonzero structure as A and then calls the column minimum degree code for K.

**Examples** 

Here is a comparison of reverse Cuthill-McKee and minimum degree on the Bucky ball example mentioned in the symrom reference page.

```
B = bucky+4*speye(60);
r = symrcm(B);
p = symmmd(B);
R = B(r,r);
S = B(p,p);
subplot(2,2,1), spy(R), title('B(r,r)')
subplot(2,2,2), spy(S), title('B(s,s)')
subplot(2,2,3), spy(chol(R)), title('chol(B(r,r))')
subplot(2,2,4), spy(chol(S)), title('chol(B(s,s))')
```



Even though this is a very small problem, the behavior of both orderings is typical. RCM produces a matrix with a narrow bandwidth which fills in almost completely during the Cholesky factorization. Minimum degree produces a structure with large blocks of contiguous zeros which do not fill in during the factorization. Consequently, the minimum degree ordering requires less time and storage for the factorization.

See Also

col mmd	Sparse column minimum degree permutation
colperm	Sparse column permutation based on nonzero count
symrcm	Sparse reverse Cuthill-McKee ordering

References

[1] Gilbert, John R., Cleve Moler, and Robert Schreiber, "Sparse Matrices in MATLAB: Design and Implementation," *SIAM Journal on Matrix Analysis and Applications* 13, 1992, pp. 333-356.

Sparse reverse Cuthill-McKee ordering

Syntax

r = symrcm(S)

Description

r = symrcm(S) returns the symmetric reverse Cuthill-McKee ordering of S. This is a permutation r such that S(r,r) tends to have its nonzero elements closer to the diagonal. This is a good preordering for LU or Cholesky factorization of matrices that come from long, skinny problems. The ordering works for both symmetric and nonsymmetric S.

For a real, symmetric sparse matrix, S, the eigenvalues of S(r,r) are the same as those of S, but eig(S(r,r)) probably takes less time to compute than eig(S).

**Algorithm** 

The algorithm first finds a pseudoperipheral vertex of the graph of the matrix. It then generates a level structure by breadth-first search and orders the vertices by decreasing distance from the pseudoperipheral vertex. The implementation is based closely on the SPARSPAK implementation described by George and Liu.

**Examples** 

The statement

B = bucky

uses an M-file in the demos toolbox to generate the adjacency graph of a truncated icosahedron. This is better known as a soccer ball, a Buckminster Fuller geodesic dome (hence the name bucky), or, more recently, as a 60-atom carbon molecule. There are 60 vertices. The vertices have been ordered by numbering half of them from one hemisphere, pentagon by pentagon; then reflecting into the other hemisphere and gluing the two halves together. With this numbering, the matrix does not have a particularly narrow bandwidth, as the first spy plot shows

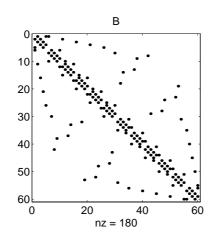
```
subplot(1, 2, 1), spy(B), title('B')
```

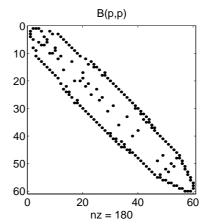
The reverse Cuthill-McKee ordering is obtained with

```
p = symrcm(B);
R = B(p, p);
```

The spy plot shows a much narrower bandwidth:

$$subplot(1, 2, 2), spy(R), title('B(p, p)')$$





This example is continued in the reference pages for symmmd.

The bandwidth can also be computed with

$$[i,j] = find(B);$$
  
 $bw = max(i-j) + 1$ 

The bandwidths of B and R are 35 and 12, respectively.

#### See Also

col mmd
col perm
cammmd

Sparse column minimum degree permutation Sparse column permutation based on nonzero count Sparse symmetric minimum degree ordering

#### References

[1] George, Alan and Joseph Liu, *Computer Solution of Large Sparse Positive Definite Systems*, Prentice-Hall, 1981.

[2] Gilbert, John R., Cleve Moler, and Robert Schreiber, "Sparse Matrices in MATLAB: Design and Implementation," to appear in *SIAM Journal on Matrix Analysis*, 1992. A slightly expanded version is also available as a technical report from the Xerox Palo Alto Research Center.

Tangent and hyperbolic tangent

**Syntax** 

$$Y = tan(X)$$
  
 $Y = tanh(X)$ 

**Description** 

The tan and tanh functions operate element-wise on arrays. The functions' domains and ranges include complex values. All angles are in radians.

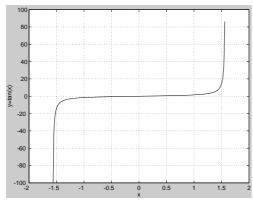
Y = tan(X) returns the circular tangent of each element of X.

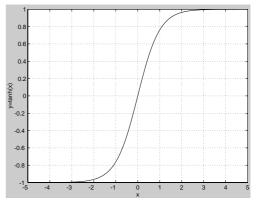
Y = tanh(X) returns the hyperbolic tangent of each element of X.

**Examples** 

Graph the tangent function over the domain  $-\pi/2 < x < \pi/2$ , and the hyperbolic tangent function over the domain  $-5 \le x \le 5$ .

$$x = (-pi/2) + 0.01: 0.01: (pi/2) - 0.01; plot(x, tan(x))$$
  
 $x = -5: 0.01: 5; plot(x, tanh(x))$ 





The expression tan(pi/2) does not evaluate as infinite but as the reciprocal of the floating point accuracy eps since pi is only a floating-point approximation to the exact value of  $\pi$ .

# **Algorithm**

$$tan(z) = \frac{\sin(z)}{\cos(z)}$$
$$tanh(z) = \frac{\sinh(z)}{\cosh(z)}$$

See Also atan, atan2

# tempdir

**Purpose** Return the name of the system's temporary directory

**Description**  $tmp_dir = tempdir$  returns the name of the system's temporary directory, if

one exists. This function does not create a new directory.

**See Also** tempname Unique name for temporary file

# tempname

**Purpose** Unique name for temporary file

Syntax tempname

**Description** tempname returns a unique string beginning with the characters tp. This

string is useful as a name for a temporary file.

**See Also** tempdi r Return the name of the system's temporary directory

Stopwatch timer

**Syntax** 

tic

any statements

toc

t = toc

Description

 $tic\ starts\ a\ stopwatch\ timer.$ 

toc prints the elapsed time since tic was used.

t = toc returns the elapsed time in t.

**Examples** 

This example measures how the time required to solve a linear system varies with the order of a matrix.

```
for n = 1:100
    A = rand(n, n);
    b = rand(n, 1);
    tic
    x = A\b;
    t(n) = toc;
end
plot(t)
```

See Also

clock Current time as a date vector

cputime Elapsed CPU time etime Elapsed time

Toeplitz matrix

### Syntax

```
T = toeplitz(c, r)
T = toeplitz(r)
```

### Description

A *Toeplitz* matrix is defined by one row and one column. A *symmetric Toeplitz* matrix is defined by just one row. toeplitz generates Toeplitz matrices given just the row or row and column description.

T = toeplitz(c, r) returns a nonsymmetric Toeplitz matrix T having c as its first column and r as its first row. If the first elements of c and r are different, a message is printed and the column element is used.

T = toeplitz(r) returns the symmetric or Hermitian Toeplitz matrix formed from vector r, where r defines the first row of the matrix.

### **Examples**

A Toeplitz matrix with diagonal disagreement is

```
c = [1 \ 2 \ 3 \ 4 \ 5];
r = [1.5 \ 2.5 \ 3.5 \ 4.5 \ 5.5];
toeplitz(c, r)
Column wins diagonal conflict:
ans =
              2.500
    1.000
                        3.500
                                  4.500
                                            5.500
    2.000
              1.000
                        2.500
                                  3.500
                                            4.500
    3.000
              2.000
                        1.000
                                  2.500
                                            3.500
    4.000
              3.000
                        2.000
                                  1.000
                                            2.500
    5.000
              4.000
                        3.000
                                  2.000
                                            1.000
```

See Also

hankel

Hankel matrix

# trace

**Purpose** Sum of diagonal elements

**Syntax** b = trace(A)

**Description** b = trace(A) is the sum of the diagonal elements of the matrix A.

**Algorithm** trace is a single-statement M-file.

t = sum(diag(A));

See Also det Matrix determinant

ei g Eigenvalues and eigenvectors

Trapezoidal numerical integration

### **Syntax**

Z = trapz(Y)
Z = trapz(X, Y)
Z = trapz(..., di m)

### **Description**

Z = trapz(Y) computes an approximation of the integral of Y via the trapezoidal method (with unit spacing). To compute the integral for spacing other than one, multiply Z by the spacing increment.

If Y is a vector, trapz(Y) is the integral of Y.

If Y is a matrix, trapz(Y) is a row vector with the integral over each column.

If Y is a multidimensional array, trapz(Y) works across the first nonsingleton dimension.

Z = trapz(X, Y) computes the integral of Y with respect to X using trapezoidal integration.

If X is a column vector and Y an array whose first nonsingleton dimension is length(X), trapz(X, Y) operates across this dimension.

Z = trapz(..., dim) integrates across the dimension of Y specified by scalar dim. The length of X, if given, must be the same as size(Y, dim).

# **Examples**

The exact value of  $\int_0^{\pi} \sin(x) dx$  is 2.

To approximate this numerically on a uniformly spaced grid, use

X = 0: pi/100: pi;Y = sin(x);

Then both

Z = trapz(X, Y)

and

Z = pi/100\*trapz(Y)

produce

Z = 1.9998

A nonuniformly spaced example is generated by

```
X = sort(rand(1, 101)*pi);
Y = sin(X);
Z = trapz(X, Y);
```

The result is not as accurate as the uniformly spaced grid. One random sample produced  $% \left\{ 1\right\} =\left\{ 1\right\} =\left\{$ 

Z = 1.9984

See Also

cumsum

cumtrapz Cumulative trapezoidal numerical integration

**Cumulative sum** 

Lower triangular part of a matrix

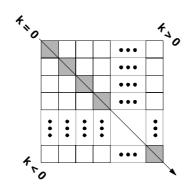
**Syntax** 

$$L = tril(X)$$
  
 $L = tril(X, k)$ 

Description

L = tril(X) returns the lower triangular part of X.

 $L=\mbox{tril}\,(X,\,k)~$  returns the elements on and below the kth diagonal of X. k=0 is the main diagonal, k>0 is above the main diagonal, and k<0 is below the main diagonal.



**Examples** 

tril(ones(4,4),-1) is

0	0	0
0	0	0
1	0	0
1	1	0
	0	0 0 1 0

See Also

di ag tri u Diagonal matrices and diagonals of a matrix Upper triangular part of a matrix

# triu

**Purpose** 

Upper triangular part of a matrix

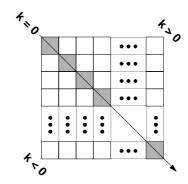
**Syntax** 

U = triu(X)U = triu(X, k)

**Description** 

U = tri u(X) returns the upper triangular part of X.

 $U=tri\,u(X,\,k)$  returns the element on and above the kth diagonal of X. k=0 is the main diagonal, k>0 is above the main diagonal, and k<0 is below the main diagonal.



**Examples** 

triu(ones(4,4),-1) is

1	1	1	1
1	1	1	1
0	1	1	1
0	0	1	1

See Also

di ag tri l Diagonal matrices and diagonals of a matrix Lower triangular part of a matrix **Purpose** Search for enclosing Delaunay triangle

**Syntax** T = tsearch(x, y, TRI, xi, yi)

**Description** T = tsearch(x, y, TRI, xi, yi) returns an index into the rows of TRI for each

point in xi,yi. The tsearch command returns NaN for all points outside the convex hull. Requires a triangulation TRI of the points x,y obtained from

del aunay.

See Also del aunay Delaunay triangulation

dsearch Search for nearest point

# type

Purpose List file

**Syntax** type filename

**Description** type *filename* displays the contents of the specified file in the MATLAB

 $command\ window\ given\ a\ full\ pathname\ or\ a\ {\tt MATLABPATH}\ relative\ partial\ path-$ 

name. Use pathnames and drive designators in the usual way for your

computer's operating system.

If you do not specify a filename extension, the type command adds the .m exten-

sion by default. The type command checks the directories specified in

MATLAB's search path, which makes it convenient for listing the contents of

M-files on the screen.

**Examples** type foo. bar lists the file foo. bar.

type foo lists the file foo. m.

See Also ! Operating system command

cd Change working directory
dbtype List M-file with line numbers
del et e Delete files and graphics objects

di r Directory listing

path Control MATLAB's directory search path

what Directory listing of M-files, MAT-files, and MEX-files

who List directory of variables in memory

See also partial path.

Purpose Convert to unsigned 8-bit integer

Syntax i = uint8(x)

Description

i = uint8(x) converts the vector x into an unsigned 8-bit integer. x can be any numeric object (such as a double). The elements of an uint8 range from 0 to 255. The result for any elements of x outside this range is not defined (and may vary from platform to platform). If x is already an unsigned 8-bit integer, uint8 has no effect.

The ui nt8 class is primarily meant to store integer values. Most operations that manipulate arrays without changing their elements are defined (examples are reshape, si ze, subscripted assignment and subscripted reference). No math operations are defined for ui nt8 since such operations are ambiguous on the boundary of the set (for example they could wrap or truncate there). You can define your own methods for ui nt8 (as you can for any object) by placing the appropriately named method in an <code>@ui</code> nt8 directory within a directory on your path. The Image Processing Toolbox does just that to define additional methods for the ui nt8 (such as the logical operators <,>,&, etc.).

Type help oopfun for the names of the methods you can overload.

See Also double Convert to double precision

Set union of two vectors

### **Syntax**

```
c = uni on(a, b)
c = uni on(A, B, 'rows')
[c, i a, i b] = uni on(...)
```

1

2

3

### **Description**

 $c = uni\ on(a,b)$  returns the combined values from a and b but with no repetitions. The resulting vector is sorted in ascending order. In set theoretic terms,  $c = a \cup b$ .

 $c=uni\ on(A,B,'rows')\ when\ A\ and\ B\ are\ matrices\ with\ the\ same\ number\ of\ columns\ returns\ the\ combined\ rows\ from\ A\ and\ B\ with\ no\ repetitions.$ 

[c, ia, ib] = union(...) also returns index vectors ia and ib such that c = a(ia) and c = b(ib) or, for row combinations, c = a(ia, :) and c = b(ib, :).

### **Examples**

### See Also

intersect Set intersection of two vectors setdiff Return the set difference of two vectors setxor Set exclusive-or of two vectors unique Unique elements of a vector

4

Unique elements of a vector

**Syntax** 

b = uni que(a)
b = uni que(A, 'rows')
[b, i ndex] = uni que(...)

**Description** 

 $b = uni \, que(a)$  returns the same values as in a but with no repetitions. The resulting vector is sorted in ascending order.

b = uni que(A, 'rows') returns the unique rows of A.

[b, i, j] = uni que(...) also returns index vectors i and j such that b = a(i) and a = b(j) (or b = a(i, :) and a = b(j, :)).

**Examples** 

a =	[1 1	5 6 2	3 3 9	8 6 2	4]						
a =											
1	1	5	6	2	3	3	9	8	6	2	4
[ b, i	i,j] =	= uni qເ	ıe(a)								
b =											
	1	2	3	4	5	6	8	9			
i =											
	2	11	7	12	3	10	9	8			
j =											
1	1	5	6	2	3	3	8	7	6	2	4
a(i)	)										
ans	=										
	1	2	3	4	5	6	8	9			
b(j)	)										
ans	=										
1	1	5	6	2	3	3	9	8	6	2	4

See Also

intersect Set intersection of two vectors
i smember True for a set member
set diff Return the set difference of two vectors
setxor Set exclusive-or of two vectors
uni on Set union of two vectors

Correct phase angles

### **Syntax**

Q = unwrap(P)

Q = unwrap(P, tol)

Q = unwrap(P, [], dim)

Q = unwrap(P, tol, dim)

### Description

Q=unwrap(P) corrects the radian phase angles in array P by adding multiples of  $\pm 2\pi$  when absolute jumps between consecutive array elements are greater than  $\pi$  radians. If P is a matrix, unwrap operates columnwise. If P is a multidimensional array, unwrap operates on the first nonsingleton dimension.

Q = unwrap(P, tol) uses a jump tolerance tol instead of the default value,  $\pi$ .

Q = unwrap(P, [], dim) unwraps along dim using the default tolerance.

Q = unwrap(P, tol, dim) uses a jump tolerance of tol.

### **Examples**

Array P features smoothly increasing phase angles except for discontinuities at elements (3, 1) and (1, 2).

P =				
	0	<u>7. 0686</u>	1.5708	2. 3562
(	0. 1963	0. 9817	1. 7671	2. 5525
6	<u> 6. 6759</u>	1. 1781	1.9635	2. 7489
(	0. 5890	1. 3744	2. 1598	2. 9452

The function Q = unwrap(P) eliminates these discontinuities.

### Limitations

The unwrap function detects branch cut crossings, but it can be fooled by sparse, rapidly changing phase values.

### See Also

abs Absolute value and complex magnitude angle Phase angle

**Purpose** Convert string to upper case

**Syntax** t = upper('str')

**Description** t = upper('str') converts any lower-case characters in the string str to

the corresponding upper-case characters and leaves all other characters

unchanged.

**Examples** upper('attention!') is ATTENTION!.

**Remarks** Character sets supported:

Mac: Standard RomanPC: Windows Latin-1

• Other: ISO Latin-1 (ISO 8859-1)

**See Also** lower Convert string to lower case

Pass or return variable numbers of arguments

### **Syntax**

```
function varargout = foo(n)
y = function bar(varargin)
```

### **Description**

function varargout = foo(n) returns a variable number of arguments from function foo. m.

 $y = function \ bar(varargin)$  accepts a variable number of arguments into function bar. m.

The varargi n and varargout statements are used only inside a function M-file to contain the optional arguments to the function. Each must be declared as the last argument to a function, collecting all the inputs or outputs from that point onwards. In the declaration, varargi n and varargout must be lowercase.

### **Examples**

The function

```
function myplot(x, varargin)
plot(x, varargin{:})
```

collects all the inputs starting with the second input into the variable varargi n. mypl ot uses the comma-separated list syntax varargi n $\{:\}$  to pass the optional parameters to pl ot. The call

```
myplot(sin(0:.1:1), 'color', [.5.7.3], 'linestyle', ':')
```

results in varargin being a 1-by-4 cell array containing the values ' color', [.5 .7 .3], 'linestyle', and ':'.

The function

```
function [s, varargout] = mysize(x)
nout = max(nargout, 1) - 1;
s = size(x);
for i = 1: nout, varargout(i) = {s(i)}; end
```

returns the size vector and, optionally, individual sizes. So

```
[s, rows, cols] = mysize(rand(4, 5));
returns s = [4 5], rows = 4, cols = 5.
```

# varargin, varargout

See Also	nargi n	Number of function arguments
	nargout	Number of function arguments
	nargchk	Check number of input arguments

# vectorize

**Purpose** Vectorize expression

**Syntax** vectorize(string)

vectori ze(functi on)

**Description** vectorize(string) inserts a . before any ^, \* or / in string. The result is a

character string.

vectorize(function) when function is an inline function object, vectorizes the formula for function. The result is the vectorized version of the inline func-

tion.

See Also inline Construct an inline object

**Purpose** MATLAB version number

**Syntax** v = version

[v, d] = version

**Description** v = versi on returns a string v containing the MATLAB version number.

[v, d] = versi on also returns a string d containing the date of the version.

**See Also** hel p Online help for MATLAB functions and M-files

whatsnew Display README files for MATLAB and toolboxes

versi on MATLAB version number

### voronoi

# Purpose Voronoi diagram

### Syntax

```
voronoi (x, y)
voronoi (x, y, TRI)
```

h = voronoi(..., 'LineSpec')
[vx, vy] = voronoi(...)

### **Definition**

Consider a set of coplanar points P. For each point  $P_X$  in the set P, you can draw a boundary enclosing all the intermediate points lying closer to  $P_X$  than to other points in the set P. Such a boundary is called a *Voronoi polygon*, and the set of all Voronoi polygons for a given point set is called a *Voronoi diagram*.

### **Description**

voronoi (x, y) plots the Voronoi diagram for the points x,y.

 $voronoi \ (x,y,TRI) \ uses \ the \ triangulation \ TRI \ instead \ of \ computing \ it \ via \ del \ aunay.$ 

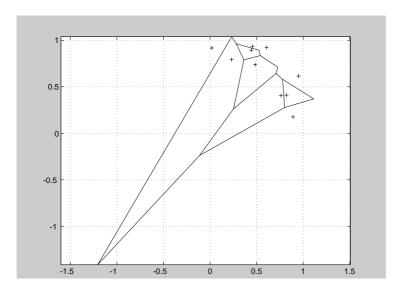
h = voronoi (..., 'Li neSpec') plots the diagram with color and line style specified and returns handles to the line objects created in h.

[vx, vy] = voronoi(...) returns the vertices of the Voronoi edges in vx and vy so that plot(vx, vy, '-', x, y, '.') creates the Voronoi diagram.

# **Examples**

This code plots the Voronoi diagram for  $10\ randomly\ generated\ points.$ 

```
rand('state',0);
x = rand(1,10); y = rand(1,10);
[vx, vy] = voronoi(x,y);
plot(x,y,'r+',vx,vy,'b-'); axis equal
```



### See Also

The Li neSpec entry in Using MATLAB Graphics, and

convhul l	Convex hull
del aunay	Delaunay triangulation
dsearch	Search for nearest point

# warning

Purpose Display warning message

**Syntax** warni ng(' message')

warning on warning off

warning backtrace
warning debug
warning once
warning always
[s, f] = warning

**Description** warning('message') displays the text 'message' as does the disp function,

except that with warning, message display can be suppressed.

warning off suppresses all subsequent warning messages.

warning on re-enables them.

warning backtrace is the same as warning on except that the file and line number that produced the warning are displayed.

warning debug is the same as dbstop if warning and triggers the debugger when a warning is encountered.

warning once displays Handle Graphics backwards compatibility warnings only once per session.

warning al ways displays Handle Graphics backwards compatibility warnings as they are encountered (subject to current warning state).

[s, f] = warning returns the current warning state s and the current warning frequency f as strings.

**Remarks** Use dbst op on warning to trigger the debugger when a warning is encoun-

tered.

**See Also** dbstop Set breakpoints in an M-file function

di sp Display text or array error Display error messages

Read Microsoft WAVE (. wav) sound file

### **Syntax**

```
y = wavread('filename')
[y, Fs, bits] = wavread('filename')
[...] = wavread('filename', N)
[...] = wavread('filename', [N1 N2])
[...] = wavread('filename', 'size')
```

### Description

wavread supports multichannel data, with up to 16 bits per sample.

y = wavread('filename') loads a WAVE file specified by the string filename, returning the sampled data in y. The . wav extension is appended if no extension is given. Amplitude values are in the range [-1, +1].

[y, Fs, bits] = wavread('filename') returns the sample rate (Fs) in Hertz and the number of bits per sample (bits) used to encode the data in the file.

 $[\dots] = wavread('filename', N)$  returns only the first N samples from each channel in the file.

 $[\dots] = wavread('filename', [N1 N2])$  returns only samples N1 through N2 from each channel in the file.

siz = wavread('filename', 'size') returns the size of the audio data contained in the file in place of the actual audio data, returning the vector siz = [samples channels].

#### See Also

auread Read NeXT/SUN (. au) sound file wavwrite Write Microsoft WAVE (. wav) sound file

# wavwrite

Purpose Write Microsoft WAVE (. wav) sound file

**Syntax** wavwrite(y, 'filename')

wavwrite(y, Fs, 'filename')
wavwrite(y, Fs, N, 'filename')

**Description** wavwrite supports multi-channel 8- or 16-bit WAVE data.

wavwrite(y,'filename') writes a WAVE file specified by the string filename. The data should be arranged with one channel per column. Amplitude values

outside the range [-1, +1] are clipped prior to writing.

wavwrite(y, Fs, 'filename') specifies the sample rate Fs, in Hertz, of the

data.

wavwrite(y, Fs, N, 'filename') forces an N-bit file format to be written, where

 $N \ll 16$ .

See Also Write NeXT/SUN (. au) sound file

wavread Read Microsoft WAVE (. wav) sound file

**Purpose** Point Web browser at file or Web site

Syntax web url

**Description** web *url* opens a Web browser and loads the file or Web site specified in the

URL (Uniform Resource Locator). The URL can be in any form your browser supports. Generally, the URL specifies a local file or a Web site on the Internet.

**Examples** web file:  $\frac{di sk}{di r^2}$  foo. html points the browser to the file foo. html.

If the file is on the MATLAB path, web(['file:' which('foo. html')]) also

works.

web http://www.mathworks.com loads The MathWorks Web page into your browser. Use web mailto:email address to send e-mail to another site.

The Web browser used is specified in the docopt M-file.

**See Also** doc Load hypertext documentation

docopt Configure local doc access defaults (in online help)

# weekday

Purpose

Day of the week

**Syntax** 

[N, S] = weekday(D)

**Description** 

[N, S] = weekday(D) returns the day of the week in numeric (N) and string (S) form for each element of a serial date number array or date string. The days of the week are assigned these numbers and abbreviations:

N	S	N	S
1	Sun	5	Thu
2	Mon	6	Fri
3	Tue	7	Sat
4	Wed		

**Examples** 

Either

[n, s] = weekday(728647)

or

[n, s] = weekday('19-Dec-1994')

returns n = 2 and s = Mon.

See Also

datenum Serial date number datevec Date components eomday End of month

**Purpose** Directory listing of M-files, MAT-files, and MEX-files

Syntax what

what dirname

**Description** what by itself, lists the M-files, MAT-files, and MEX-files in the current direc-

tory.

what *di rname* lists the files in directory *di rname* on MATLAB's search path. It is not necessary to enter the full pathname of the directory. The last component, or last couple of components, is sufficient. Use what *class* or what *di rname*/pri vate to list the files in a method directory or a private directory

(for the class named *class*).

**Examples** The statements

what general

and

what matlab/general

both list the M-files in the general directory. The syntax of the path depends

on your operating system:

UNIX: matlab/general
VMS: MATLAB. GENERAL
MS-DOS: MATLAB\GENERAL
Macintosh: MATLAB: General

See Also di r Directory listing

lookfor Keyword search through all help entries path Control MATLAB's directory search path

whi ch Locate functions and files

who List directory of variables in memory

### whatsnew

**Purpose** Display README files for MATLAB and toolboxes

Syntax whatsnew

whatsnew matlab

whatsnew tool boxpath

**Description** what snew, by itself, displays the README file for the MATLAB product or a spec-

ified toolbox. If present, the README file summarizes new functionality that is

not described in the documentation.

whatsnew matlab displays the README file for MATLAB.

what snew tool boxpath displays the README file for the toolbox specified by the

string tool boxpath.

**Examples** whatsnew matlab % MATLAB README file

whatsnew signal % Signal Processing Toolbox README file

**See Also** hel p Online help for MATLAB functions and M-files

l ookfor Keyword search through all help entries path Control MATLAB's directory search path

versi on MATLAB version number whi ch Locate functions and files

Locate functions and files

### **Syntax**

```
whi ch fun
whi ch fun -all
whi ch file.ext
whi ch fun1 in fun2
whi ch fun(a, b, c, ...)
s = whi ch(...)
```

### Description

which *fun* displays the full pathname of the specified function. The function can be an M-file, MEX-file, workspace variable, built-in function, or SIMULINK model. The latter three display a message indicating that they are variable, built in to MATLAB, or are part of SIMULINK. Use which private/*fun* or which *class/fun* or which *class/pri* vate/*fun* to further qualify the function name for private functions, methods, and private methods (for the class named *class*).

which fun—all displays the paths to all functions with the name fun. The first one in the list is the one normally returned by which. The others are either shadowed or can be executed in special circumstances. The—all flag can be used with all forms of which.

which file. ext displays the full pathname of the specified file.

which fun1 in fun2 displays the pathname to function fun1 in the context of the M-file fun2. While debugging fun2, which fun1 does the same thing. You can use this to determine if a local or private version of a function is being called instead of a function on the path.

which fun(a, b, c, ...) displays the path to the specified function with the given input arguments. For example, which feval (g), when g=i nl i ne('sin(x)'), indicates that i nl i ne/feval. m is invoked.

 $s = whi \ ch(\dots)$  returns the results of whi ch in the string s instead of printing it to the screen. s will be the string built-in or variable for built-in functions or variables in the workspace. You must use the functional form of which when there is an output argument.

### which

### **Examples**

For example,

which inv

reveals that i nv is a built-in function, and

which pinv

indicates that pi nv is in the matfun directory of the MATLAB Toolbox.

The statement

whi ch j acobi an

probably says

jacobian not found

because there is no file j acobi an.m on MATLAB's search path. Contrast this with lookfor j acobi an, which takes longer to run, but finds several matches to the keyword j acobi an in its search through all the help entries. (If j acobi an. m does exist in the current directory, or in some private directory that has been added to MATLAB's search path, which j acobi an finds it.)

### See Also

dir, exist, help, lookfor, path, what, who

Repeat statements an indefinite number of times

### Syntax

while expression statements

### Description

while repeats statements an indefinite number of times. The statements are executed while the real part of *expressi on* has all nonzero elements. *expressi on* is usually of the form

```
expressi on rop expressi on where rop is ==, <, >, <=, >=, or ^\sim=.
```

The scope of a while statement is always terminated with a matching end.

### **Examples**

The variable eps is a tolerance used to determine such things as near singularity and rank. Its initial value is the *machine epsilon*, the distance from 1.0 to the next largest floating-point number on your machine. Its calculation demonstrates while loops:

```
eps = 1;
while (1+eps) > 1
    eps = eps/2;
end
eps = eps*2
```

#### See Also

all Test to determine if all elements are nonzero

any Test for any nonzeros

break Break out of flow control structures

end Terminate for, while, switch, and if statements or

indicate last index

for Repeat statements a specific number of times

if Conditionally execute statements return Return to the invoking function

switch Switch among several cases based on expression

List directory of variables in memory

### **Syntax**

```
who
whos
who global
whos global
who -file filename
whos -file filename
who ... var1 var2
whos ... var1 var2
s = who(...)
s = whos(...)
```

### Description

who by itself, lists the variables currently in memory.

whos by itself, lists the current variables, their sizes, and whether they have nonzero imaginary parts.

who global and whos global list the variables in the global workspace.

who -file *filename* and whos -file *filename* list the variables in the specified MAT-file.

who ... var1 var2 and whos ... var1 var2 restrict the display to the variables specified. The wildcard character \* can be used to display variables that match a pattern. For instance, who A\* finds all variables in the current workspace that start with A. Use the functional form, such as whos ('-file', filename, v1, v2), when the filename or variable names are stored in strings.

 $s=who(\ldots)$  returns a cell array containing the names of the variables in the workspace or file. Use the functional form of who when there is an output argument.

s = whos(...) returns a structure with the fields:

name variable name

bytes number of bytes allocated for the array

class of variable

Use the functional form of whos when there is an output argument.

See Also dir, exist, help, what

# wilkinson

Purpose Wilkinson's eigenvalue test matrix

**Syntax** W = wilkinson(n)

**Description** W = wilkinson(n) returns one of J. H. Wilkinson's eigenvalue test matrices.

It is a symmetric, tridiagonal matrix with pairs of nearly, but not exactly, equal

eigenvalues.

**Examples** wilkinson(7) is

The most frequently used case is wilkinson(21). Its two largest eigenvalues are both about 10.746; they agree to 14, but not to 15, decimal places.

**See Also** eig Eigenvalues and eigenvectors

gallery Test matrices pascal Pascal matrix

Read a Lotus123 WK1 spreadsheet file into a matrix

**Syntax** 

M = wk1read(filename)

M = wk1read(filename, r, c)

M = wk1read(filename, r, c, range)

Description

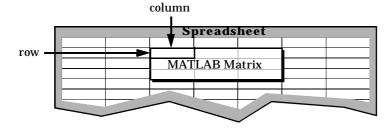
M = wk1read(filename) reads a Lotus123 WK1 spreadsheet file into the matrix M.

M = wk1read(filename, r, c) starts reading at the row-column cell offset specified by (r, c). r and c are zero based so that r=0, c=0 specifies the first value in the file.

M = wk1read(filename, r, c, range) reads the range of values specified by the parameter range, where range can be:

• A four-element vector specifying the cell range in the format

 $[upper\_left\_row\ upper\_left\_col\ lower\_right\_row\ lower\_right\_col\,]$ 



- $\bullet$  A cell range specified as a string; for example, '  $A1\dots C5'$  .
- $\bullet$  A named range specified as a string; for example, '  $Sal\ es'$  .

See Also

wk1write

Write a matrix to a Lotus123 WK1 spreadsheet file

# wk1write

**Purpose** Write a matrix to a Lotus123 WK1 spreadsheet file

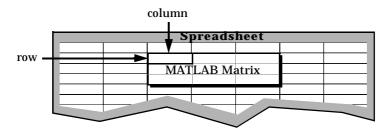
**Syntax** wk1write(filename, M)

wk1write(filename, M, r, c)

**Description** wk1write(filename, M) writes the matrix Minto a Lotus123 WK1 spreadsheet

file named filename.

wk1write(filename, M, r, c) writes the matrix starting at the spreadsheet location (r, c). r and c are zero based so that r=0, c=0 specifies the first cell in the spreadsheet.



See Also wk1read

Read a Lotus 123 WK1 spreadsheet file into a matrix

# writesnd

**Purpose** Write snd resources and files

**Syntax** writesnd(data, samplerate, bitspersample, *filename*)

**Description** writesnd(data, samplerate, bitspersample, filename) writes the sound

information specified by data and samplerate into an snd resource in

filename.

**Example** writesnd(y, Fs, 16, 'gong. snd')

# xlgetrange

**Purpose** Get range of cells from Microsoft Excel worksheet

**Syntax** xl getrange([rmi n, cmi n, rmax, cmax], workbookname, worksheetnum)

**Description** xl getrange([rmin, cmin, rmax, cmax], workbookname, worksheetnum)

 $returns \ the \ data \ in \ the \ range \ r< rmi \ n>c < cmi \ n>: \ r< rmax>c < cmax> of \ sheet$  worksheet num of the Microsoft Excel workbook workbookname. worksheet num

defaults to 1 if not specified. Only numerical data is supported.

**See Also** appl escript Load a compiled AppleScript from a file and execute it

xl set range Set range of cells in Microsoft Excel worksheet

# xlsetrange

**Purpose** Set range of cells in Microsoft Excel worksheet

**Syntax** xl setrange(data, [rmin, cmin, rmax, cmax], workbookname, worksheetnum)

**Description** xl setrange(data, [rmi n, cmi n, rmax, cmax], workbookname, worksheetnum)

sets the cells in the range r<rmi n>c<cmi n>: r<rmax>c<cmax> of sheet worksheet num of the Microsoft Excel workbook workbookname to data.

worksheet num defaults to 1 if not specified. Only numerical data is supported.

See Also appl escript Load a compiled AppleScript from a file and execute it

xl getrange Get range of cells from Microsoft Excel worksheet

### xor

**Purpose** 

Exclusive or

Syntax

C = xor(A, B)

**Description** 

C = xor(A, B) performs an exclusive OR operation on the corresponding elements of arrays A and B. The resulting element C(i, j, ...) is logical true (1) if A(i, j, ...) or B(i, j, ...), but not both, is nonzero.

Α	В	С
zero	zero	0
zero	nonzero	1
nonzero	zero	1
nonzero	nonzero	0

**Examples** 

Given  $A = [0 \ 0 \ pi \ eps]$  and  $B = [0 \ -2.4 \ 0 \ 1]$ , then

To see where either A or B has a nonzero element and the other matrix does not,

spy(xor(A, B))

See Also

& Logical AND operator
| Logical OR operator

all Test to determine if all elements are nonzero

any Test for any nonzeros

find Find indices and values of nonzero elements

Create an array of all zeros

### **Syntax**

```
B = zeros(n)
```

B = zeros(m, n)

B = zeros([m n])

B = zeros(d1, d2, d3...)

B = zeros([d1 d2 d3...])

B = zeros(size(A))

### Description

B = zeros(n) returns an n-by-n matrix of zeros. An error message appears if n is not a scalar.

B = zeros(m, n) or B = zeros([m n]) returns an m-by-n matrix of zeros.

B = zeros(d1, d2, d3...) or  $B = zeros([d1 \ d2 \ d3...])$  returns an array of zeros with dimensions d1-by-d2-by-d3-by-...

B = zeros(size(A)) returns an array the same size as A consisting of all zeros.

#### Remarks

The MATLAB language does not have a dimension statement—MATLAB automatically allocates storage for matrices. Nevertheless, most MATLAB programs execute faster if the zeros function is used to set aside storage for a matrix whose elements are to be generated one at a time, or a row or column at a time.

### **Examples**

With n = 1000, the for loop

for 
$$i = 1$$
:  $n$ ,  $x(i) = i$ ; end

takes about 1.2 seconds to execute on a Sun SPARC-1. If the loop is preceded by the statement x = zeros(1, n); the computations require less than 0.2 seconds.

#### See Also

eye Identity matrix

ones Create an array of all ones

rand Uniformly distributed random numbers and arrays randn Normally distributed random numbers and arrays



# **List of Commands**

This appendix lists MATLAB commands and functions alphabetically. For a list of commands grouped by functional category, see the Command Summary.

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